

Poisson Blending



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P2...

Will be released
tomorrow...

GPU Tricks



Topics?

Intelligent Blending

Demo:



Example:



→
Kernel



→
Kernel



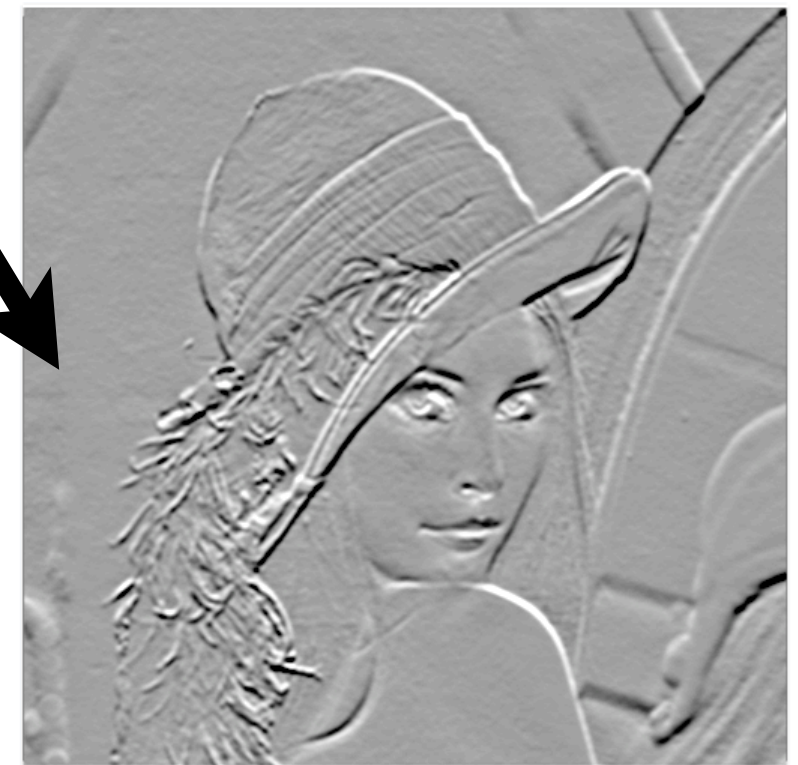
→
Kernel



How Can We Do This?

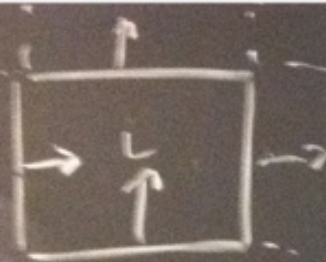
- Think of *any* sort of algorithm which could do this!
- If we expressed this as an *objective function*, what would it be?
- What is the minimum of this function?
- How could we compute this efficiently?





How can we
store this?

Poisson Blending

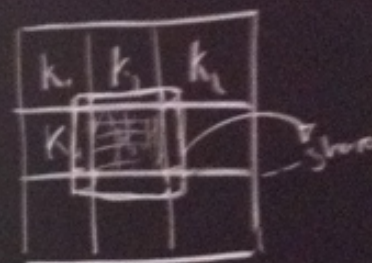


$\vec{x} \triangleq$ the image we're solving for.

$\Delta_{ij} \triangleq$ gradients from the image we're pasting (constant)

$$\phi = \frac{1}{2} \sum_i \sum_{j \sim i} \left[x_i - x_j - \Delta_{ij} \right]^2 \quad \Delta_{ij} = -\Delta_{ji}$$

$$\frac{d\phi}{dx_i} = \sum_{j \sim i} (x_i - x_j - \Delta_{ij}) + \frac{1}{2} \sum_{j \sim i} \frac{d}{dx_i} (x_j - x_i - \Delta_{ji})^2$$



$$Mx = b$$

$$M^{-1}$$

situation

$$= \sum_{j \sim i} (x_i - x_j - \Delta_{ij}) = 0 \quad (x_i - x_j + \Delta_{ji})$$

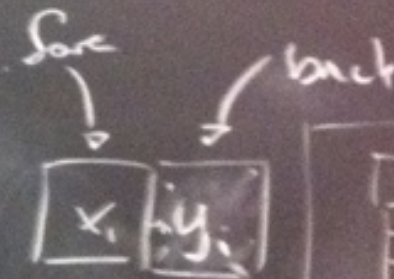
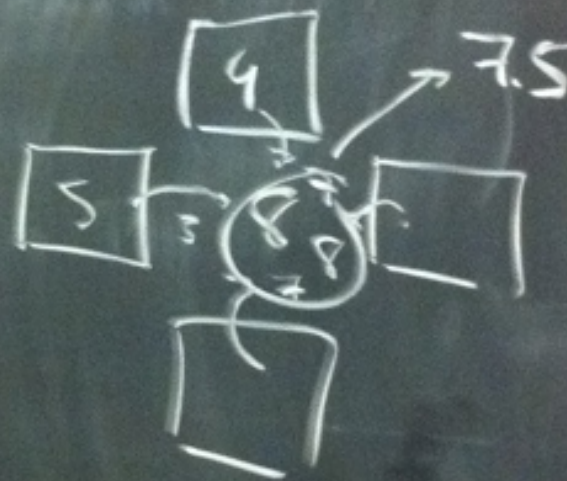
DERIVATIVE
MATRIX (solve)

$$4x_i - \sum_{j \sim i} x_j = \sum_{j \sim i} \Delta_{ij}$$

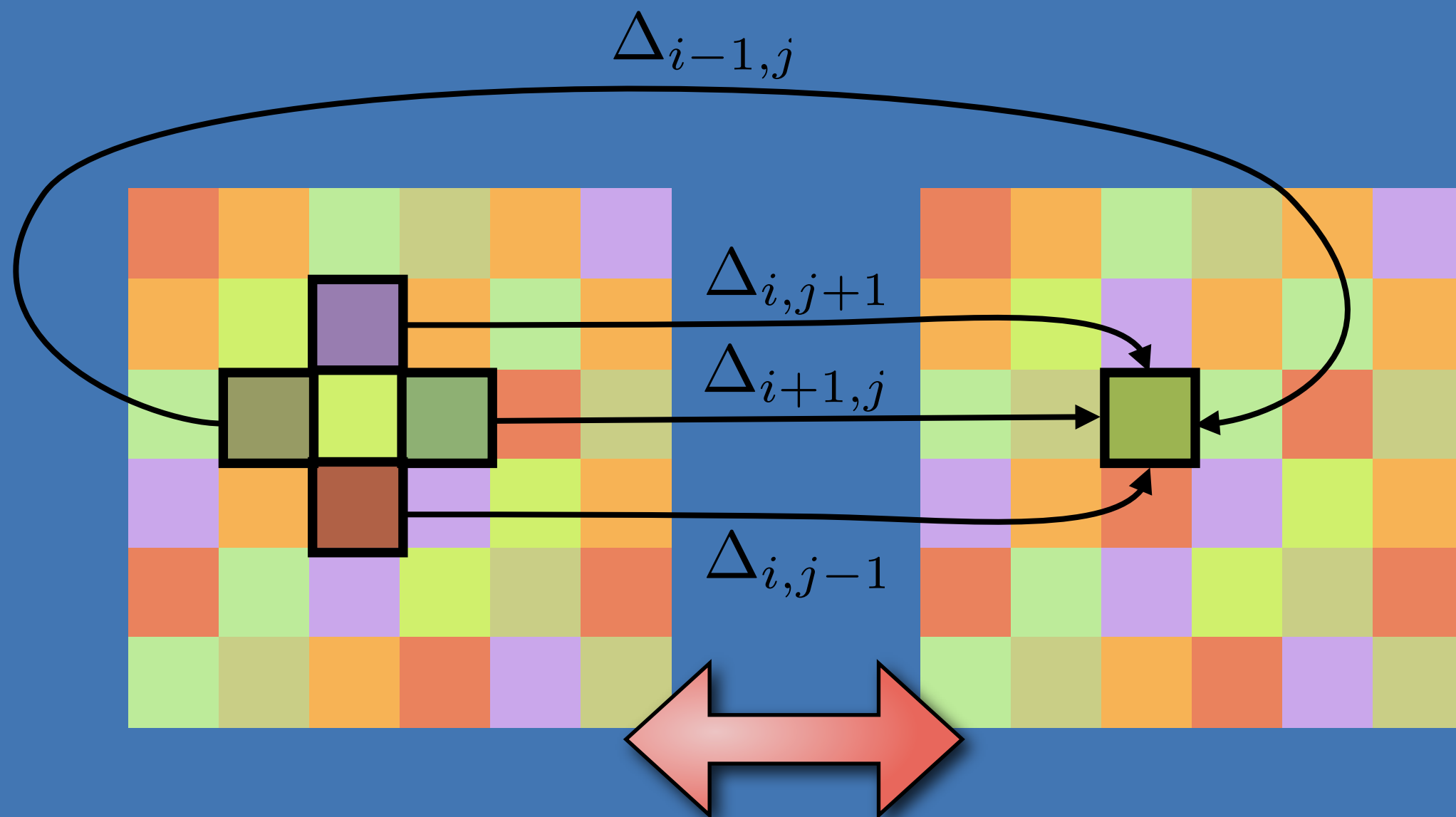
$$\begin{bmatrix} -1 & & \\ -1 & 4 & -1 \\ & -1 & \end{bmatrix}$$

JACOBI ITERATION

$$x_i = \frac{1}{4} \sum_{j \sim i} (x_j + \Delta_{ij})$$



Poisson Blending (Jacobi Iterations)



GPU Caching

Board...

Conjugate Gradient

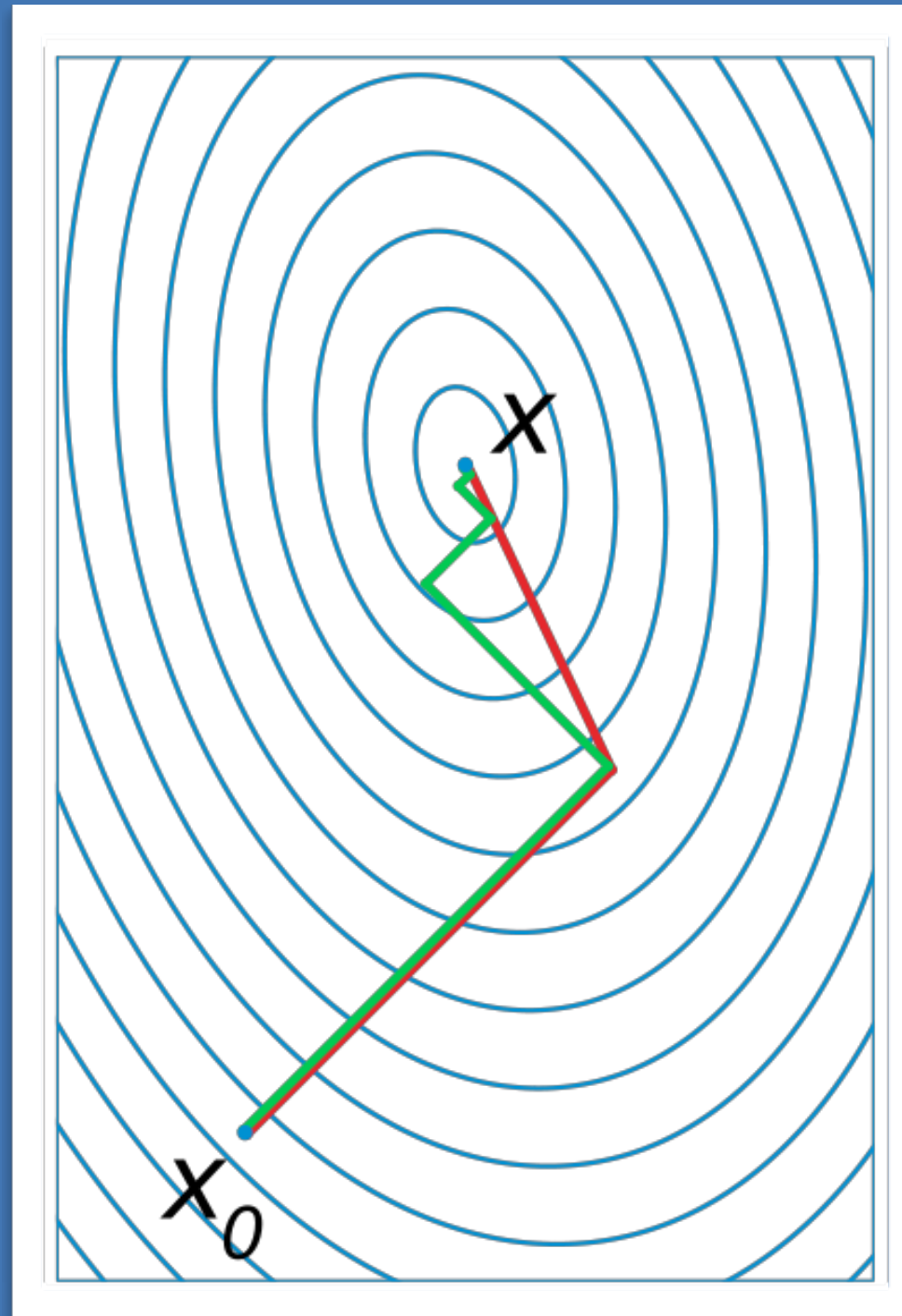
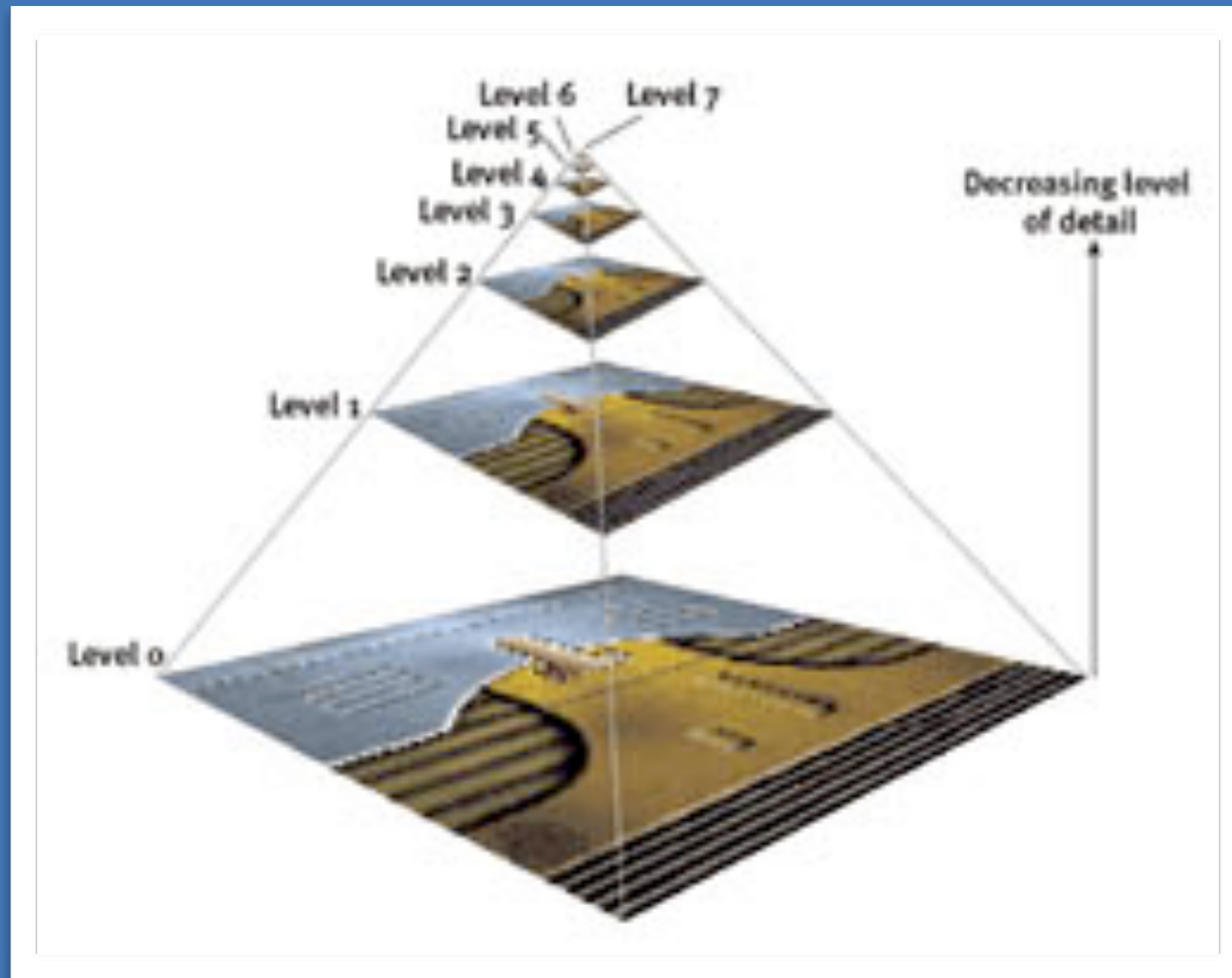


Image Pyramid



Other Membranes

SIGGRAPH 2009

Coordinates for Instant Image Cloning

[Zeev Farbman](#)

The Hebrew University

Gil Hoffer

Tel Aviv University

Yaron Lipman

Princeton University

[Daniel Cohen-Or](#)

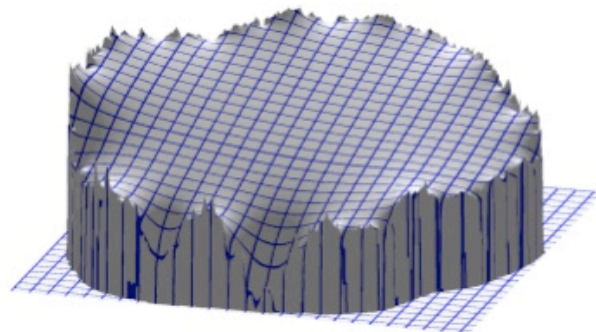
Tel Aviv University

[Dani Lischinski](#)

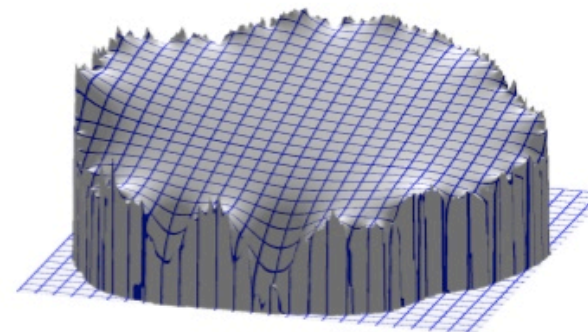
The Hebrew University



(a) Source patch



(b) Laplace membrane



(c) Mean-value membrane

$$\lambda_i(\mathbf{x}) = \frac{w_i}{\sum_{j=0}^{m-1} w_j}, \quad i = 0, \dots, m-1,$$

where

$$w_i = \frac{\tan(\alpha_{i-1}/2) + \tan(\alpha_i/2)}{\|\mathbf{p}_i - \mathbf{x}\|},$$