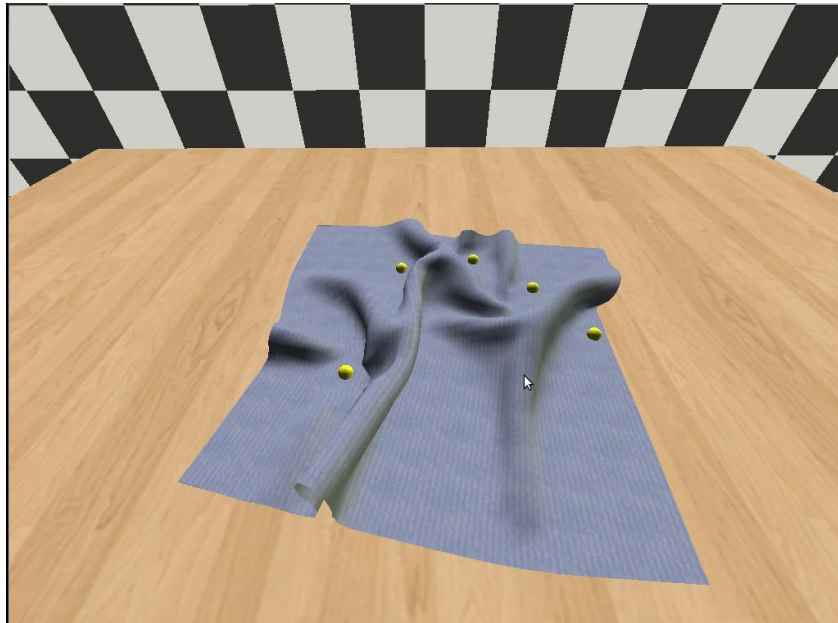


Cloth Simulation and Manipulation



Ken Toh

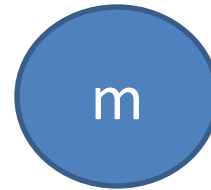
21 Feb 2011

Contents

- Physically-based Simulation: An Overview
- Cloth Representation
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- Cloth Manipulation with Multi-Touch

Physically-based Simulation

- Model the phenomenon as a collection of particles (ie. particle system)
- Particle has the following physical quantities:
- \mathbf{x} : position
- \mathbf{v} : velocity
- \mathbf{a} : acceleration
- m : mass
- \mathbf{f} : force



Newton's 2nd Law: $\mathbf{a} = (1/m) \mathbf{f}$

Euler Integration

*Simplest scheme but
might not be stable for
big time steps!*

- The goal is always to find the new position and velocity of the particle after each new time step dt .
- First, sum up all the forces acting on the particle. Then use N2L to find the acceleration:
 - $\mathbf{a} = (1/m) \mathbf{f}$
- Using the acceleration, we can in turn find the new velocity and position by using Euler's:
 - $\mathbf{v}_{t+1} = \mathbf{v}_t + \mathbf{a}_t dt$
 - $\mathbf{x}_{t+1} = \mathbf{x}_t + \mathbf{v}_{t+1} dt$

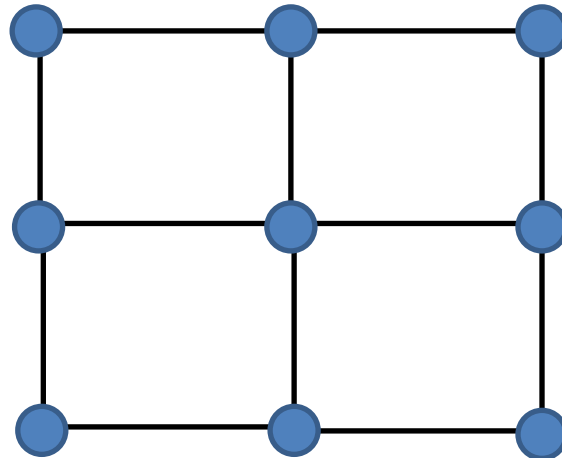
How about a whole particle system?

- General steps for simulating a particle system:
- For each particle:
 - Find and accumulate forces acting on particle
 - Compute acceleration \mathbf{a} using Newton's 2nd Law
 - Integrate to get \mathbf{x} and \mathbf{v} .
 - Update new \mathbf{x} and \mathbf{v} , and zero out forces

Repeat again during next time step...

Cloth

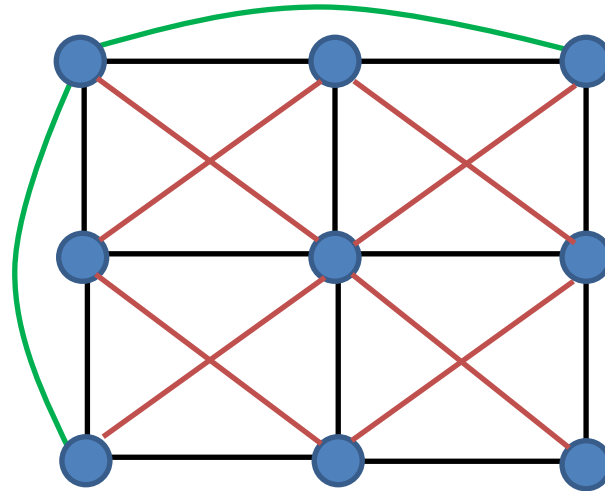
- Spring-based Cloth
- A structured lattice of particles interconnected by spring dampers



What's wrong with this simple representation?

Cloth Properties

- Want to capture resistive properties of cloth:
- Resistance To:
- Stretching (Black)
- Bending (Green)
- Shearing (Red)



Cloth Simulation

At each time step, loop through each particle:

- Add forces acting on particle
 - Gravity force (-9.81ms^{-2})
 - drag force, user-defined forces, etc
- Also compute the spring damper forces acting on each particle and add them
- Integrate to find new positions and velocities

Spring Damper Forces

- Each spring connects two particles.
- Important properties:

- Spring Constant k_s
- Damping Constant k_d
- Rest Length r



$$\mathbf{f}_1 = - \left[k_s (|\Delta \mathbf{x}| - r) + k_d \left(\frac{\Delta \mathbf{v} \cdot \Delta \mathbf{x}}{|\Delta \mathbf{x}|} \right) \right] \frac{\Delta \mathbf{x}}{|\Delta \mathbf{x}|}$$
$$\mathbf{f}_2 = -\mathbf{f}_1$$

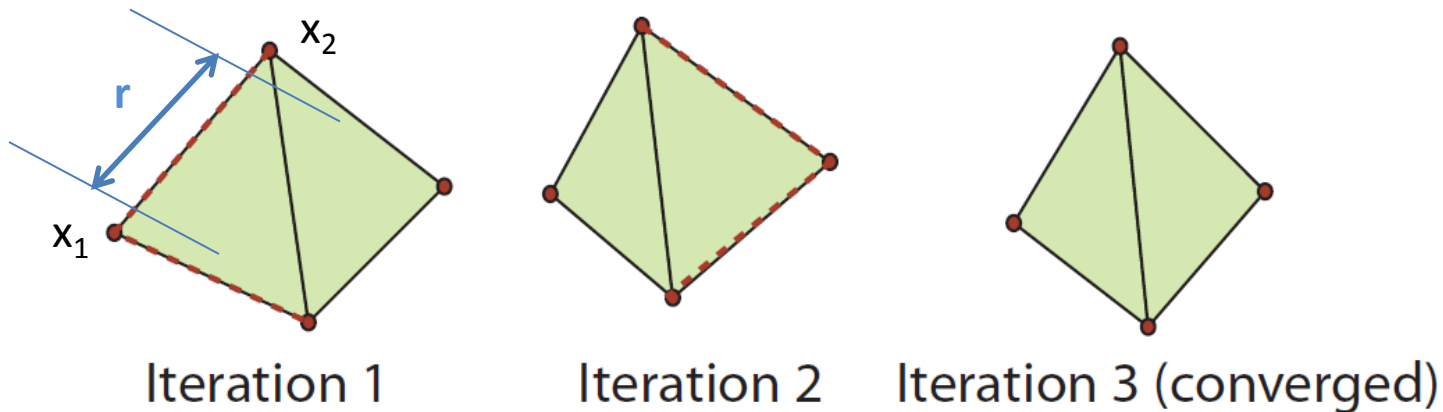
For each damper, compute the force it exerts on each particle in the pair.

Constraint-based (Inextensible) Cloth

- **Force** based spring dampers tend to lead to rather stretchy cloth. Stiff springs are problematic
- Use **position** constraints instead. After each time step, check for constraint violations and attempt to satisfy these constraints iteratively. (Provot [1995])
- Used this in my project!

Iterative Constraint Satisfaction

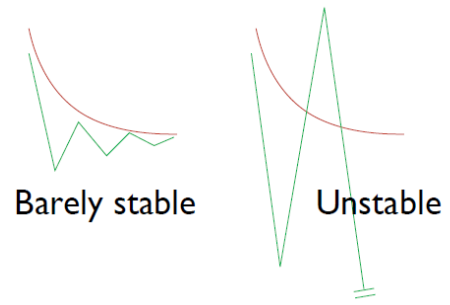
- Iteratively “fix” each constraint that is violated a few times after each time step.



$$\Delta \mathbf{x}_1 = \frac{1}{2} (|\mathbf{x}_2 - \mathbf{x}_1| - r) \frac{\mathbf{x}_2 - \mathbf{x}_1}{|\mathbf{x}_2 - \mathbf{x}_1|}$$

$$\Delta \mathbf{x}_2 = -\Delta \mathbf{x}_1$$

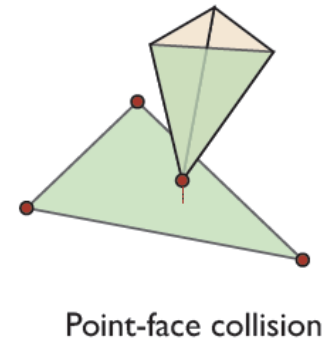
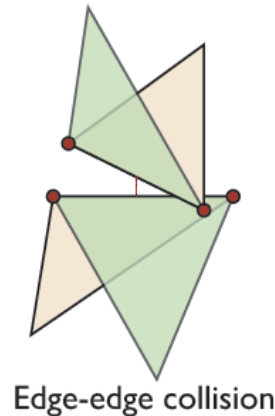
Remarks on stability



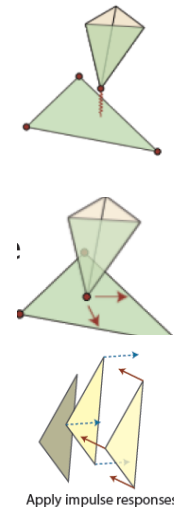
- Euler (Explicit) Integration can easily become unstable (overshooting!) unless we run it with very tiny time steps.
- Simulation can still blow up due to energy gains despite our attempts to introduce controlled damping
- Other methods of integration to improve stability: Verlet, Midpoint, Runge Kutta 2, Runge Kutta 4, etc.

Collision Overview

- **Detection**
- Typically, check for co-planarity of 4 points
- Use acceleration schemes



- **Response**
- Penalty forces – use springs (hard to tune)
- Constraint-based response (only pt-face)
- Impulse based response (mult. iterations)



Interactive Cloth Manipulation

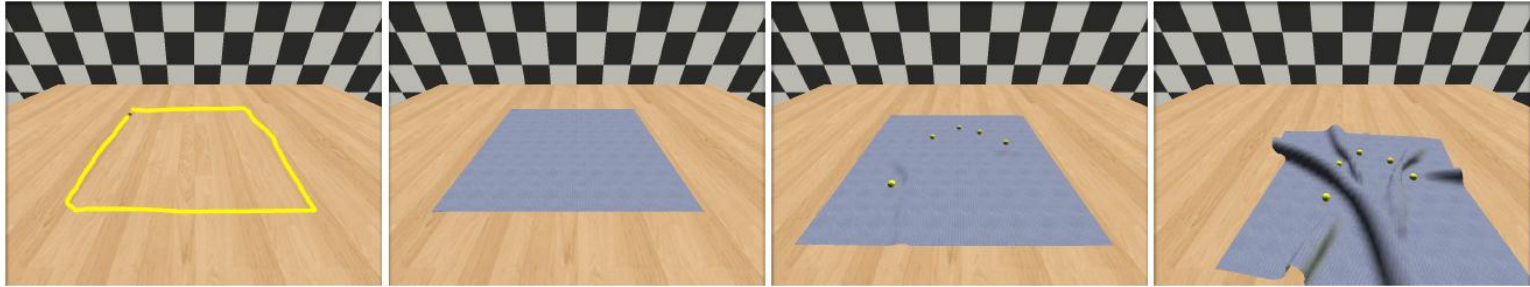


Figure 1: The user first creates a cloth by drawing its shape on the scene. The user then manipulates the cloth using multiple sticky fingers.

- **Verlet Integration and Position-based constraint satisfaction** (often used in games as well!)
- Supports pinching, folding, pinning, tearing, draping, lifting, crumpling, spreading, rotation, translation etc
- Note that these manipulations require multiple finger-control



Simulation Model

- Verlet Integration and Position-based Iterative Constraint Satisfaction (mentioned earlier)
- Verlet is velocity-less!
- Fast, much more stable than Euler and works directly with positions
- Keep an extra variable \mathbf{x}_{t-1} : old position
- Velocity approximated by $\mathbf{x}_t - \mathbf{x}_{t-1}$

- $$\mathbf{x}_{t+1} = 2\mathbf{x}_t - \mathbf{x}_{t-1} + \mathbf{a} dt^2$$

Cloth Manipulation With Sticky Fingers

- Direct manipulation of positions important
- It takes time for applied spring forces to act
- Solitary mouse cursor inadequate for manipulation
- Solution: Multiple “sticky” fingers
- User Interface: Multi-Touch

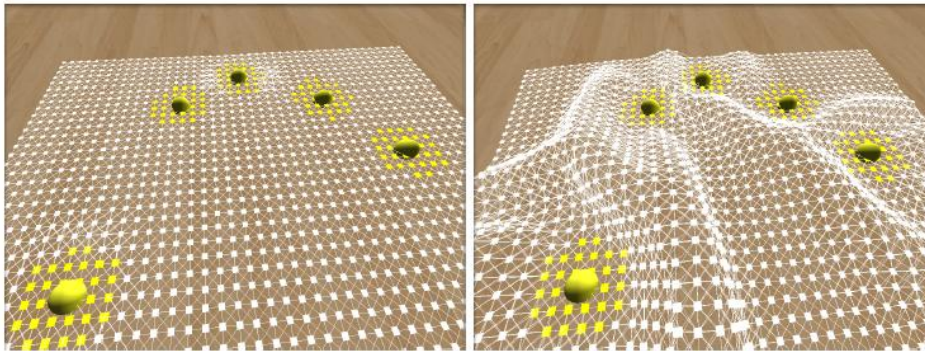


Figure 5: Sticky Fingers: Underlying cloth particles within a radius from the center of an active finger are stuck to that finger and move with it.

Tearing

- Easy way: break springs/remove constraints that are overstretched. But may lose “area”
- More accurate way: node splitting.

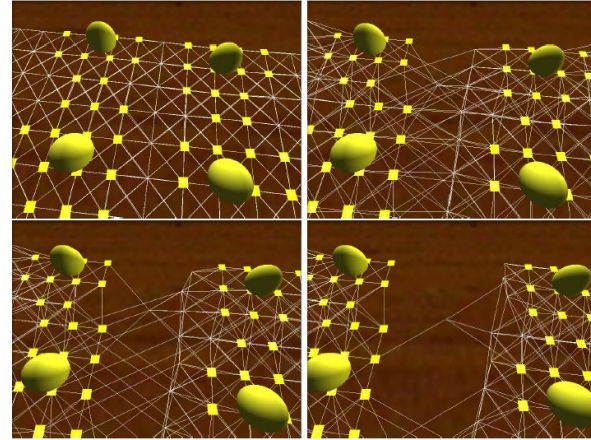
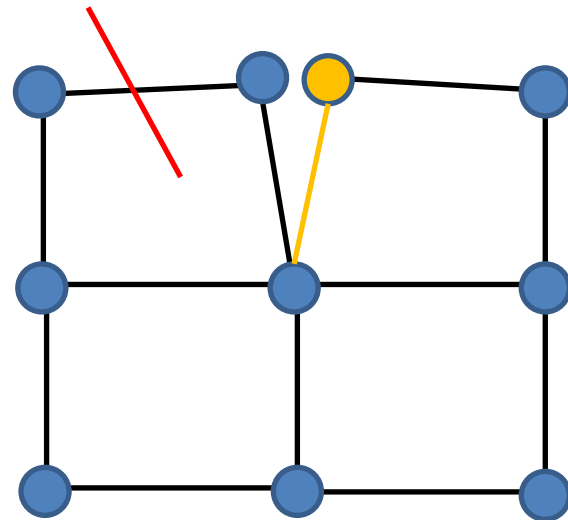
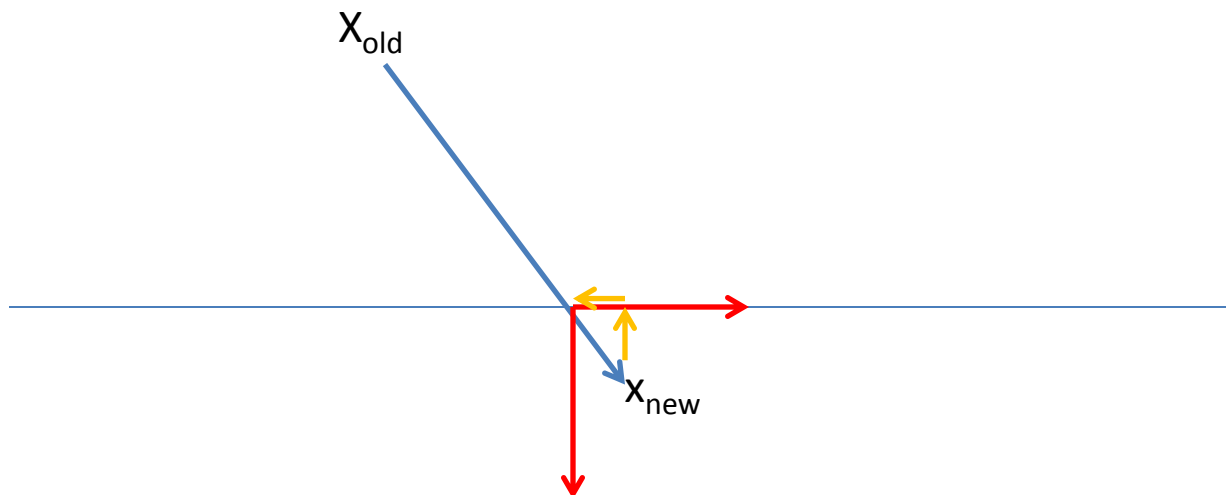


Figure 12: Simple mesh tearing is achieved by removing constraints that are “over-stretched” beyond an allowed distance threshold



Handling Collision

- Self collisions ignored
- Simple projection of particle to geometry surface upon collision
- Scale tangential component of response by a suitable coefficient of friction.
- Attenuate projected x_{new} with the scaled tangential component



Demos