Image Processing



Overview



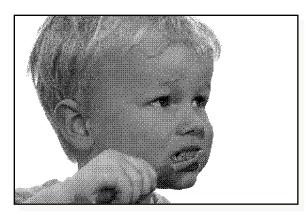
Images



Neighborhood Filters



Pixel Filters



Dithering

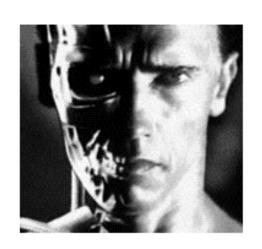
Image as a Function

- We can think of an image as a function, f,
- f: $R^2 \rightarrow R$
 - -f(x, y) gives the **intensity** at position (x, y)
 - Realistically, we expect the image only to be defined over a rectangle, with a finite range:
 - $f: [a,b] \times [c,d] \rightarrow [0,1]$
- A color image is just three functions pasted together. We can write this as a "vectorvalued" function: [r(x, y)]

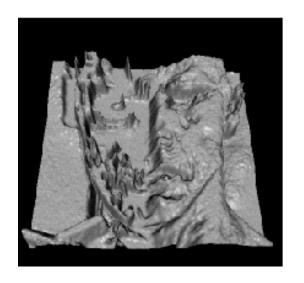
valued" function:

$$f(x,y) = \begin{bmatrix} r(x,y) \\ g(x,y) \\ b(x,y) \end{bmatrix}$$

Image as a Function







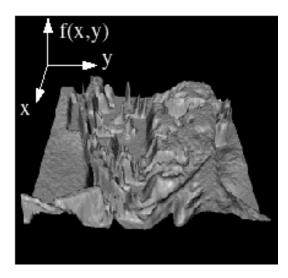


Image Processing

- Define a new image g in terms of an existing image f
 - We can transform either the domain or the range of f
- Range transformation:

$$g(x,y) = t(f(x,y))$$

What kinds of operations can this perform?

Image Processing

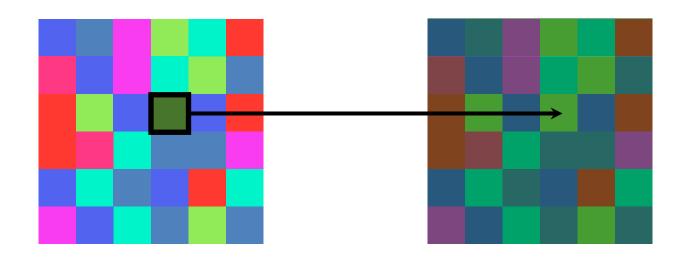
 Some operations preserve the range but change the domain of f:

$$g(x,y) = f(t_x(x,y), t_y(x,y))$$

What kinds of operations can this perform?

 Still other operations operate on both the domain and the range of f.

Point Operations



Point Processing

Original



Darken



Lower Contrast



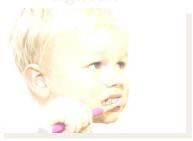
Nonlinear Lower Contrast



Invert



Lighten



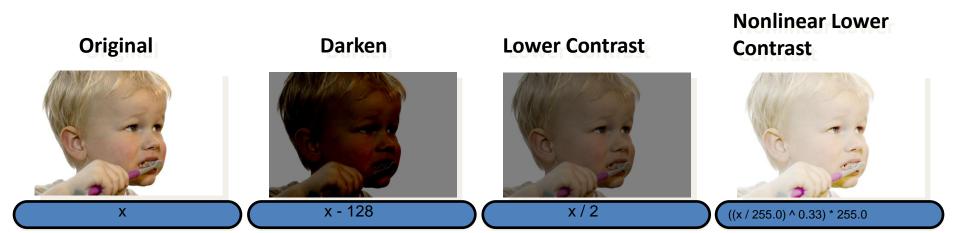
Raise Contrast

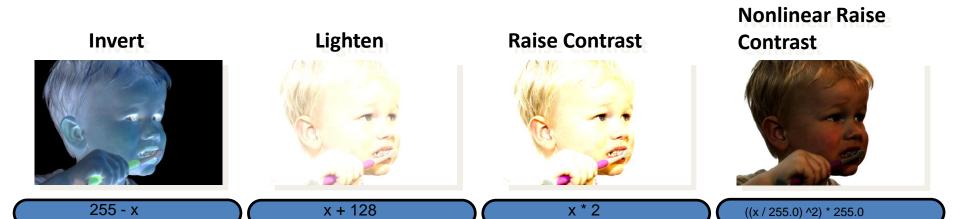


Nonlinear Raise Contrast



Point Processing





Gamma correction

Monitors have a intensity to voltage response curve which is roughly a 2.5 power function Send $v \rightarrow$ actually display a pixel which has intensity equal to $v^{2.5}$



Graph of Input



Graph of Output $L = V ^2 2.5$



Tom Ridge left the Pennsylvania governorship last October, when U.S. President George W. Bush appointed him to head the newly created Office of Homeland Security.

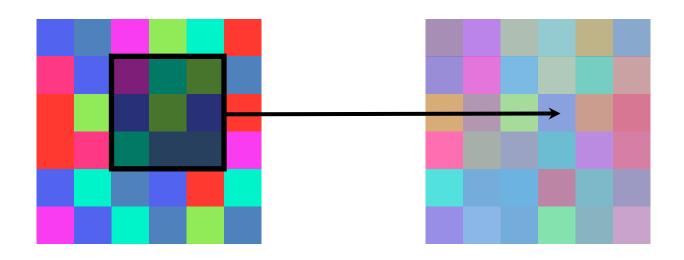
$$\wp = 1.0; f(v) = v$$



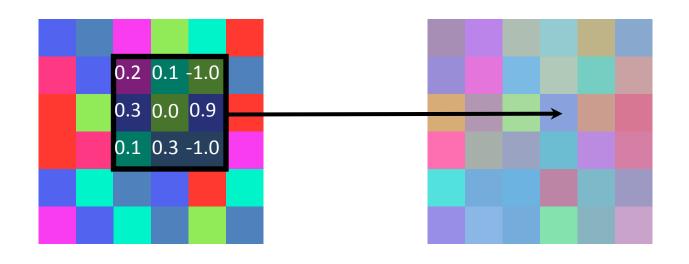
Tom Ridge left the Pennsylvania governorship last October, when U.S. President George W. Bush appointed him to head the newly created Office of Homeland Security.

$$\wp$$
= 2.5; $f(v) = v^{1/2.5} = v^{0.4}$

Neighborhood Operations



Convolution



$$F = \begin{bmatrix} 0.2 & 0.1 & -1.0 \\ 0.3 & 0.0 & 0.9 \\ 0.1 & 0.3 & -1.0 \end{bmatrix} \qquad I' = F * I$$

Properties of Convolution

Commutative

$$a*b=b*a$$

Associative

$$(a*b)*c = a*(b*c)$$

Cascade system

$$f \longrightarrow h_1 \longrightarrow h_2 \longrightarrow g$$

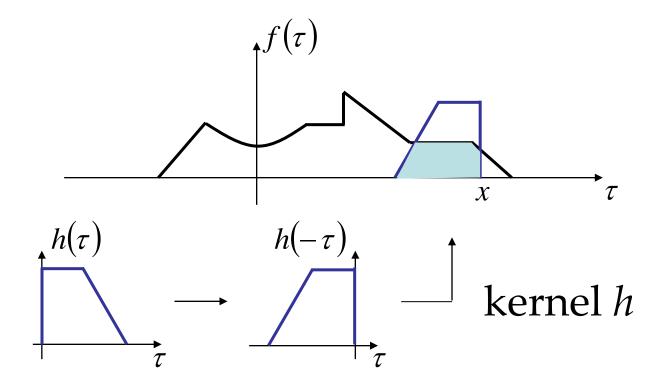
$$= f \longrightarrow h_1 * h_2 \longrightarrow g$$

$$= f \longrightarrow h_2 * h_1 \longrightarrow g$$

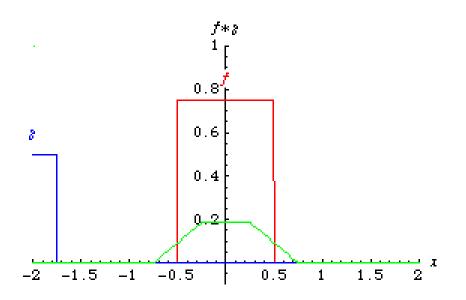
Convolution

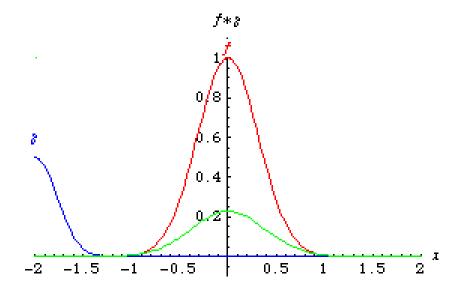
Convolution is linear and shift invariant

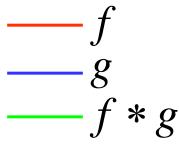
$$g(x) = \int_{-\infty}^{\infty} f(\tau)h(x-\tau)d\tau \qquad g = f * h$$



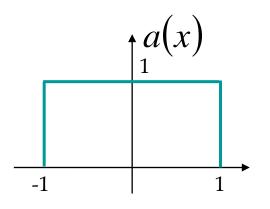
Convolution - Example

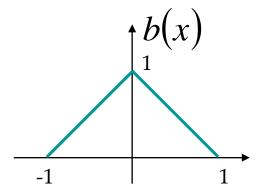




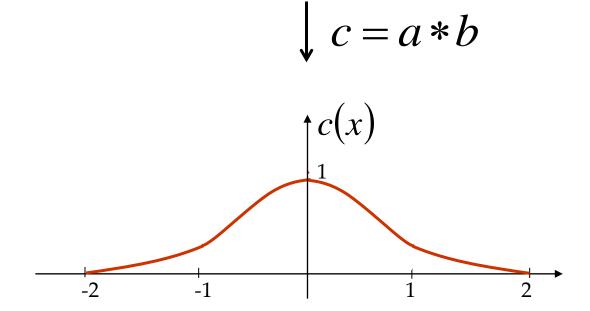


Convolution - Example

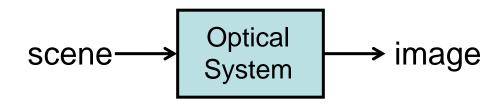




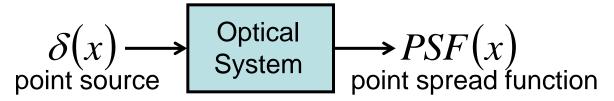
$$\int c = a * b$$



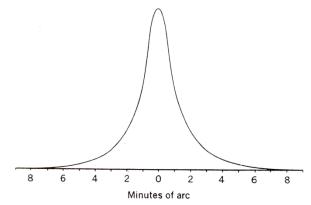
Point Spread Function



- Ideally, the optical system should be a Dirac delta function.
- However, optical systems are never ideal.



Point spread function of Human Eyes



Point Spread Function



normal vision



myopia



hyperopia



astigmatism

Images by Richmond Eye Ass

Original Image



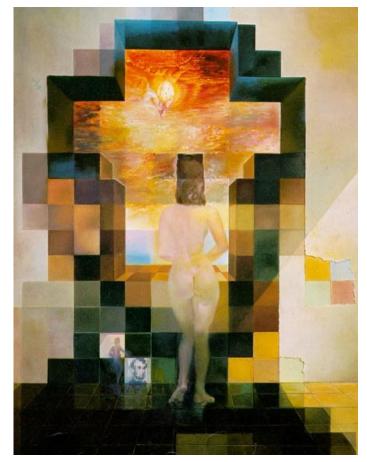
Blurred Image



Gaussian Smoothing



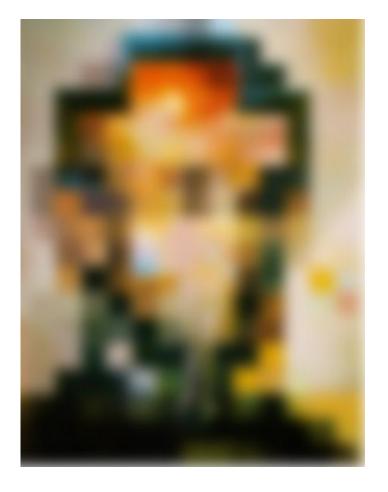
by Charles Allen Gillbert



by Harmon & Julesz

Gaussian Smoothing



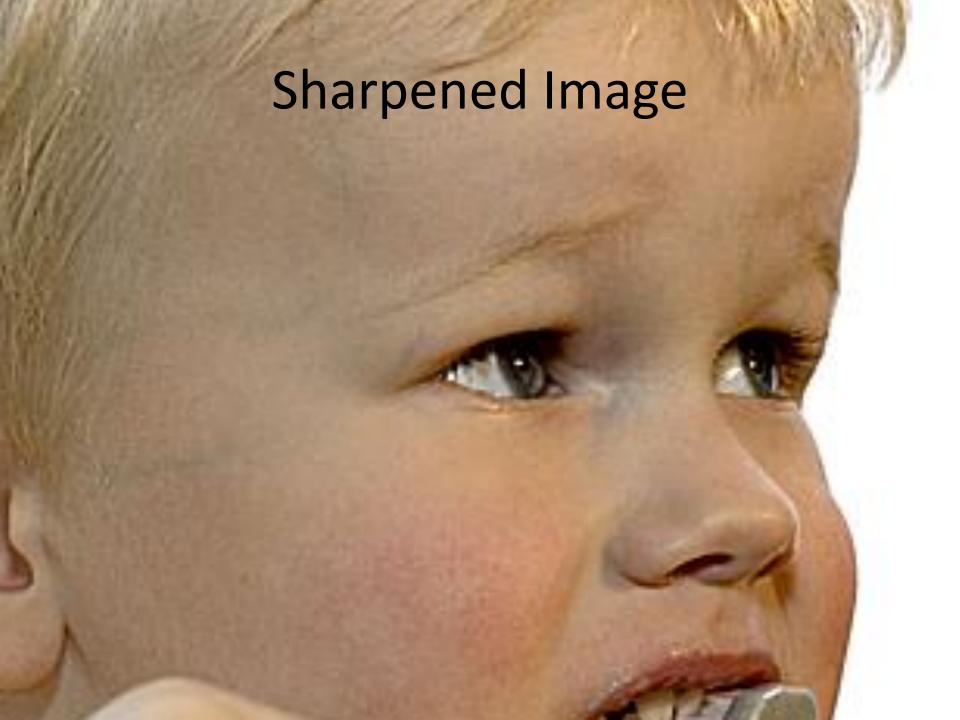


Original Image



Sharpened Image







Noise

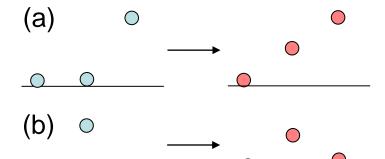


Blurred Noise

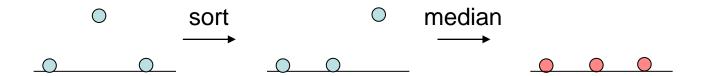


Median Filter

- Smoothing is averaging
 - (a) Blurs edges
 - (b) Sensitive to outliers



- Median filtering
 - Sort N^2-1 values around the pixel
 - Select middle value (median)



Non-linear (Cannot be implemented with convolution)

Median Filter



Can this be described as a convolution?

Original Image



Example: Noise Reduction

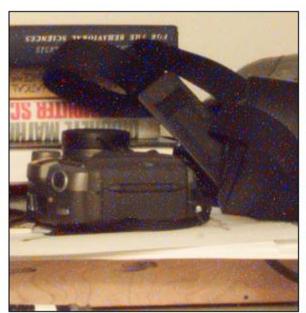
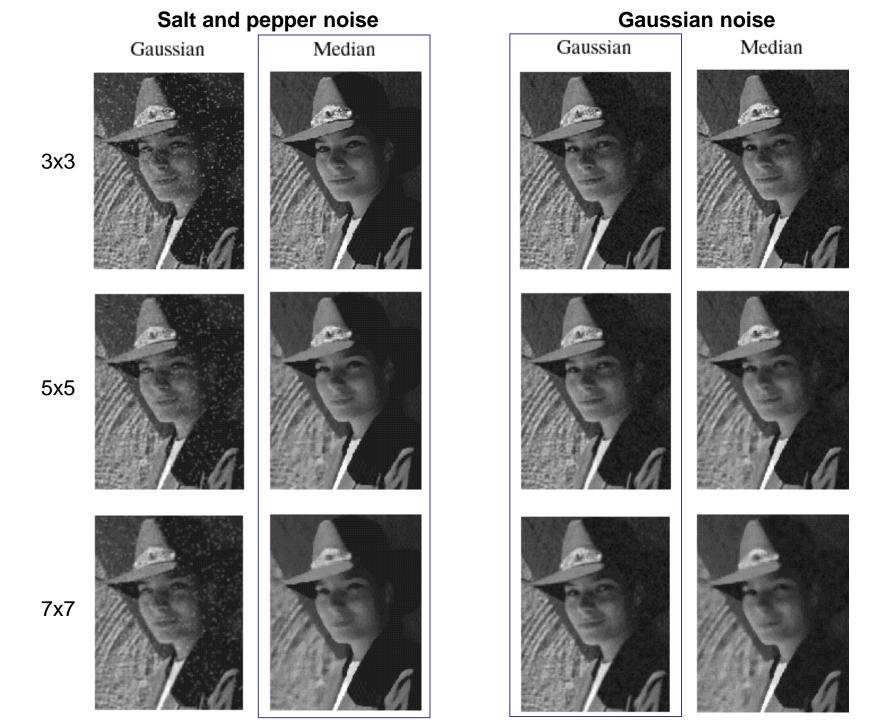


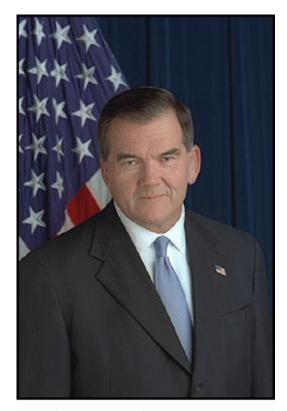
Image with noise



Median filter (5x5)



Example: Noise Reduction



Tom Ridge left the Pennsylvania governorship last October, when U.S. President George W. Bush appointed him to head the newly created Office of Homeland Security.

Original image



Tom Ridge left the Pennsylvania governorship last October, when U.S. President George W. Bush appointed him to head the newly created Office of Homeland Security.

Image with noise



There thinggs self-drug transmissionaping generatives again to realize where in the transmission in the transmission of the constitution of the co

Median filter (5x5)

Original Image



X-Edge Detection



Y-Edge Detection



General Edge Detection



Can this be described as a convolution?

Image Processing

 Some operations preserve the range but change the domain of f:

$$g(x,y) = f(t_x(x,y), t_y(x,y))$$

What kinds of operations can this perform?

 Still other operations operate on both the domain and the range of f.

Image Scaling

This image is too big to fit on the screen. How can we reduce it?

How to generate a halfsized version?

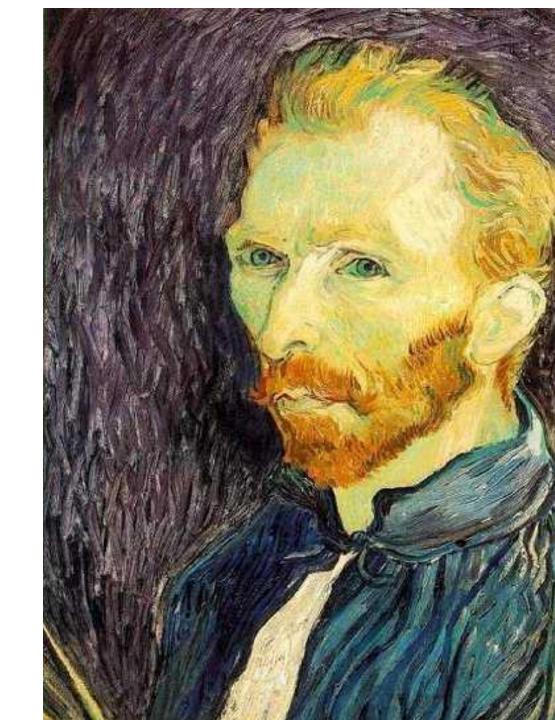
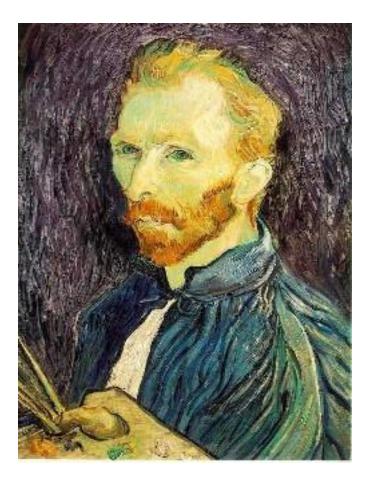


Image Sub-Sampling





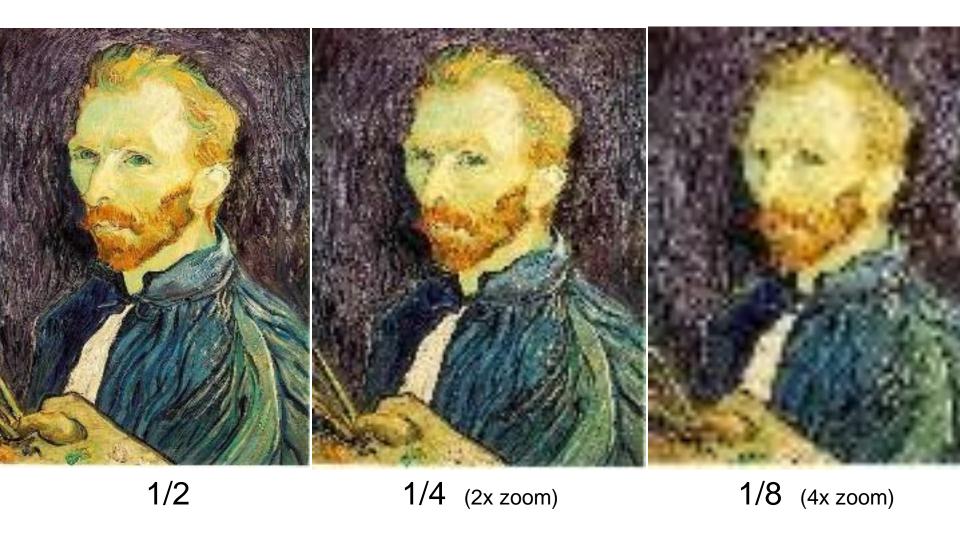


1/4

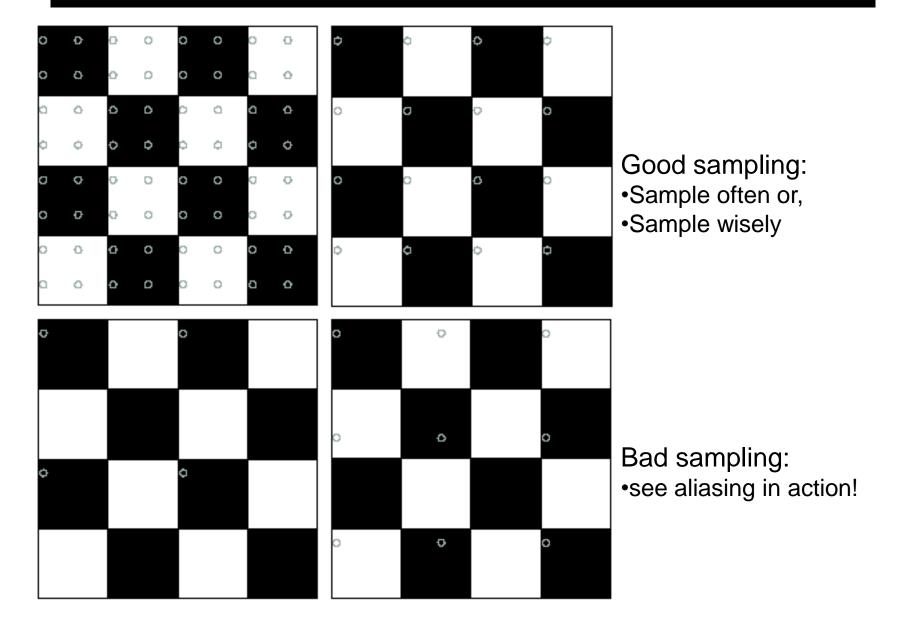
Throw away every other row and column to create a 1/2 size image - called *image sub-sampling*

1/8

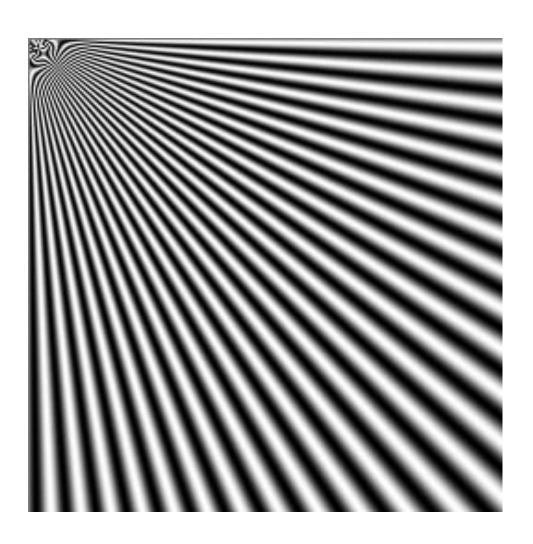
Image Sub-Sampling



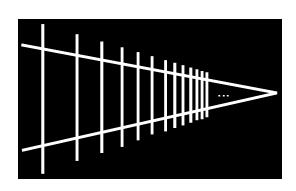
Good and Bad Sampling



Aliasing

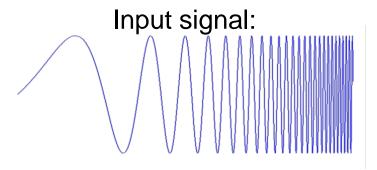


Alias: n., an assumed name

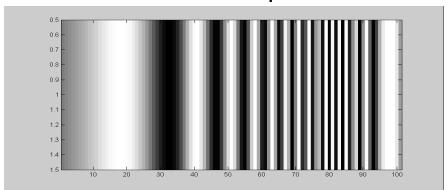


Picket fence receding into the distance will produce aliasing...

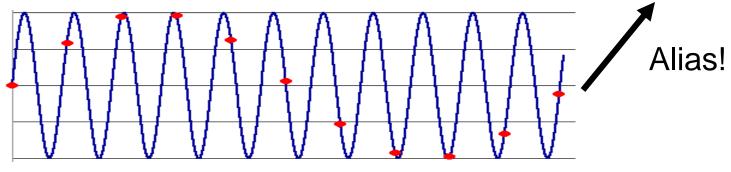
WHY?



Matlab output:



x = 0:.05:5; imagesc(sin((2.^x).*x))

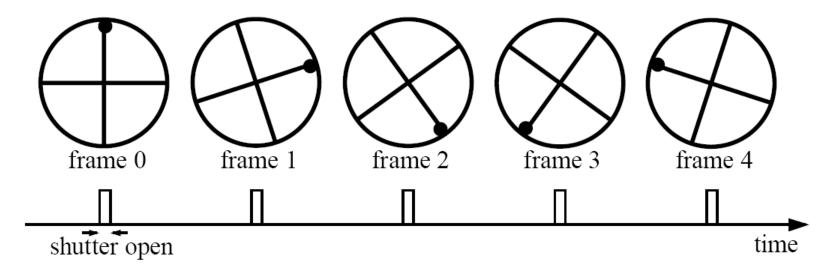


Not enough samples

Really bad in video

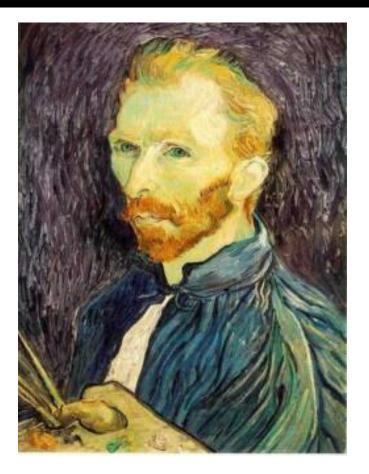
Imagine a spoked wheel moving to the right (rotating clockwise). Mark wheel with dot so we can see what's happening.

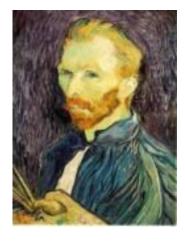
If camera shutter is only open for a fraction of a frame time (frame time = 1/30 sec. for video, 1/24 sec. for film):



Without dot, wheel appears to be rotating slowly backwards! (counterclockwise)

Sub-Sampling with Gaussian Pre-Filtering





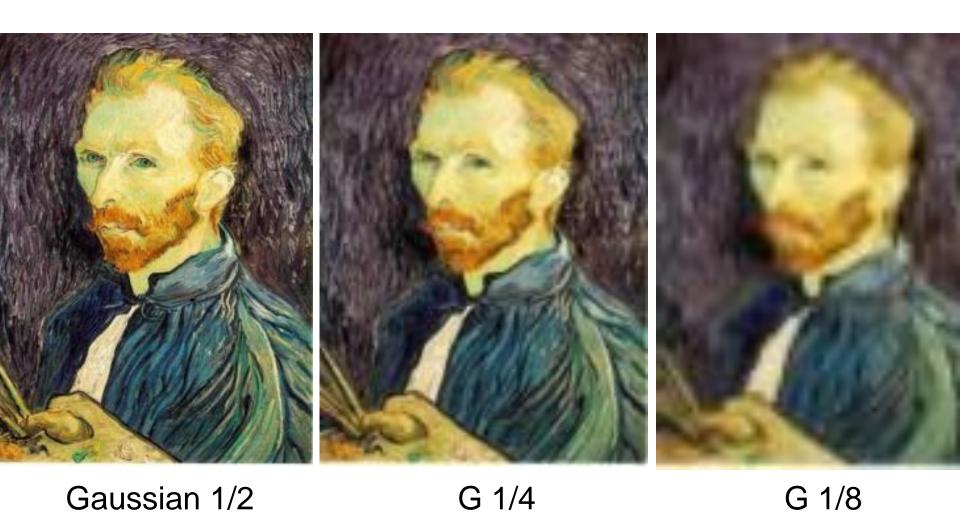


G 1/4

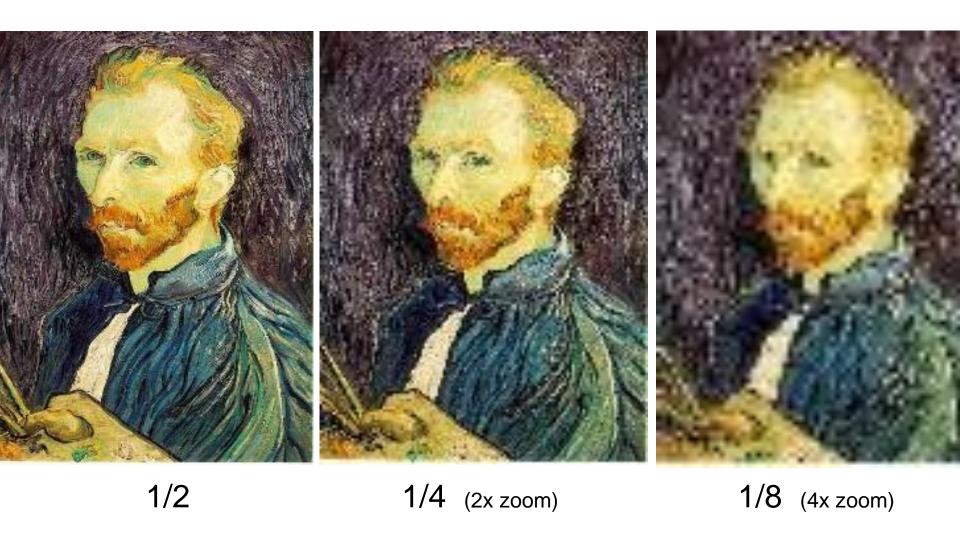
Gaussian 1/2

- Solution: filter the image, then subsample
 - Filter size should double for each ½ size reduction. Why?

Sub-Sampling with Gaussian Pre-Filtering



Compare with...

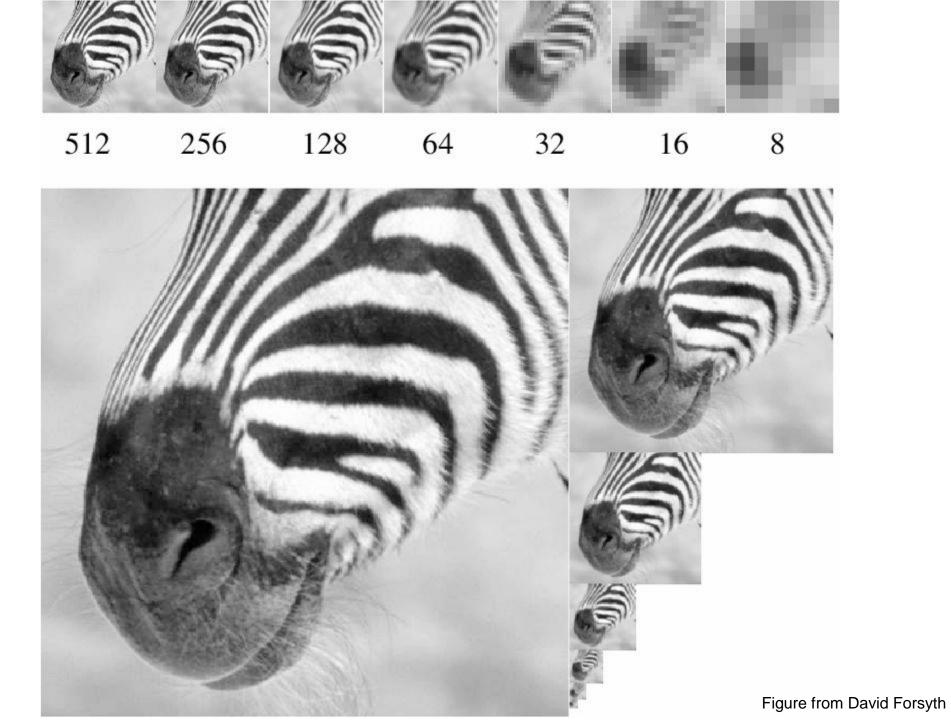




Canon D60 (w/ anti-alias filter)

Sigma SD9 (w/o anti-alias filter)

From Rick Matthews website, images by Dave Etchells



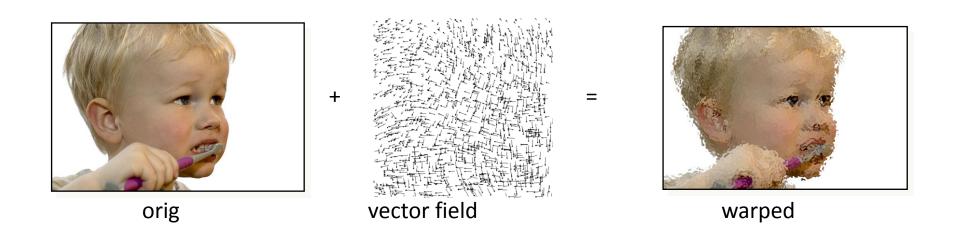
Original Image



Warped Image



Warped Image



how?

Advection (just like a fluid)

