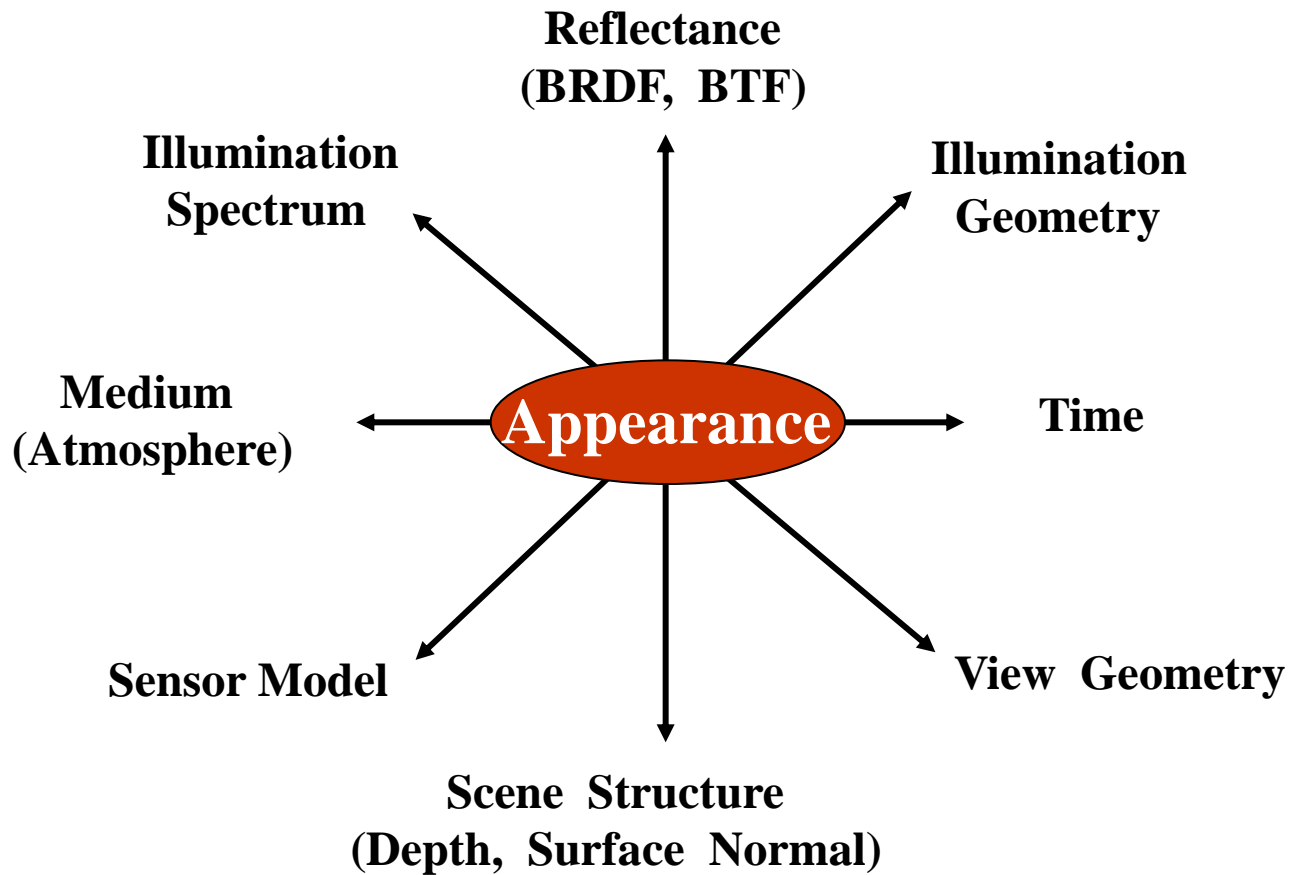


# Lighting and Color

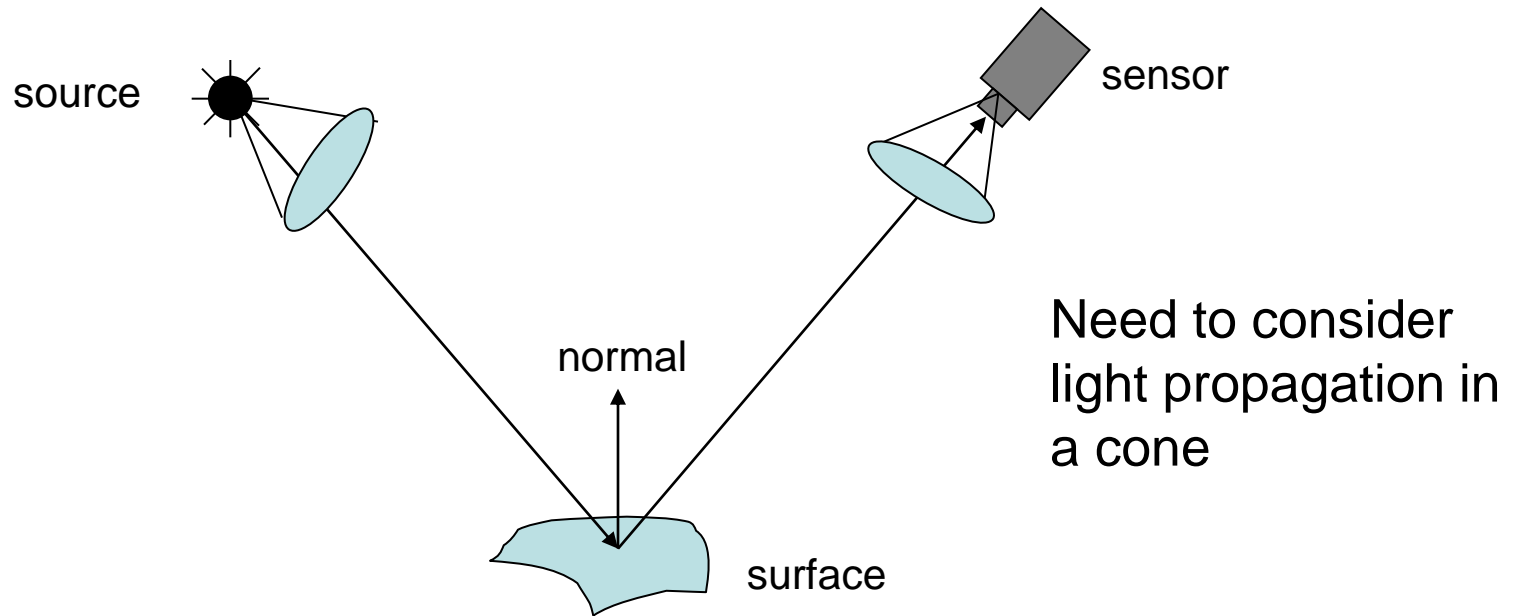
Thanks to Langer-Zucker, Henrik Wann Jensen, Ravi Ramamoorthi, Hanrahan, Preetham

# Appearance of An Outdoor Scene



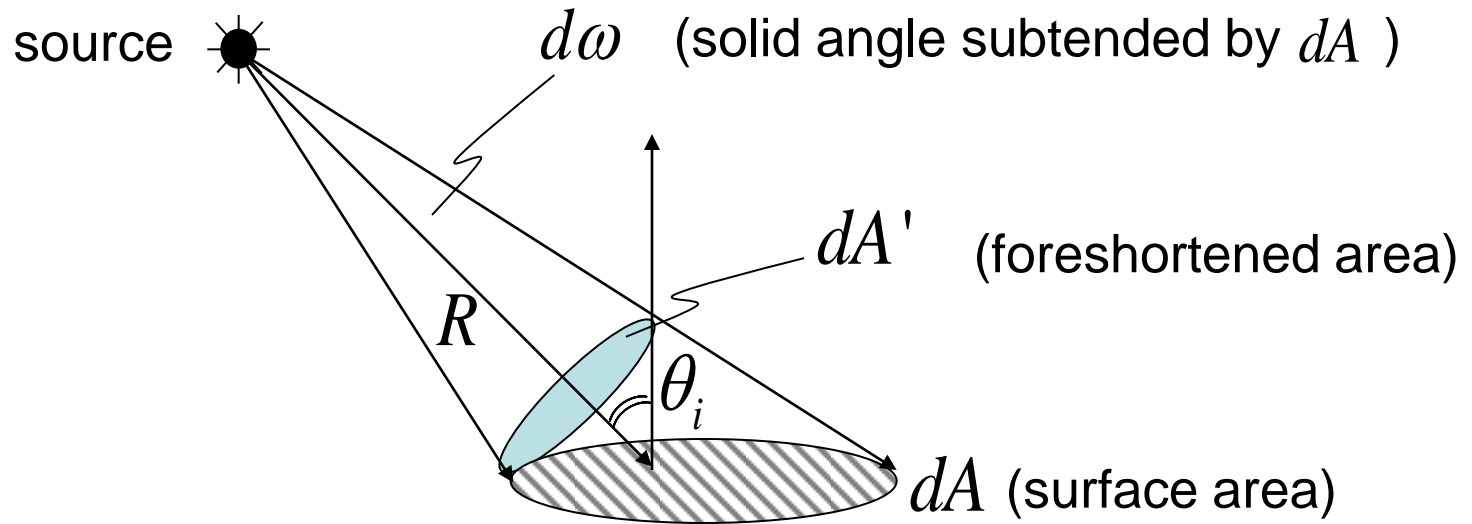
# How to quantify light?

---



# Solid Angle

---

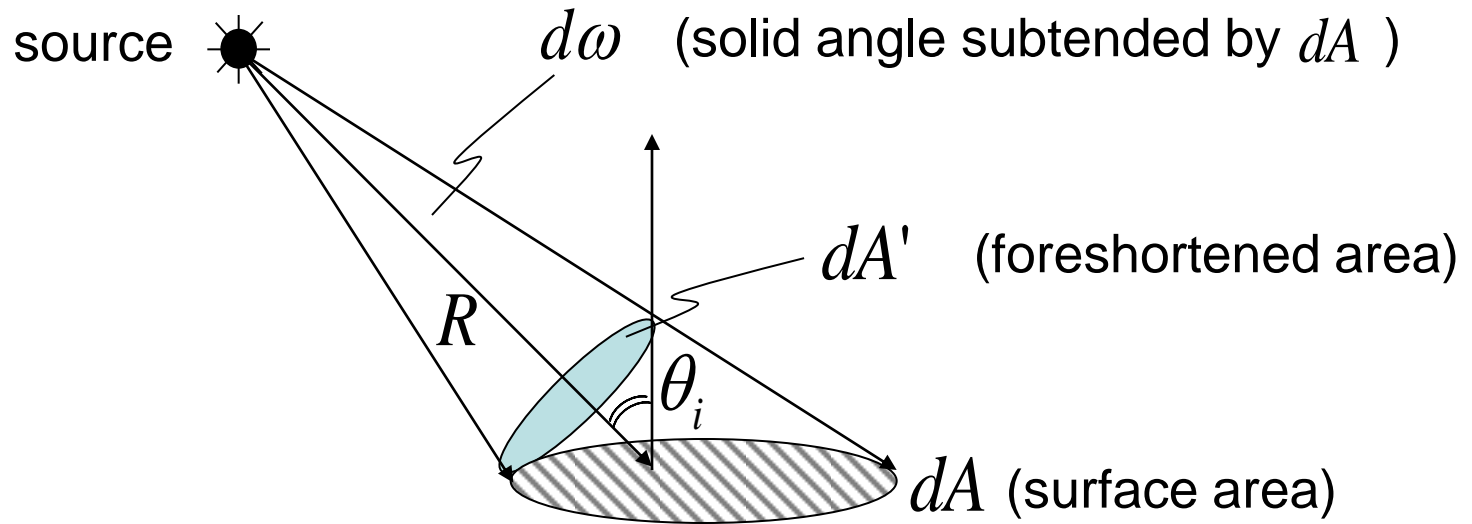


Solid Angle : 
$$d\omega = \frac{dA'}{R^2} = \frac{dA \cos \theta_i}{R^2} \quad (\text{steradian})$$

What is the solid angle subtended by a hemisphere?

# Radiant Intensity of Source

---

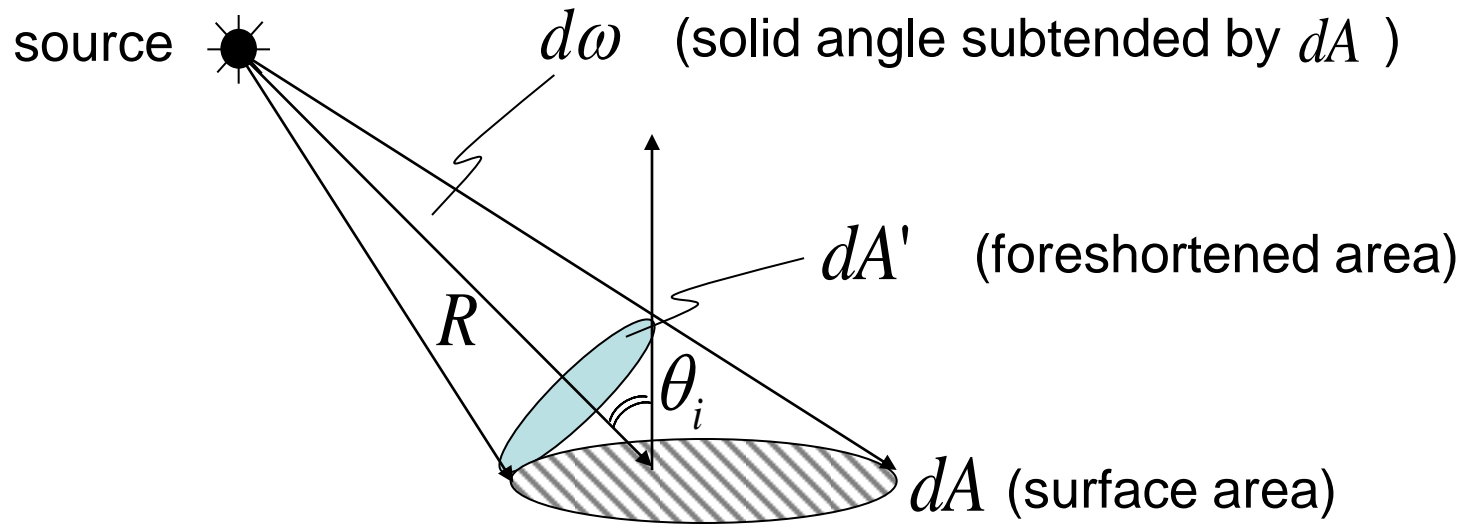


Radiant Intensity of Source : 
$$I = \frac{d\Phi}{d\omega} \quad (\text{watts / steradian})$$

Light Flux (power) emitted per unit solid angle

# Surface Irradiance

---



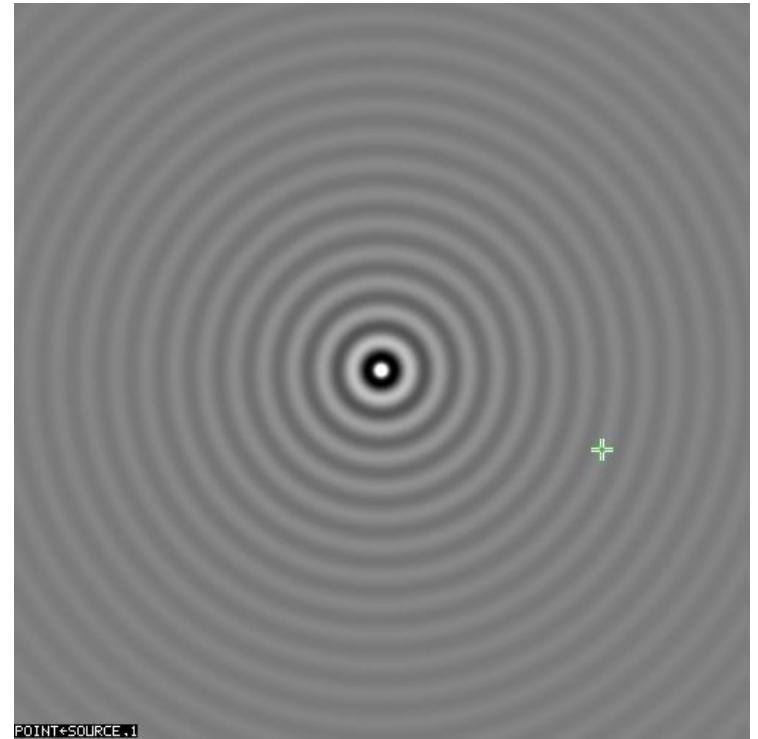
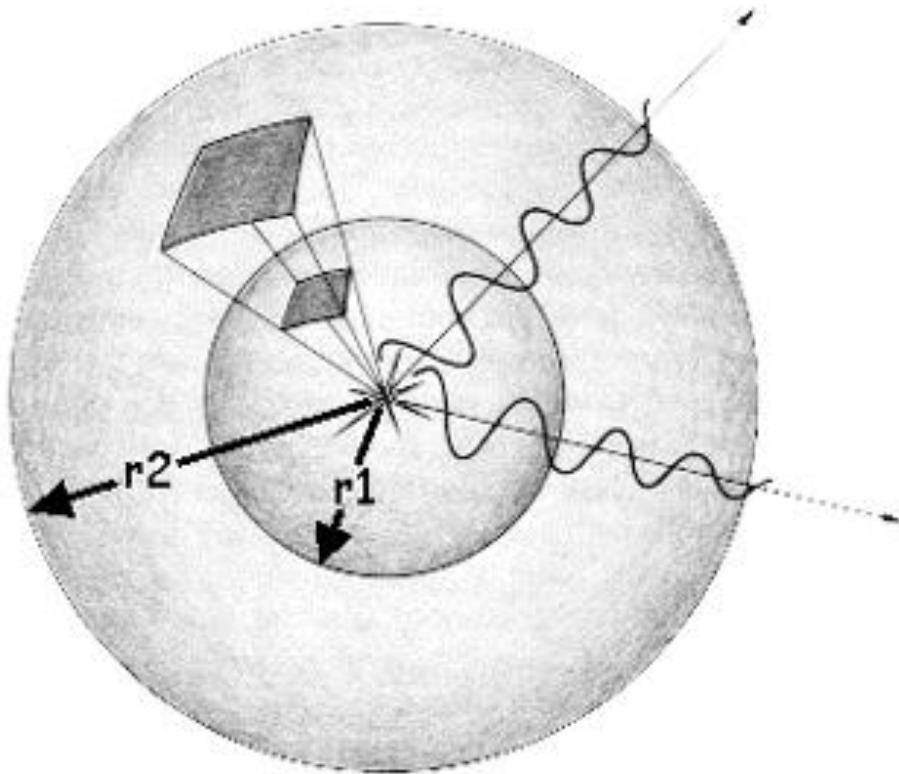
Surface Irradiance :

$$E = \frac{d\Phi}{dA} \quad (\text{watts} / \text{m}^2)$$

Light Flux (power) incident per unit surface area.

Does not depend on where the light is coming from!

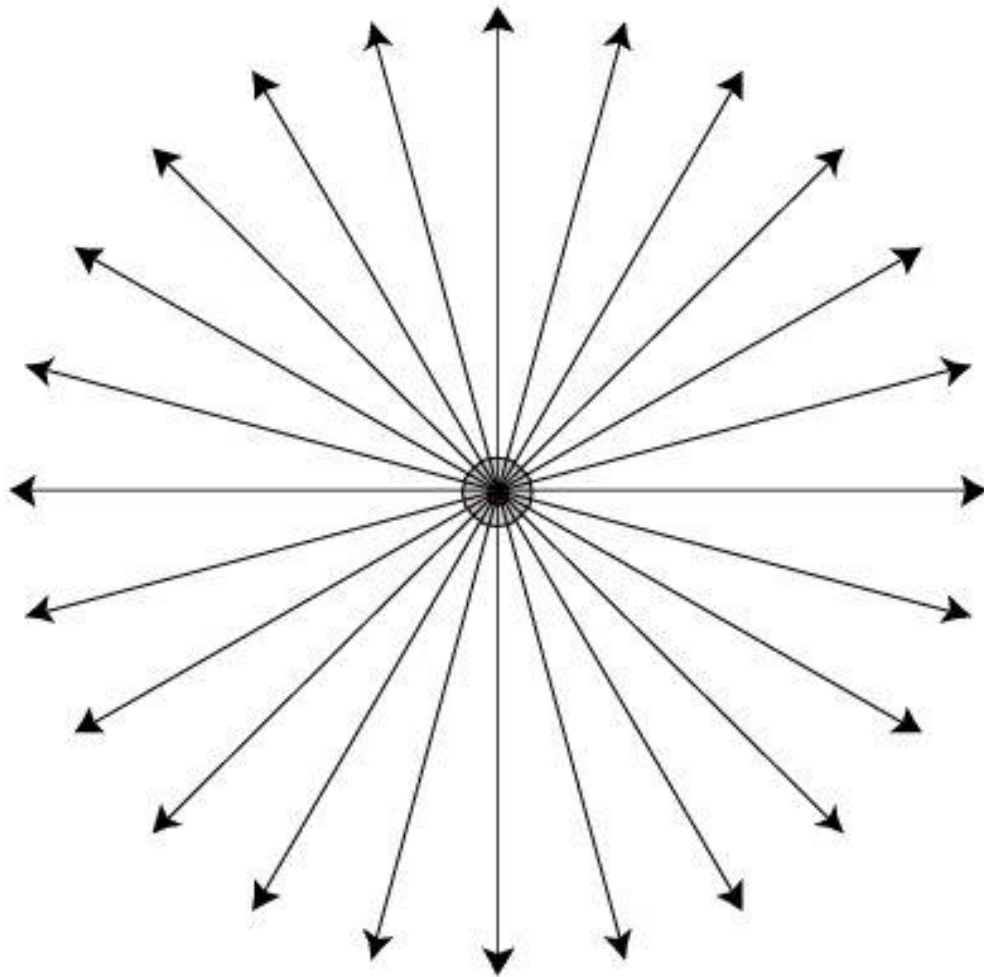
# Isotropic Point Light Source



We see an inverse distance squared fall off in intensity.  
Here light does not weaken, but only spreads in a sphere.

# Isotropic Point Source

---

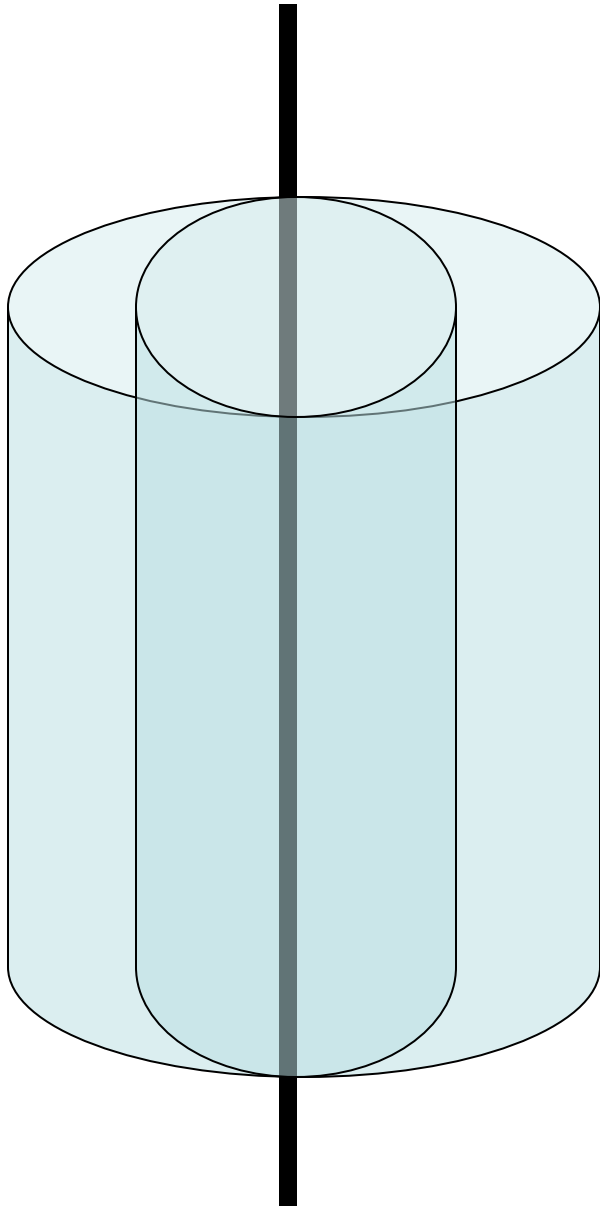


$$\begin{aligned}\Phi &= \int_{s^2} I d\omega \\ &= 4\pi I\end{aligned}$$

$$I = \frac{\Phi}{4\pi}$$



# Infinite Line Source



Line source shows cylindrical symmetry.

The intensity fall-off is inversely proportional to distance from the line source. Why?

$$d\Phi = I d\omega = E dA$$

# Infinite Planar Area Source

- Assume every point on the plane is an isotropic point light source.
- We saw inverse squared fall off, inverse fall off...so, this must be...
- Intensity CONSTANT with respect to distance! WHY?

As distance increases,

$$d\Phi = I d\omega = E dA$$

Intensity from one point source decreases

But we add intensities from all point sources on the plane.

# Distant and Collimated Lighting

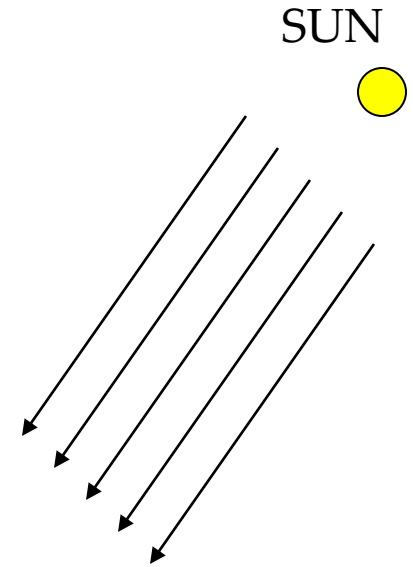
## Distant Lighting:

Essentially source at infinity

All surface points receive light from the same direction

Intensity fall must not be ignored!

Most vision and graphics algorithms assume this.

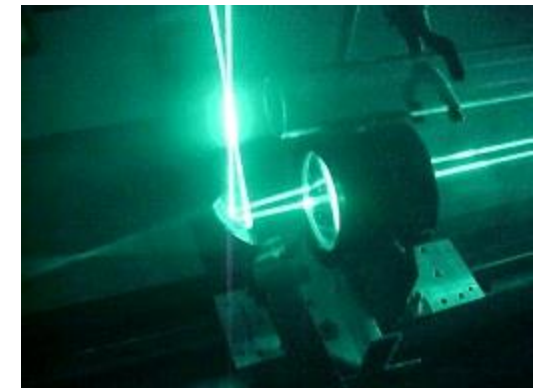


## Collimated:

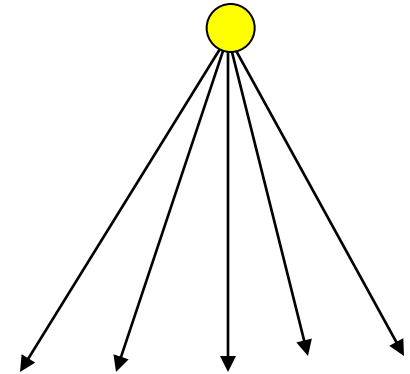
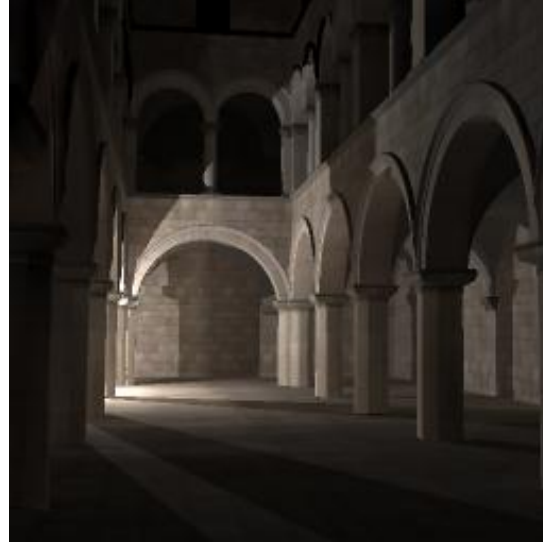
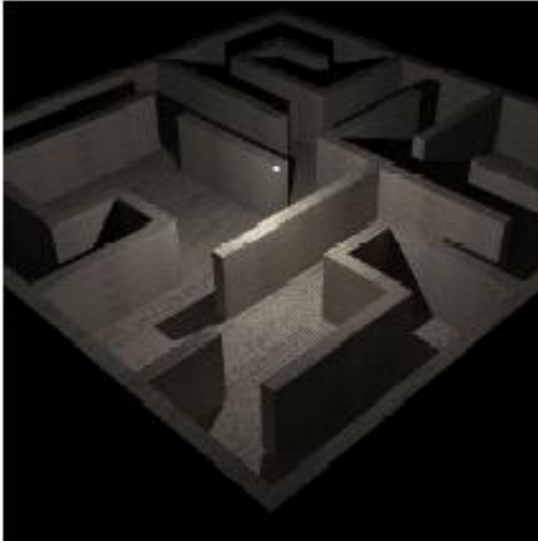
Parallel rays of light on the surface

Lasers (no fall off) - need not be at infinity

Lighting at infinity - (inverse squared fall off)



# Divergent and Near-field Lighting



- Every scene point can receive light from a different direction.
- Much harder to model.
- Examples: near by point sources, spot lights
- Assume distant lighting when size of scene is 10% of the distance to the source.

# Fluorescent versus Incandescent Lighting

## Fluorescent:

Less heat generated.

More efficient lighting for the same brightness.

Flickers continuously.

Shows sparse, spikes in spectrum.

## Incandescent:

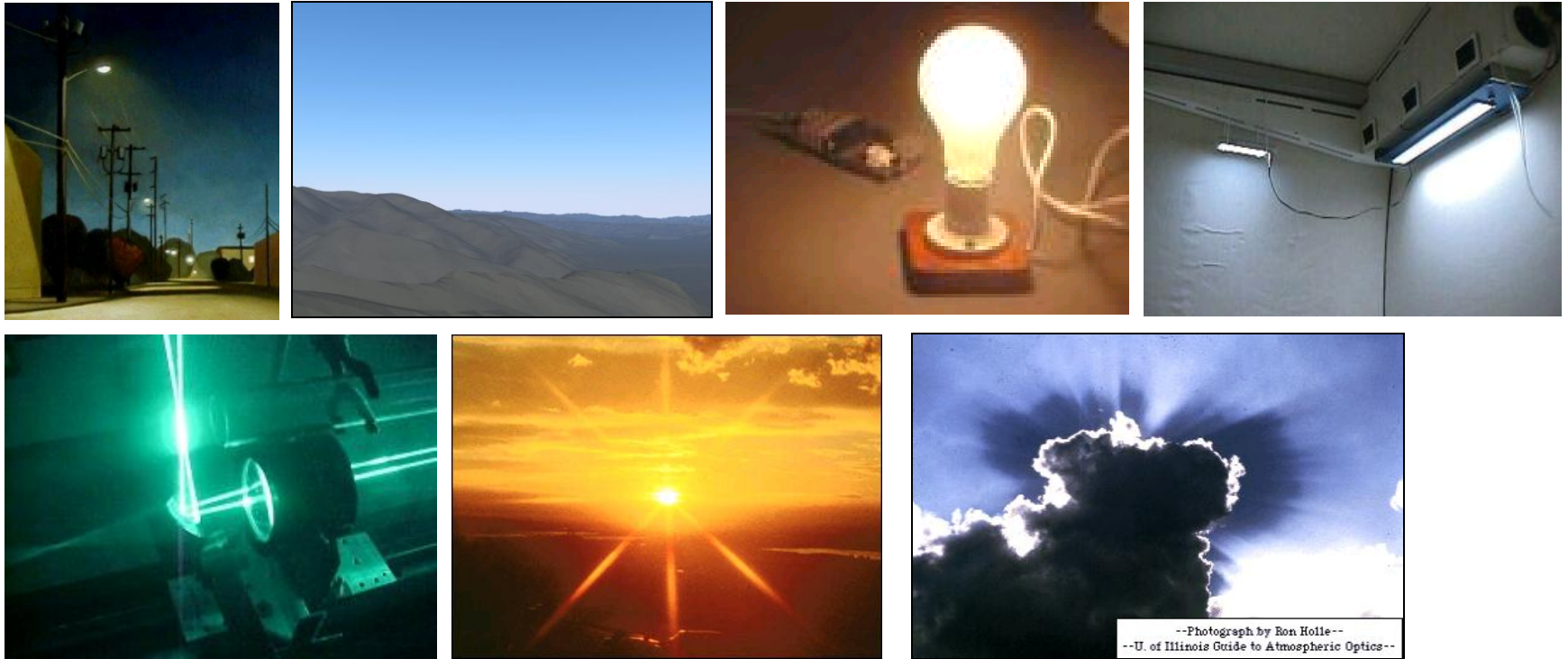
Lots of heat generated.

Less efficient lighting for the same brightness.

No flickers.

Shows continuous spectrum.

# Is there a unified representation for light sources?



How do we compare the light from a street lamp to that from an overcast sky?

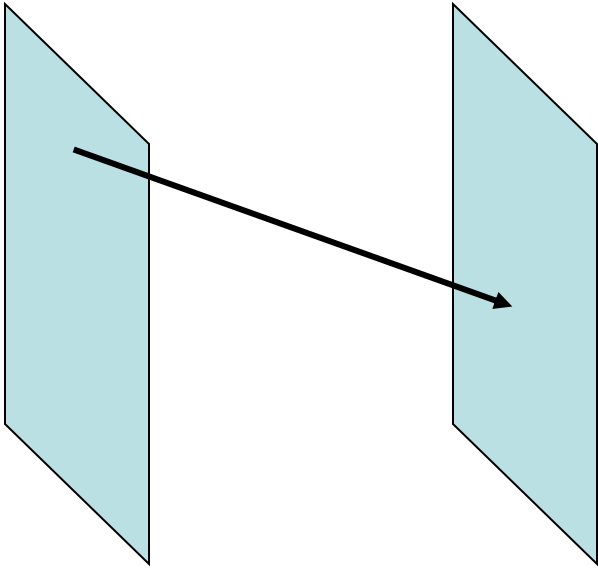
It is important to unify source representation so that algorithms may be developed for all sources instead of one per type of source.

Consider the SPACE of LIGHT RAYS!

# 4D Hypercube of Rays

(x,y)-plane

(p,q)-plane



- Assumes vacuum (no absorption or scattering)
- No fluorescence, phosphorescence

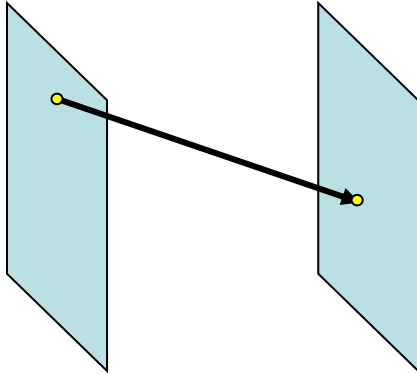
$$\mathcal{M}_{src} \equiv \left\{ (x, y, p, q) : x \in \left[-\frac{h_x}{2}, \frac{h_x}{2}\right], \right. \\ \left. y \in \left[-\frac{h_y}{2}, \frac{h_y}{2}\right], p \in \left[-\frac{h_p}{2}, \frac{h_p}{2}\right], q \in \left[-\frac{h_q}{2}, \frac{h_q}{2}\right] \right\}.$$

# Representation of Sources

Langer and Zucker, CVPR 97

$(x,y)$ -plane

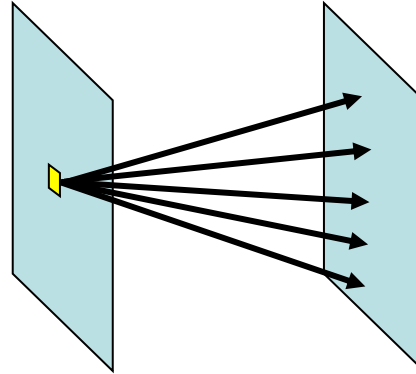
$(p,q)$ -plane



Laser beam – 0D

$(x,y)$ -plane

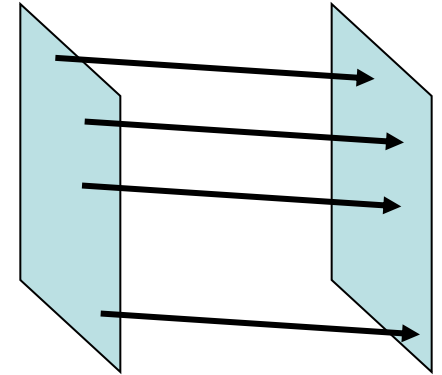
$(p,q)$ -plane



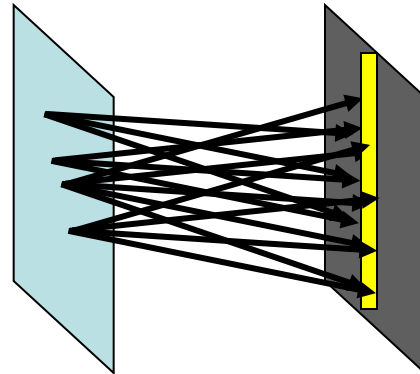
Point source – 2D

$(x,y)$ -plane

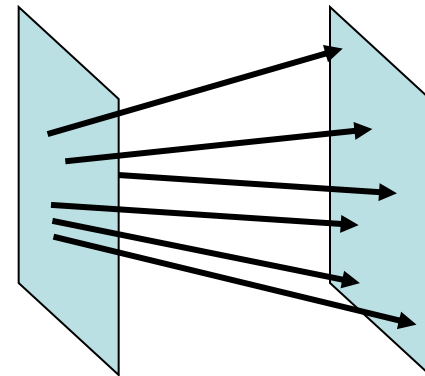
$(p,q)$ -plane



Distant Source (Sun) – 2D



Area source (Sky) with a crack in the door – 3D



Area source (Sky) with door completely open – 4D



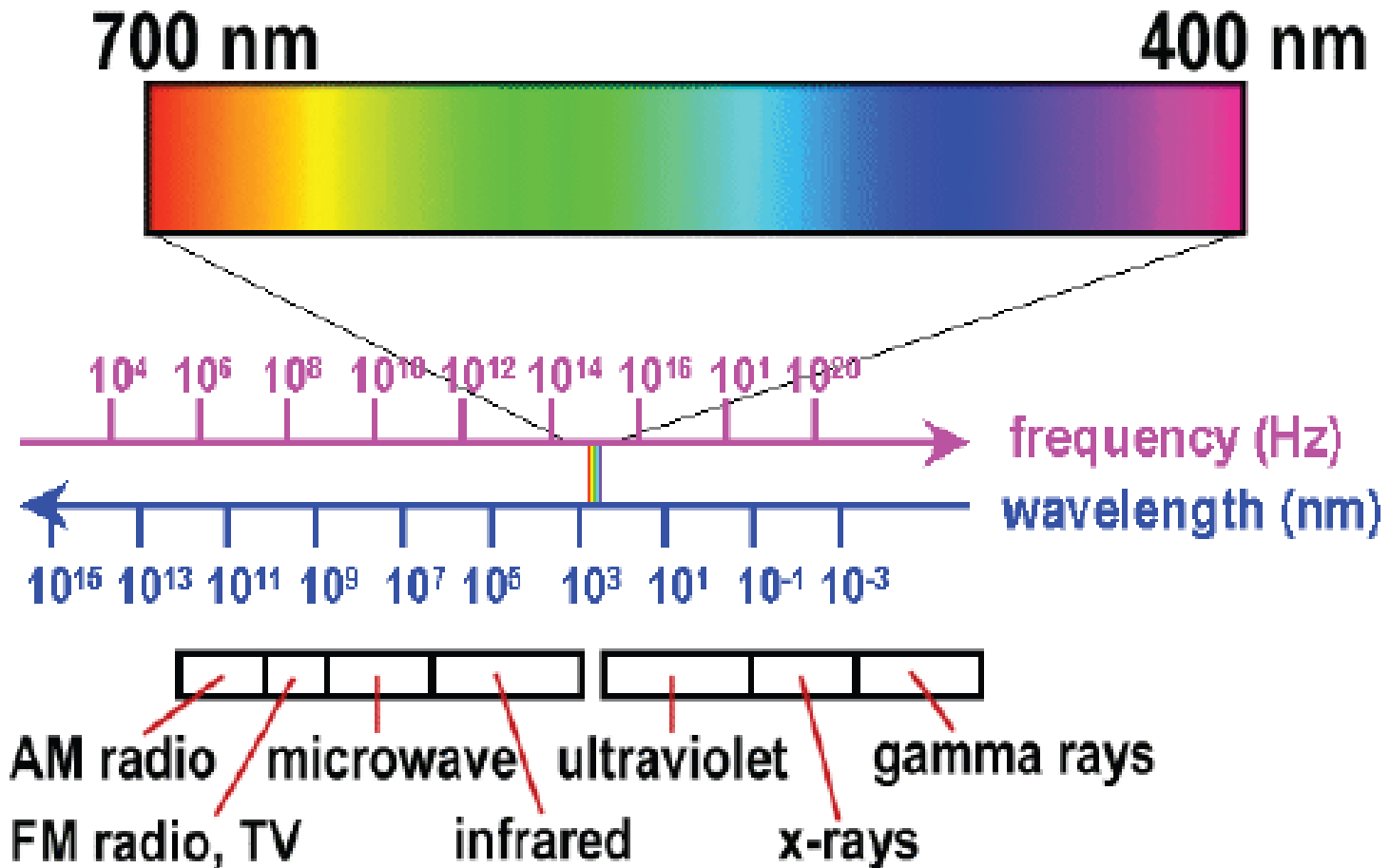
# The Rendering Equation

$$L_o(\mathbf{x}, \omega, \lambda, t) = L_e(\mathbf{x}, \omega, \lambda, t) + \int_{\Omega} f_r(\mathbf{x}, \omega', \omega, \lambda, t) L_i(\mathbf{x}, \omega', \lambda, t) (-\omega' \cdot \mathbf{n}) d\omega'$$

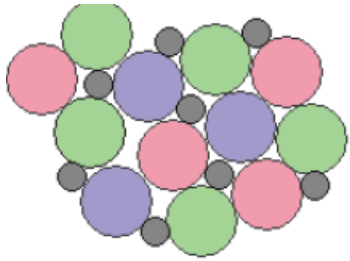
[http://en.wikipedia.org/wiki/Rendering\\_equation](http://en.wikipedia.org/wiki/Rendering_equation)

Color

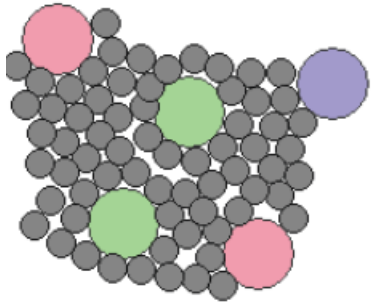
# Visible Spectrum



# Rods, Cones, and Color Perception

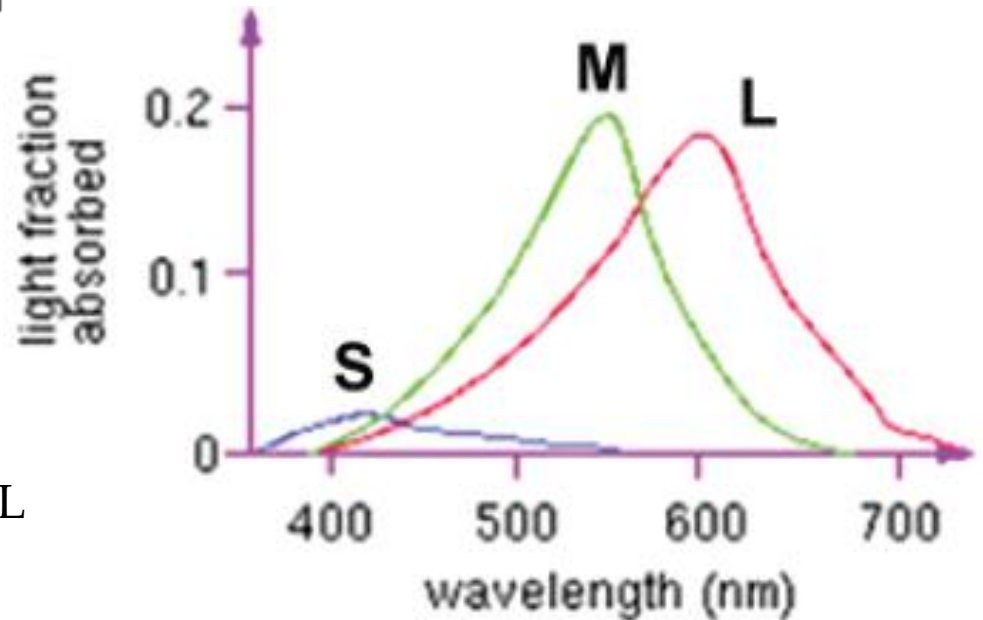


1.35 mm from retina center



8 mm from retina center

3 types of cones: S, M, and L



# Color Models

## Spectrum

allows any radiation (visible or invisible) to be described  
usually unnecessary and impractical

## RGB

convenient for display (CRT uses red, green, and blue phosphors)  
not very intuitive

## HSV

an intuitive color space  
H is hue - what color is it? S is saturation or purity - how non-gray is it? V is value - how bright is it?  
H is cyclic therefore it is a non-linear transformation of RGB

## CIE XYZ

a linear transform of RGB used by color scientists

# Better Color Models












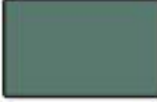
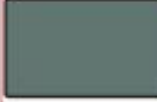
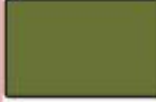




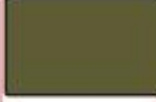






Scanned Paint	101 Samples Riemann Sum	8 Samples IMPASTo	3 Samples RGB w/ K-M	3 Samples RGB Linear
				
				
				
				
				



Figure 11: A painting created with IMPASTo, after a painting by

source:

IMPASTo: a realistic, interactive model for paint  
William Baxter, Jeremy Wendt, Ming C. Lin  
NPAR 2004, June 2004, pp. 45-56.

# Metamers

[http://www.cs.brown.edu/exploratories/freeSoftware/repository/edu/brown/cs/exploratories/applets/spectrum/metamers\\_java\\_browser.html](http://www.cs.brown.edu/exploratories/freeSoftware/repository/edu/brown/cs/exploratories/applets/spectrum/metamers_java_browser.html)

# Color Constancy



Figure 5.4: All the center squares have the same lightness; the apparent lightness, however, is profoundly influenced by the surrounding squares.

**fig:lightness-squares**



Figure 5.5: The ratio of the center square's darkness to the surrounding square's darkness is approximately the same in each example; we tend to see the center squares as exhibiting far less variation in lightness than those in the previous figure.



# Visible Range of Intensities

Human Overall Luminance Vision Range  
(14 orders of magnitude, scale in log cd/m<sup>2</sup>)



Human Simultaneous  
Luminance Vision Range

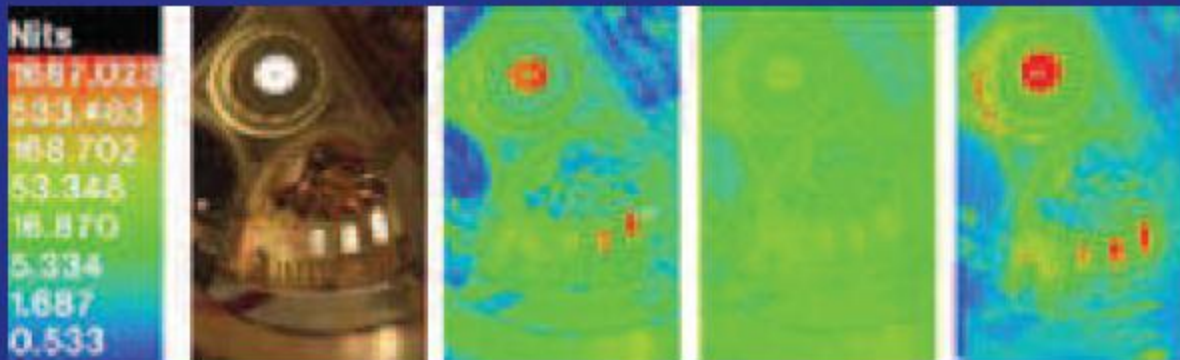


Today's Devices



# Visible Range of Intensities

Conventional CRTs have 600:1 dynamic range  
Flat-panel LCDs are 500:1.



HDR image, range, conventional display, HDR display

Goal for displays: 1,000,000 : 1 contrast or better!