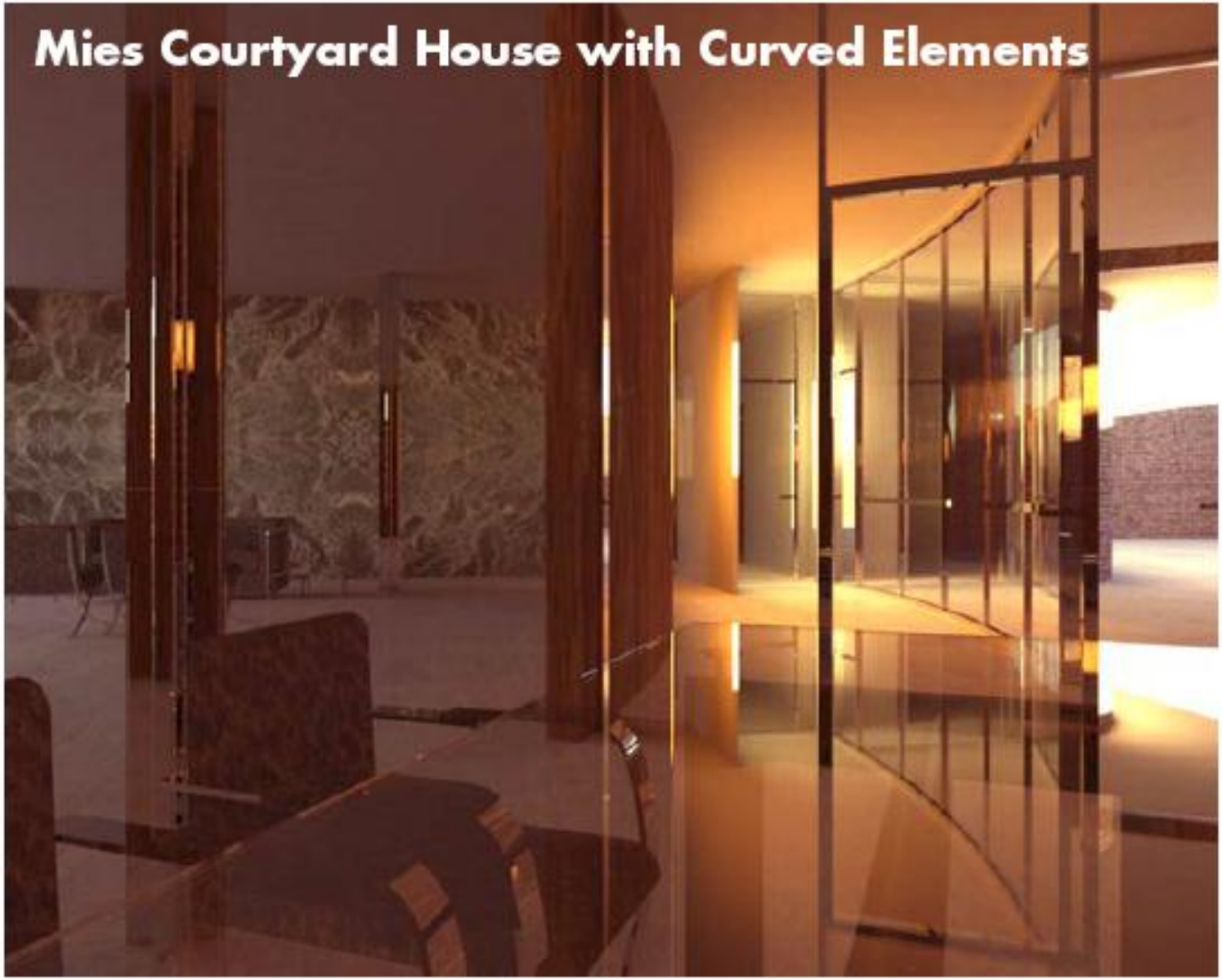
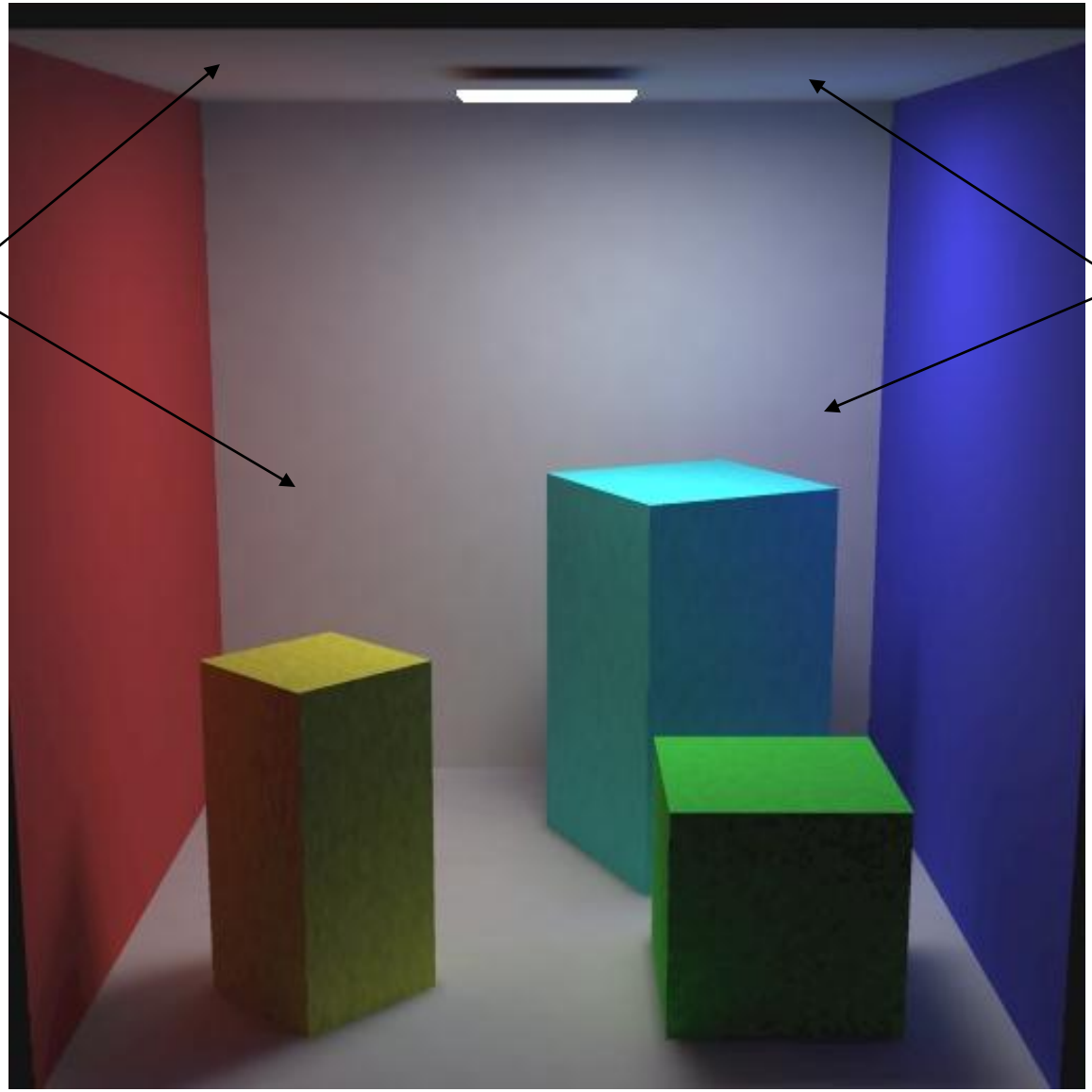


Modeling: Stephen Duck; Rendering: Henrik Wann Jensen

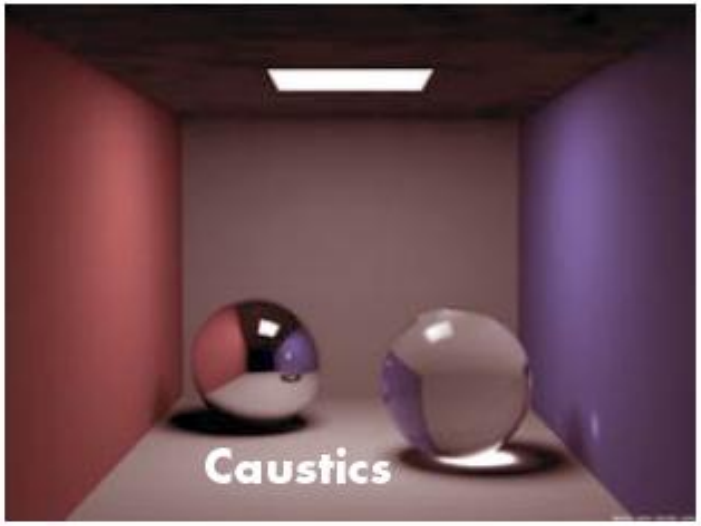
Radiosity

Thanks to Kavita Bala, Pat Hanrahan, Doug James, Ledah Casburn

Cornell Box



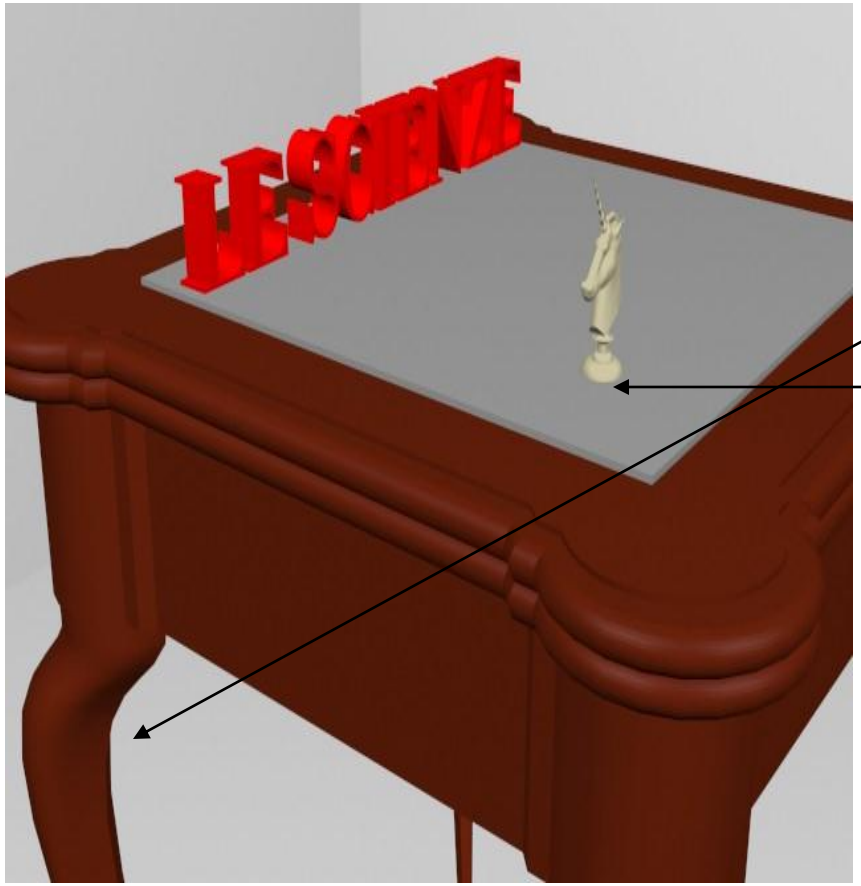
Lighting Effects



The ambient lighting in the upper-right image is approximated by a constant value. This is typical of most scanline algorithms. The middle and lower-left images were rendered with a ray tracing global illumination algorithm.

The middle image was rendered with no ambient light calculations. The lower-left image was rendered with several levels of diffuse re-reflection to give a better approximation of the ambient light in this scene.

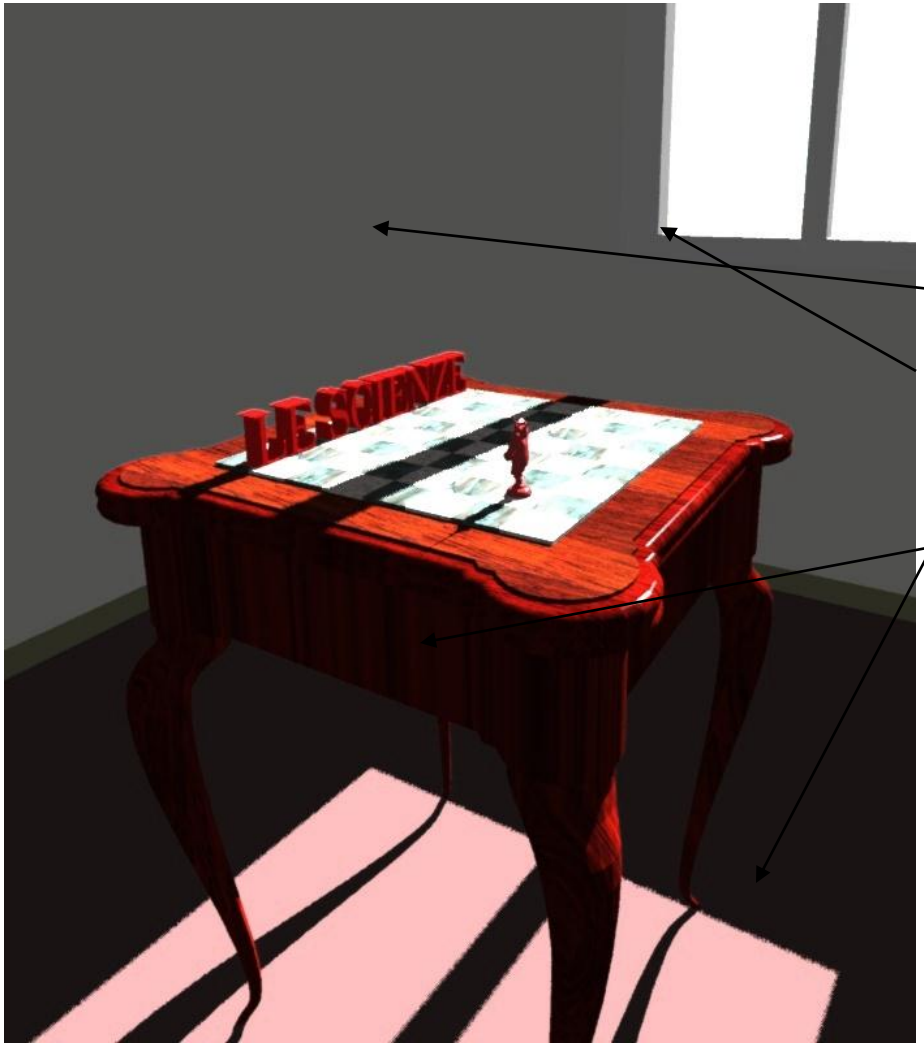
Phong Shading



Plastic looking scene

- no object interactions
- no shadows

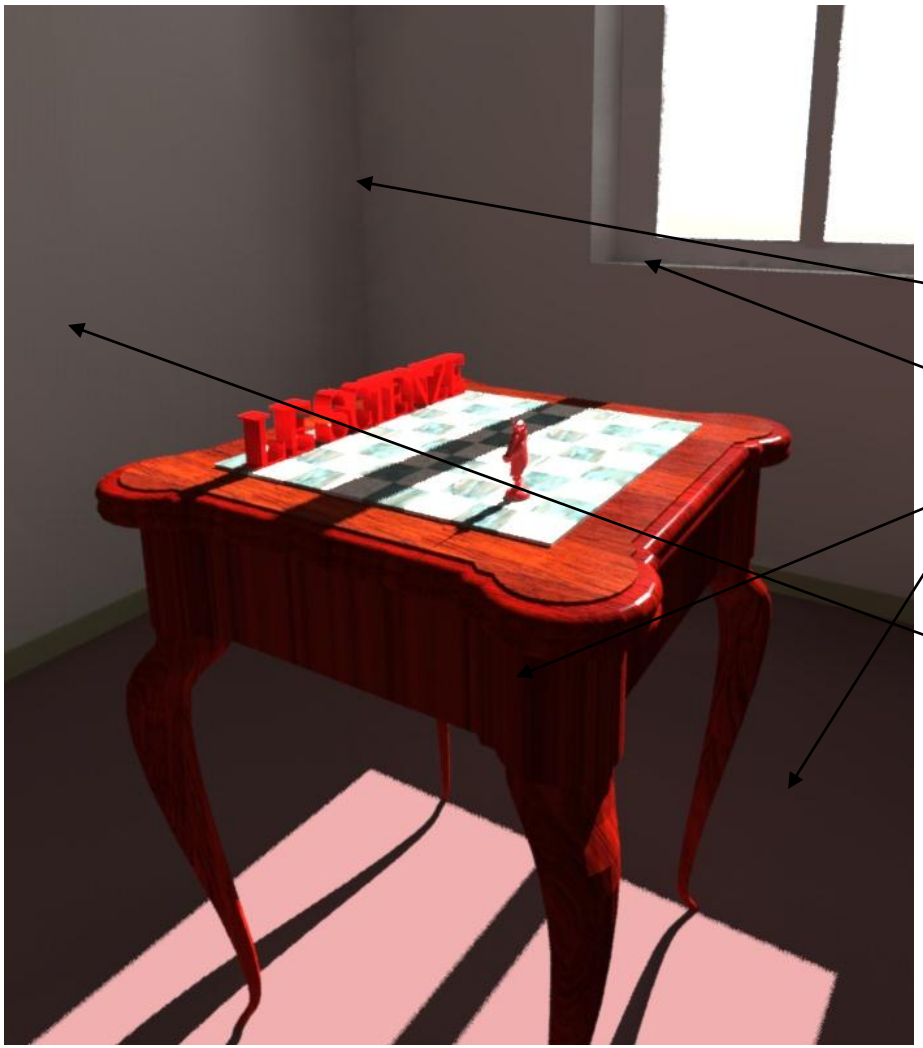
Ray Tracing



Scene doesn't look realistic enough.

- where is the corner of room?
- is window flush with wall?
- is the carpet and wood supposed to be this dark?

Radiosity – today's topic

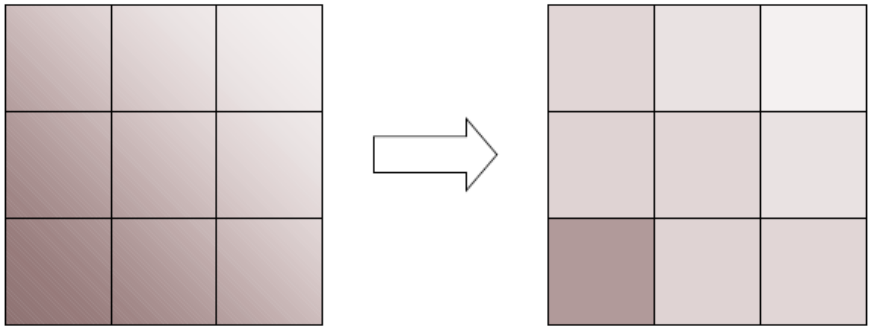


Indirect lighting affects realism.

- room has a corner
- window has depth
- carpet and wood on table is lighter
- walls look more pink

Planar piecewise constancy assumption

- Subdivide scene into small "uniform" polygons



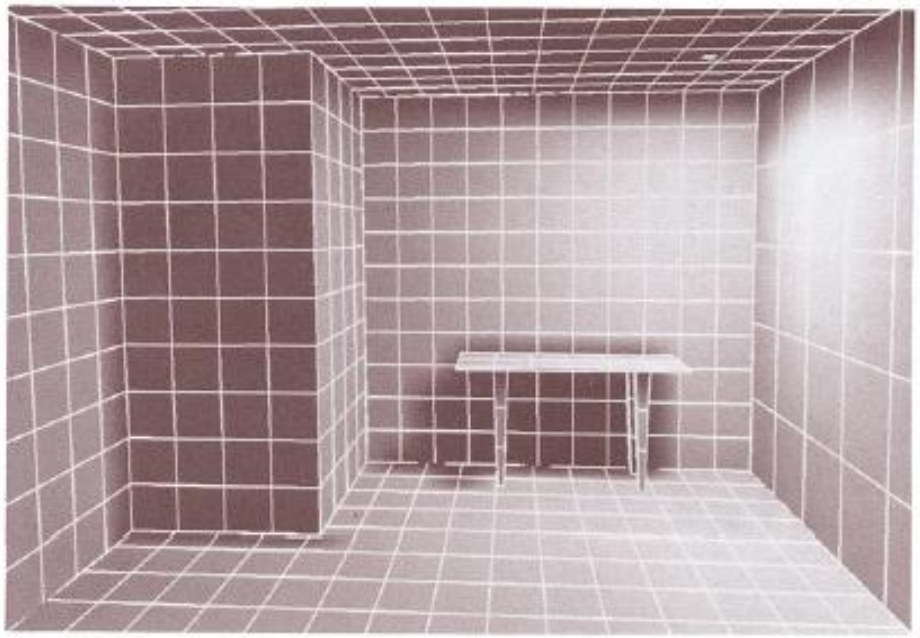


Table in room sequence from Cohen and Wallace

Diffuse Interreflections - Radiosity

- Consider lambertian surfaces and sources.
- Radiance independent of viewing direction.
- Consider total power leaving per unit area of a surface.
- Can simulate soft shadows and color bleeding from diffuse surfaces.
- Used abundantly in heat transfer literature

Irradiance, Radiosity

- Irradiance E is the power **received** per unit surface area
  - Units: W/m^2

- Radiosity
  - Power per unit area **leaving** the surface (like irradiance)

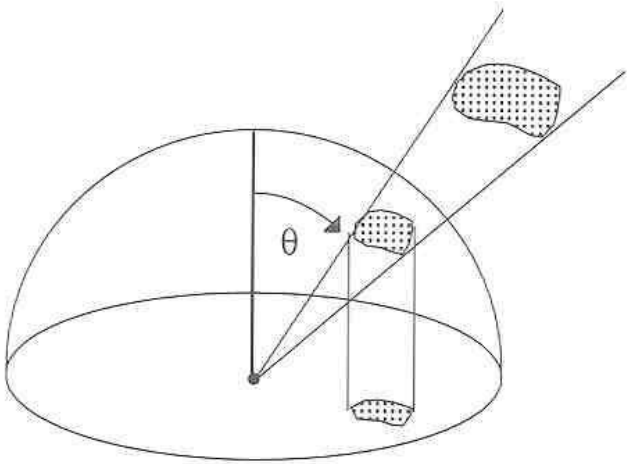
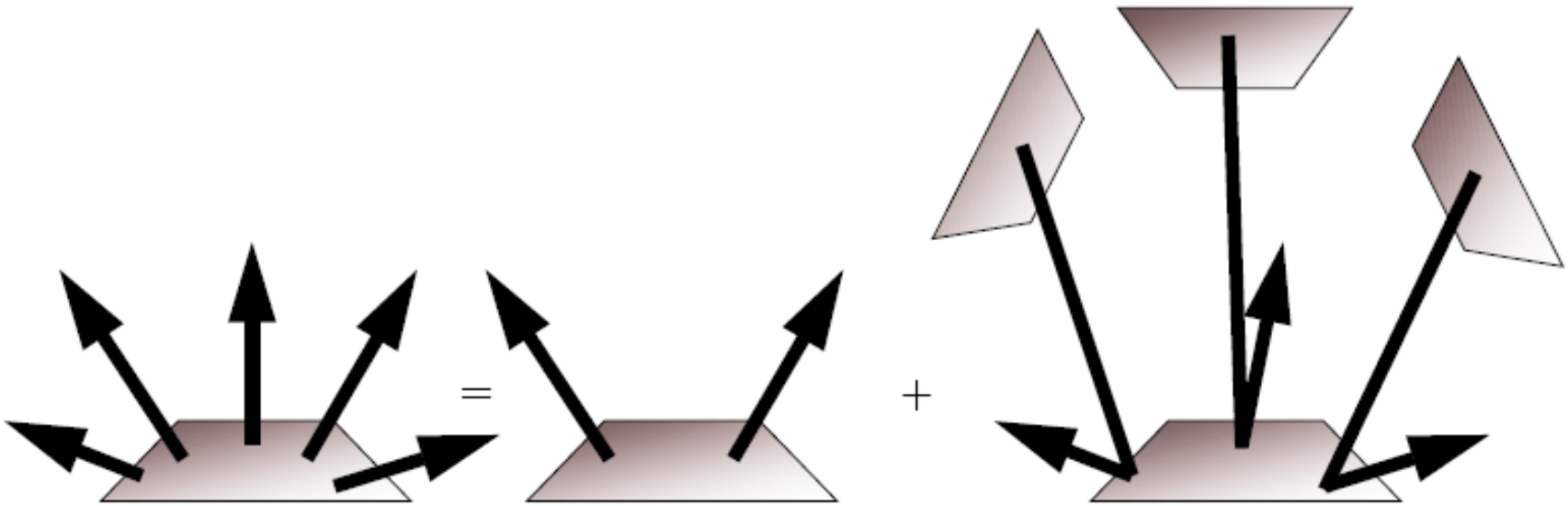


Figure 2.8: *Projection of differential area.*

Conservation of Energy



Emitted power = self-emitted power + received & reflected power

Power Equation

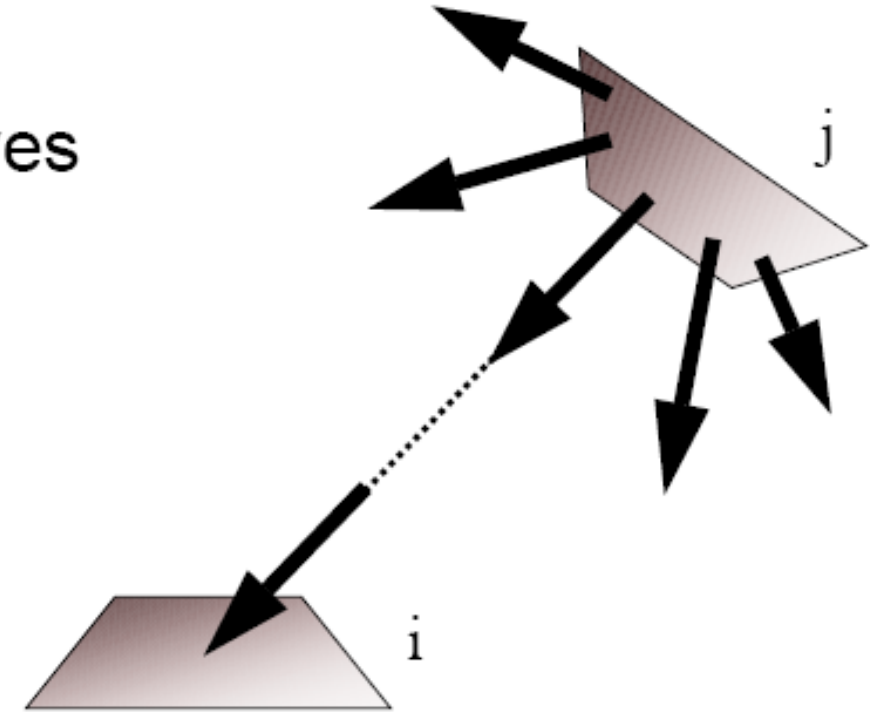
- Power from each polygon:

$$\forall i : \Phi_i = \Phi_{ei} + \rho_i \sum_{j=1}^{N} \Phi_j \, F(j \rightarrow i)$$

- Linear System of Equations:
  - Φ_i : power of patch i (unknown)
  - $\Phi_{e,i}$: emission of patch i (known)
  - ρ_I : reflectivity of patch i (known)
  - F(j→i): form-factor (coefficients of matrix)

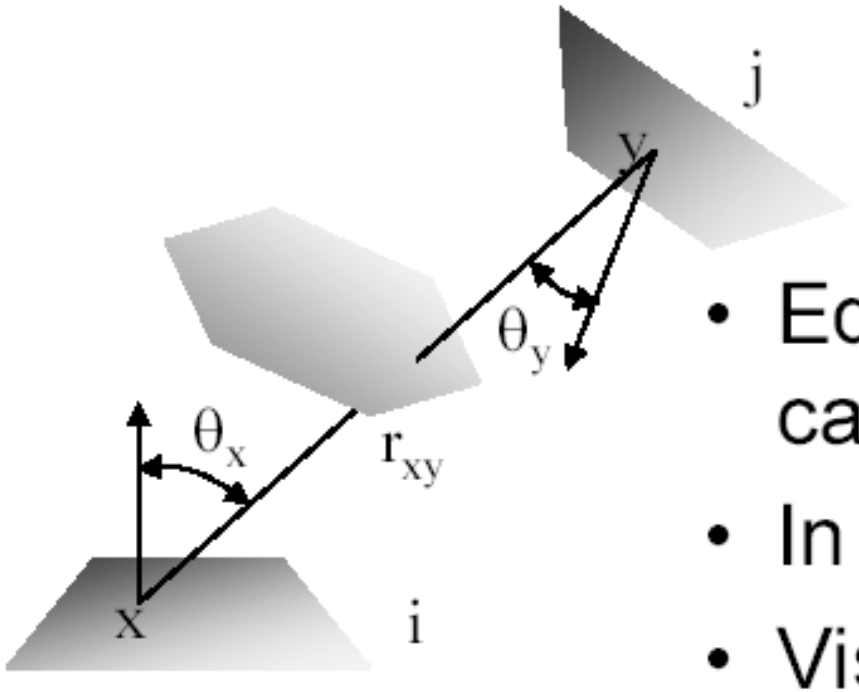
Form Factor

- $F_{j \to i}$ = the fraction of power emitted by j, which is received by i
- Area
  - if i is smaller, it receives less power
- Orientation
  - if i faces j, it receives more power
- Distance
  - if i is further away, it receives less power



Form Factor

$$F(j \to i) = \frac{1}{A_j} \int_{A_i} \int_{A_j} \frac{\cos\theta_x \cos\theta_y}{\pi r_{xy}^2} V(x,y)\, dA_y\, dA_x$$



- Equations for special cases (polygons)
- In general hard problem
- Visibility makes it harder

Form Factors Invariant

$$F(j \rightarrow i) = \frac{1}{A_j} \int_{A_i} \int_{A_j} \frac{\cos\theta_x \cos\theta_y}{\pi r_{xy}^2} V(x,y)\, dA_y\, dA_x$$

$$F(i \rightarrow j) = \frac{1}{A_i} \int_{A_j} \int_{A_i} \frac{\cos\theta_x \cos\theta_y}{\pi r_{xy}^2} V(x,y)\, dA_x\, dA_y$$

$$F(i \rightarrow j) A_i = F(j \rightarrow i) A_j$$

Form Factor Computation

$$F(j \to i) = \frac{1}{A_j} \int_{A_i} \int_{A_j} \frac{\cos\theta_x \cos\theta_y}{\pi r_{xy}^2} V(x,y)\, dA_y\, dA_y$$

- Schroeder and Hanrahan derived an analytic expression for polygonal surfaces.
- In general, computing double integral is hard.
- Use Monte Carlo Integration.

Power → Radiosity

$$\Phi_i = \Phi_{e,i} + \rho_i \sum_{j=1}^{N} \Phi_j F(j \to i)$$

Divide by A_i

$$\frac{\Phi_i}{A_i} = \frac{\Phi_{e,i}}{A_i} + \rho_i \sum_{j=1}^{N} \frac{\Phi_j F(j \to i)}{A_i}$$

$$B_i = B_{e,i} + \rho_i \sum_{j=1}^{N} \frac{\Phi_j \dfrac{F(i \to j) A_i}{A_j}}{A_i}$$

$$B_i = B_{e,i} + \rho_i \sum_{j=1}^{N} \frac{\Phi_j F(i \to j)}{A_j}$$

$$B_i = B_{e,i} + \rho_i \sum_{j=1}^{N} B_j F(i \to j)$$

Linear System of Radiosity Equations

$$\forall \text{patches i:} \qquad B_i = B_{ei} + \rho_i \sum_j F_{i \to j} B_j$$

$$\begin{bmatrix} 1-\rho_1 F_{1\to 1} & -\rho_1 F_{1\to 2} & \cdots & -\rho_1 F_{1\to n} \\ -\rho_2 F_{2\to 1} & 1-\rho_2 F_{2\to 2} & \cdots & -\rho_2 F_{2\to n} \\ \cdots & \cdots & \cdots & \cdots \\ -\rho_n F_{n\to 1} & -\rho_n F_{n\to 2} & \cdots & 1-\rho_n F_{n\to n} \end{bmatrix} \begin{bmatrix} B_1 \\ B_2 \\ \cdots \\ B_n \end{bmatrix} = \begin{bmatrix} B_{e1} \\ B_{e2} \\ \cdots \\ B_{en} \end{bmatrix}$$

Known

Unknown

Known

- Matrix Inversion to Solve for Radiosities.

Iterative approaches

- Jacobi iteration
- Start with initial guess for energy distribution (light sources)
- Update radiosity/power of all patches based on the previous guess

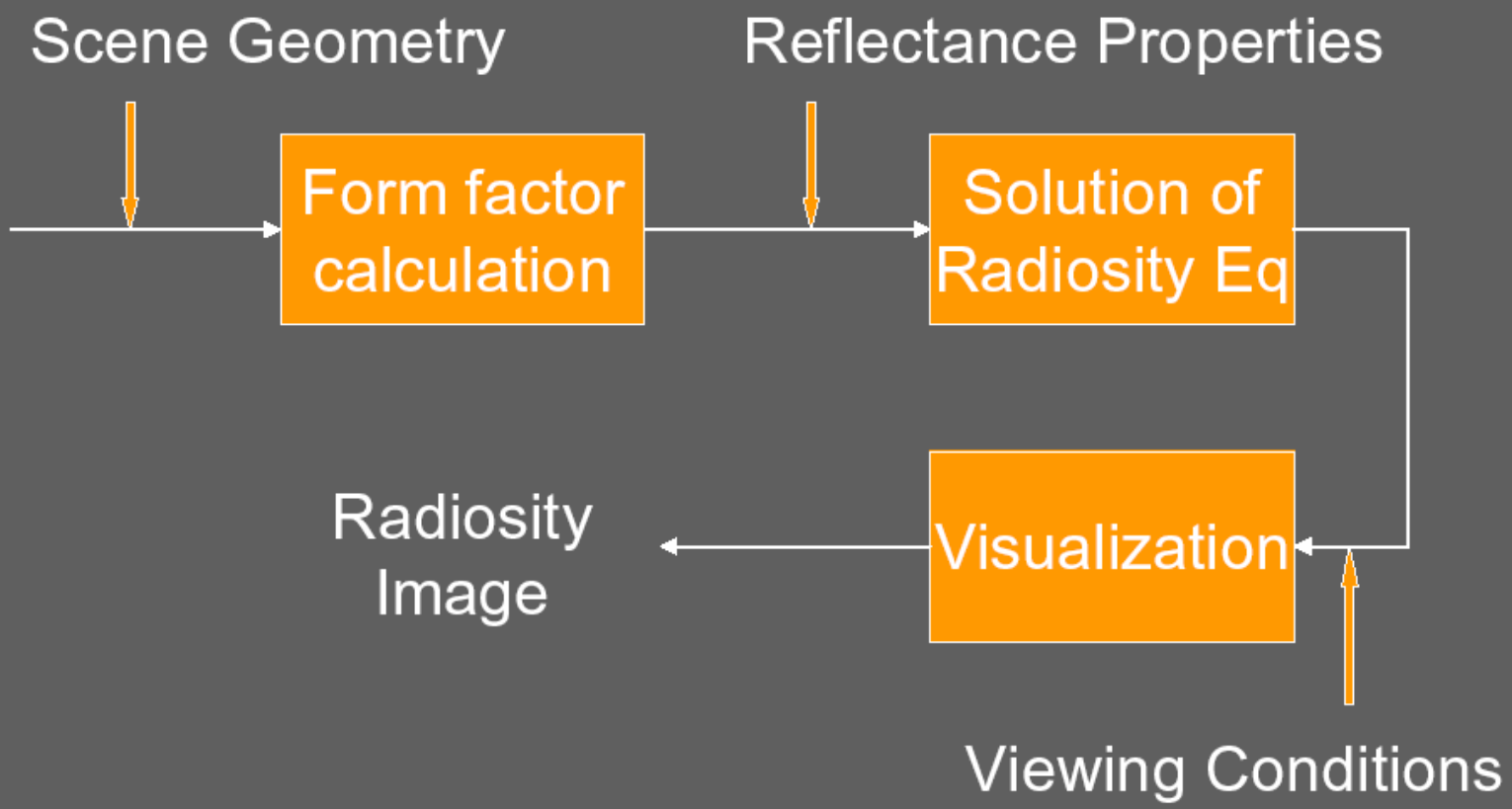
$$B_i = B_{e,i} + \rho_i \sum_{j=1}^{N} B_j F(i \rightarrow j)$$

new value

old values

- Repeat until converged

Radiosity "Pipeline"



Being Smart about Form Factors

- Form factors depend only on scene geometry. If geometry is constant, they only need to be calculated once.
- Solution of the radiosity system is independent of viewing conditions, so if only the viewer position changes, it only needs to be solved once—can walk around the scene in real-time after it's initially generated

Being Smart about Form Factors

Form factors are complicated. Full numeric approximation of these is expensive—many special cases may be solved analytically.

Because we assume that radiosity is constant across a patch, two patches are typically assumed to be fully inter-visible or not at all inter-visible. That means that patches have to be small enough to resolve shadows and other complexities

How to perform visibility testing?

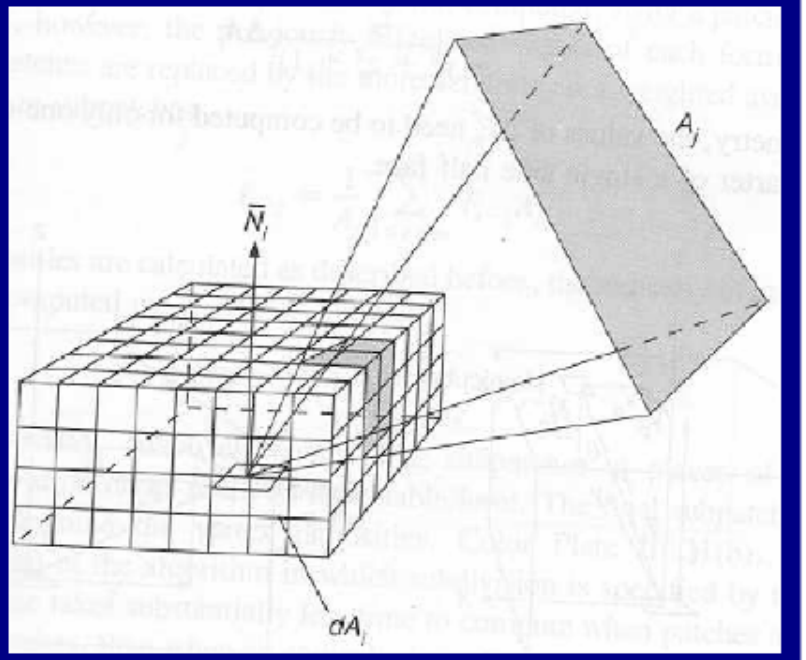
Two basic methods, both of which have aliasing problems:

- Raycasting (typically slow)
- Hemicube method (z-buffer exploit)

Anti-aliasing may be performed in both cases

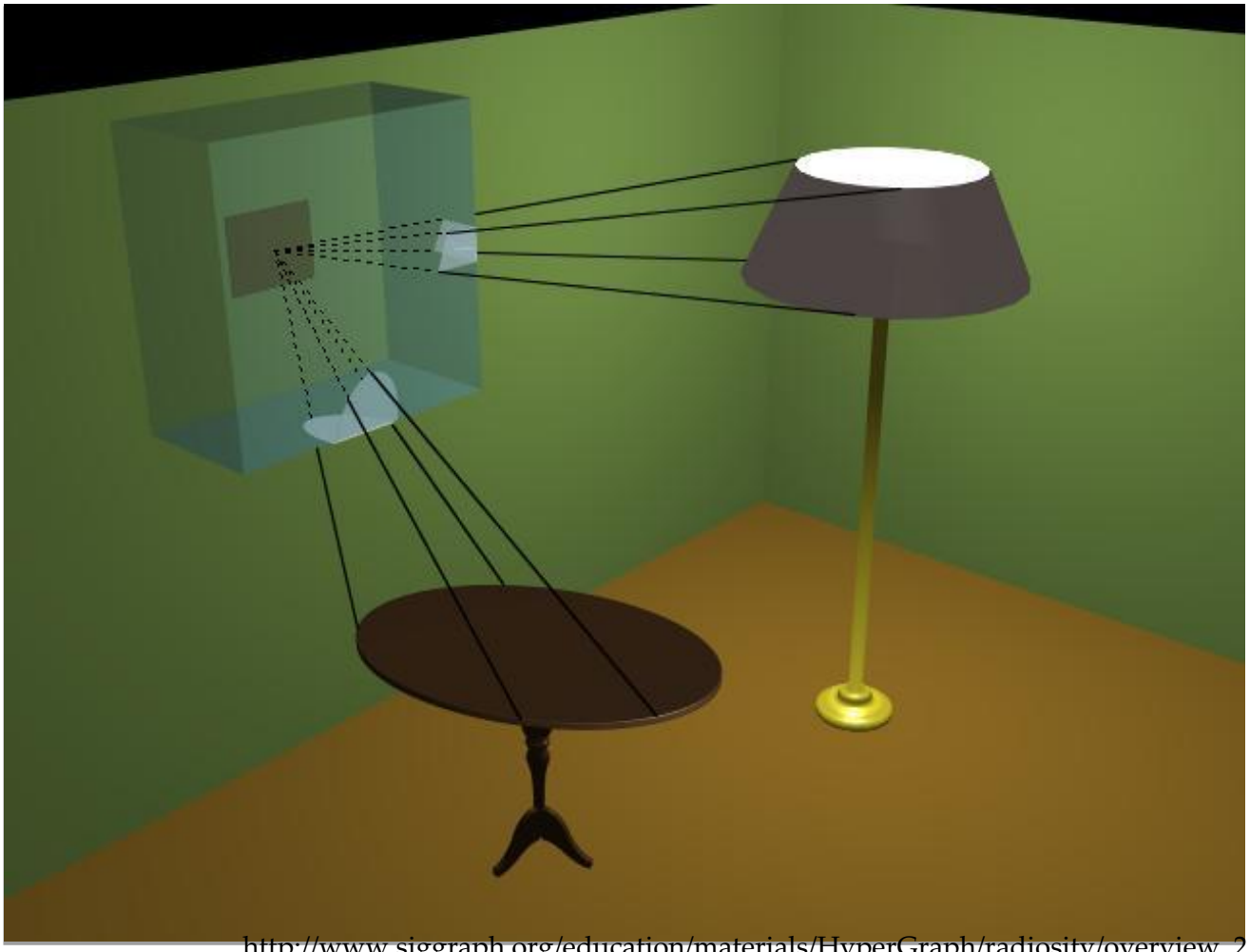
Hemicube Visibility Testing

- Render the entire scene from the perspective of the center of the current patch
- Rather than color, store patch identifiers, using the z-buffer to determine visibility
- Takes advantage of graphics hardware



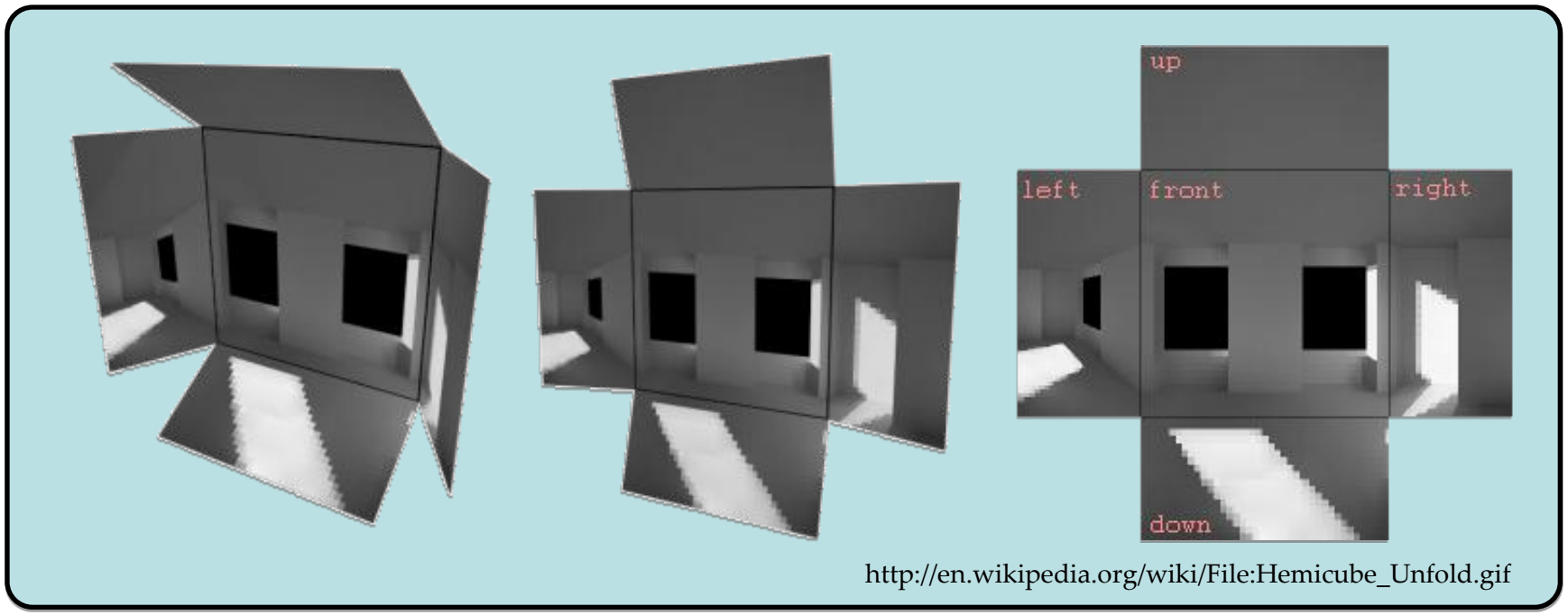
R. Ramamoorthi

Hemicube in Action

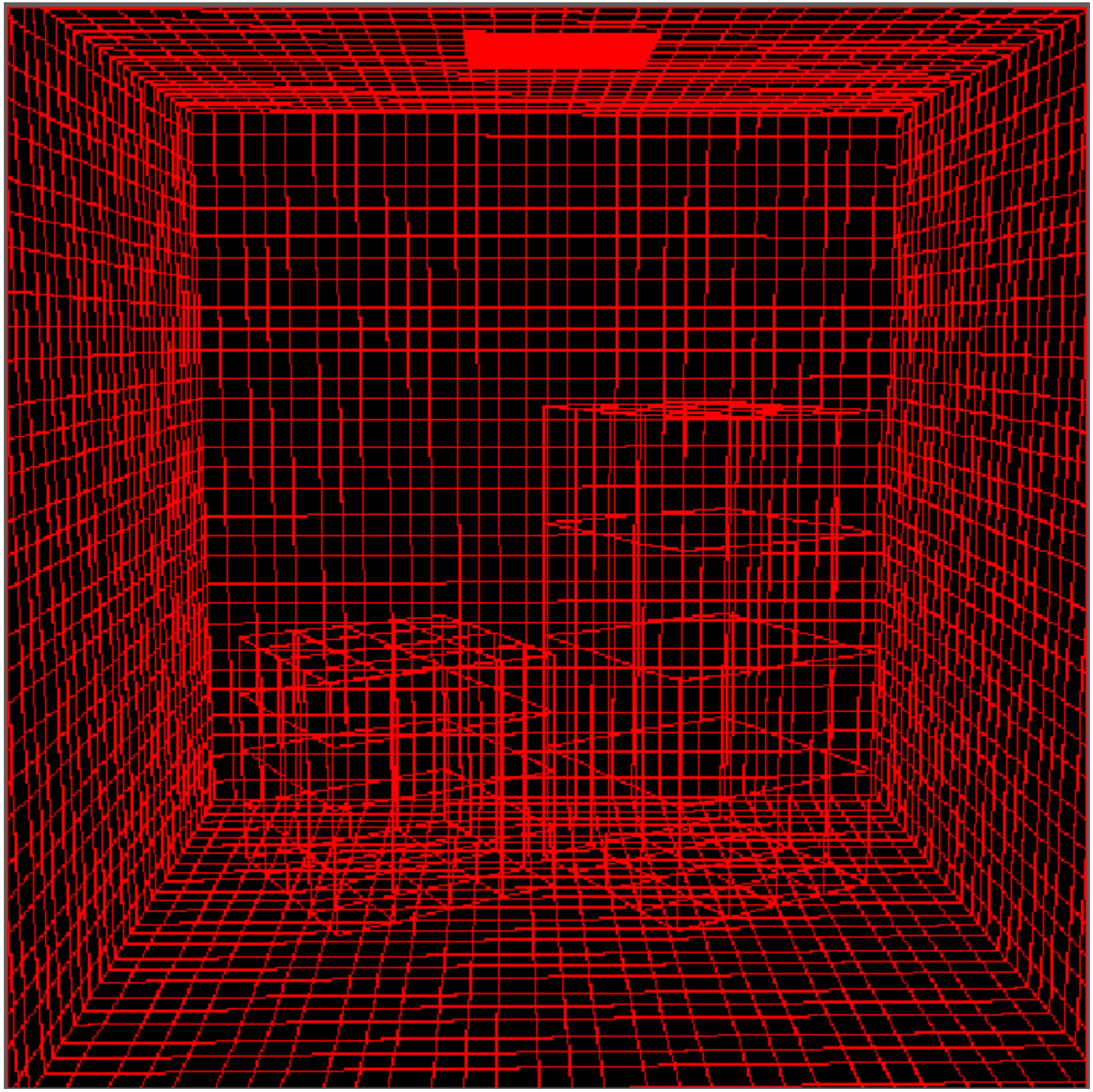


http://www.siggraph.org/education/materials/HyperGraph/radiosity/overview_2.htm

Hemicube in Action

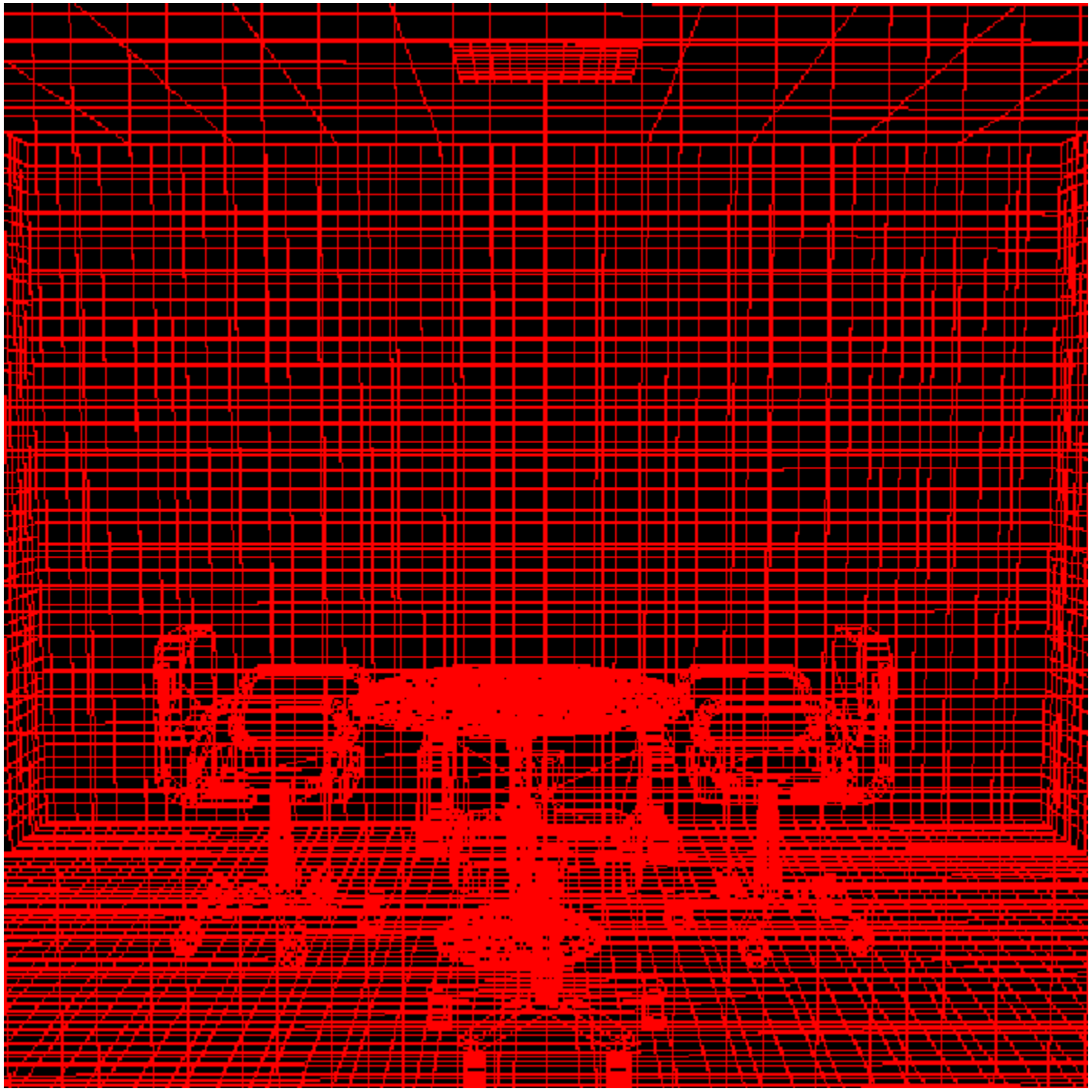


http://en.wikipedia.org/wiki/File:Hemicube_Unfold.gif



Wireframe

- Classical Approach
- No Interpolation



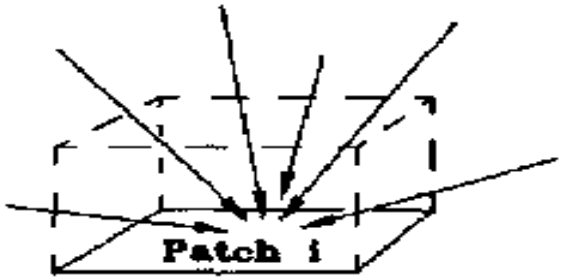
Wireframe

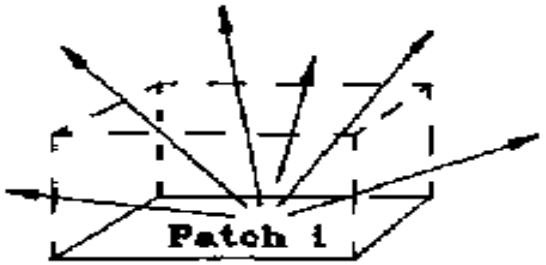
- Classical Approach
- Low Res

- Classical Approach
- High Res
- More accurate

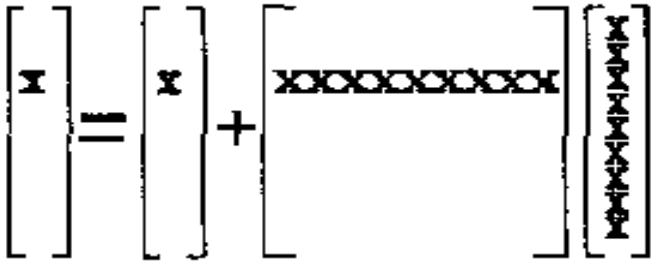
- Classical Approach
- High Res
- Interpolated

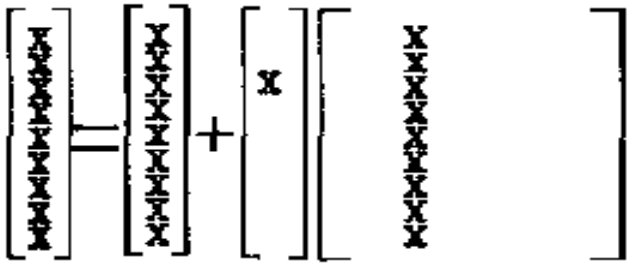
Progressive Solution





GATHERING vs. SHOOTING





$$B_i = E_i + \sum_{j=1}^{N} (\rho_i F_{ij}) B_j$$

For all j:

$$B_j = B_j + B_i (\rho_j F_{ji})$$

where: $F_{ji} = F_{ij} A_i / A_j$

Figure 1: Gathering vs. Shooting

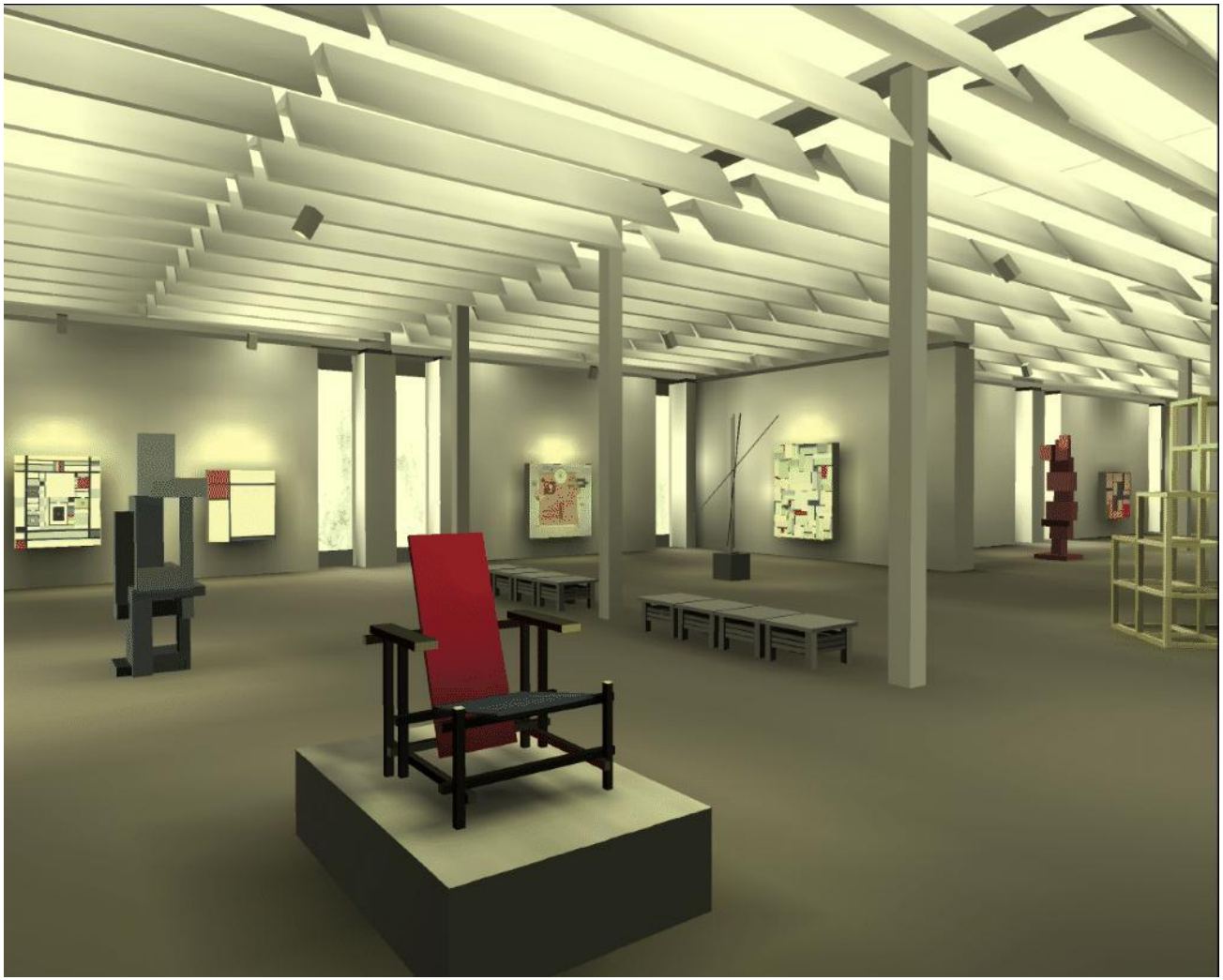
A Progressive Refinement Approach to Fast Radiosity Image Generation, Cohen et al 88

PROGRESSIVE SOLUTION

The above images show increasing levels of global diffuse illumination. From left to right: 0 bounces, 1 bounce, 3 bounces.

Sample Scenes

Sample Scenes



From Cohen, Chen, Wallace and Greenberg 1988

Sample Scenes

Sample Scenes

Sample Scenes

Radiosity Summary

Classic radiosity = finite element method

Assumptions

- Diffuse reflectance
- Usually polygonal surfaces

Advantages

- Soft shadows and indirect lighting
- View independent solution
- Precompute for a set of light sources
- Useful for walkthroughs

Review: Local vs. Global Illumination

- Global illumination: Ray tracing
  - Realistic specular reflection/transmission
  - Simplified diffuse reflection*
- Global illumination: Radiosity
  - Realistic diffuse reflection
  - Diffuse-only: No specular interaction*

indirect direct both

Radiosity Examples

http://www.autodesk.com/us/lightscape/examples/html/index.htm

Raytracing Examples

http://www.povray.org/

Raytracing Examples

Radiosity Examples

http://www.autodesk.com/us/lightscape/examples/html/index.htm

Image vs. Object Space

- Image space: Ray tracing
  - Trace backwards from viewer
  - View-dependent calculation
  - Result: rasterized image (pixel by pixel)
- Object space: Radiosity
  - Assume only diffuse-diffuse interactions
  - View-independent calculation
  - Result: 3D model, color for each surface patch
  - Can render with OpenGL

A Better Idea: The Best of Both Worlds

Combine radiosity and raytracing

Goal: Represent four forms of light transport:

- Diffuse -> Diffuse
- Diffuse -> Specular
- Specular -> Diffuse
- Specular -> Specular

Two-pass approach, one for each method

First Pass: Enhanced Radiosity

- Diffuse -> Diffuse
  - Normal diffuse reflection model
  - Diffuse transmission (translucent objects) – requires modified form factor
- Specular -> Diffuse
  - Specular transmission (transparent objects, e.g. windows) – involves extended form factor
  - Specular reflection (reflective objects, e.g. mirrors) – create actual “mirror image” environment with copies of all patches. Expensive!

Enhanced Radiosity - Evaluation

- Only accounts for a single specular reflection (try creating “mirror image” environments for two mirrors facing each other)
- Accurate diffuse model
- Equations solved as in the classical method
- Still viewer-independent

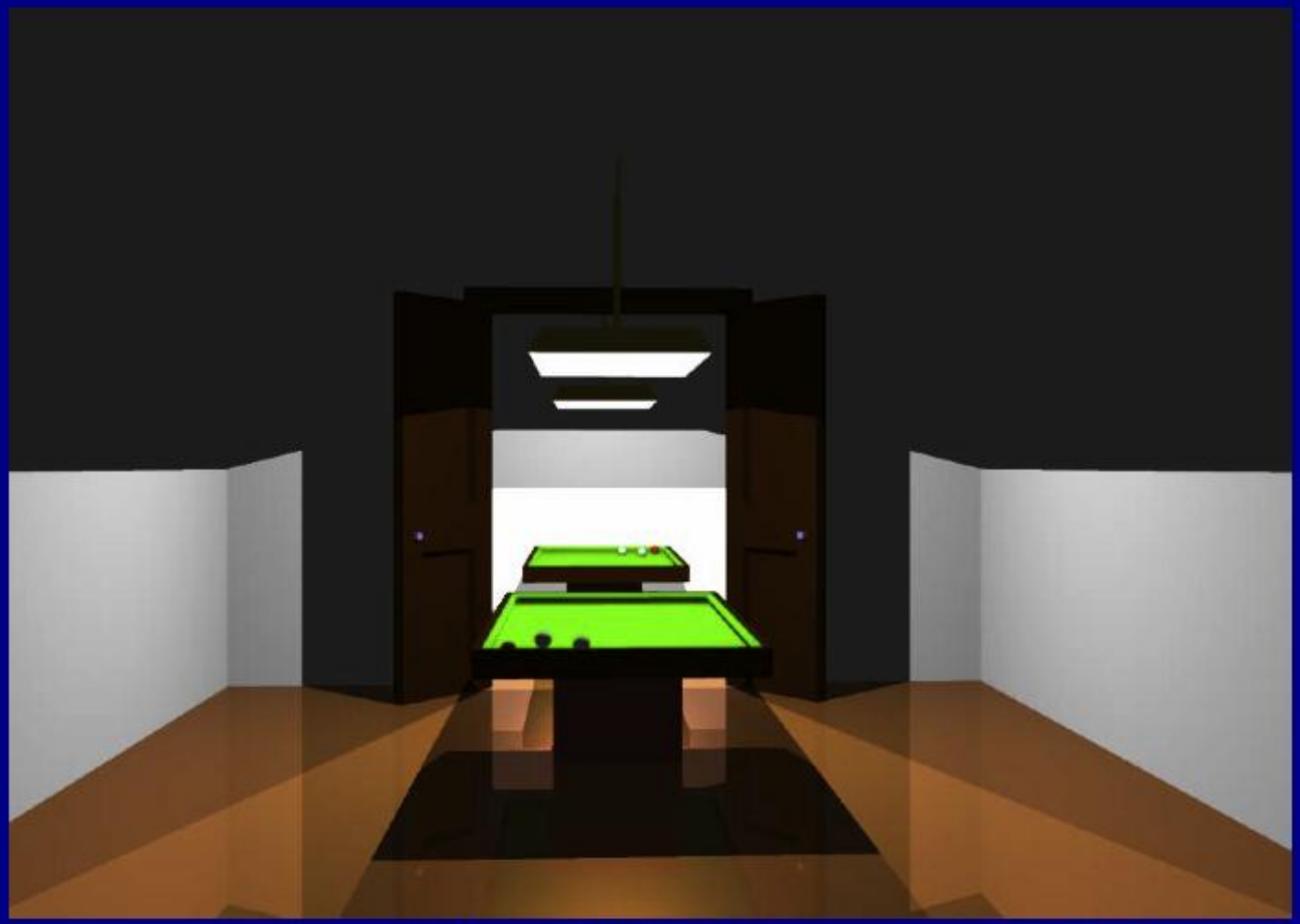
Second Pass: Enhanced Raytracing

- Specular -> Specular
  - Reflection and transmission as in classical method
- Diffuse -> Specular
  - Use the radiosity calculated in the first pass
  - Integrate incoming light over a hemisphere (or hemicube), or approximate with a tiny frustum in the direction of reflection
  - Recurse if visible surface is specular

First Pass Result

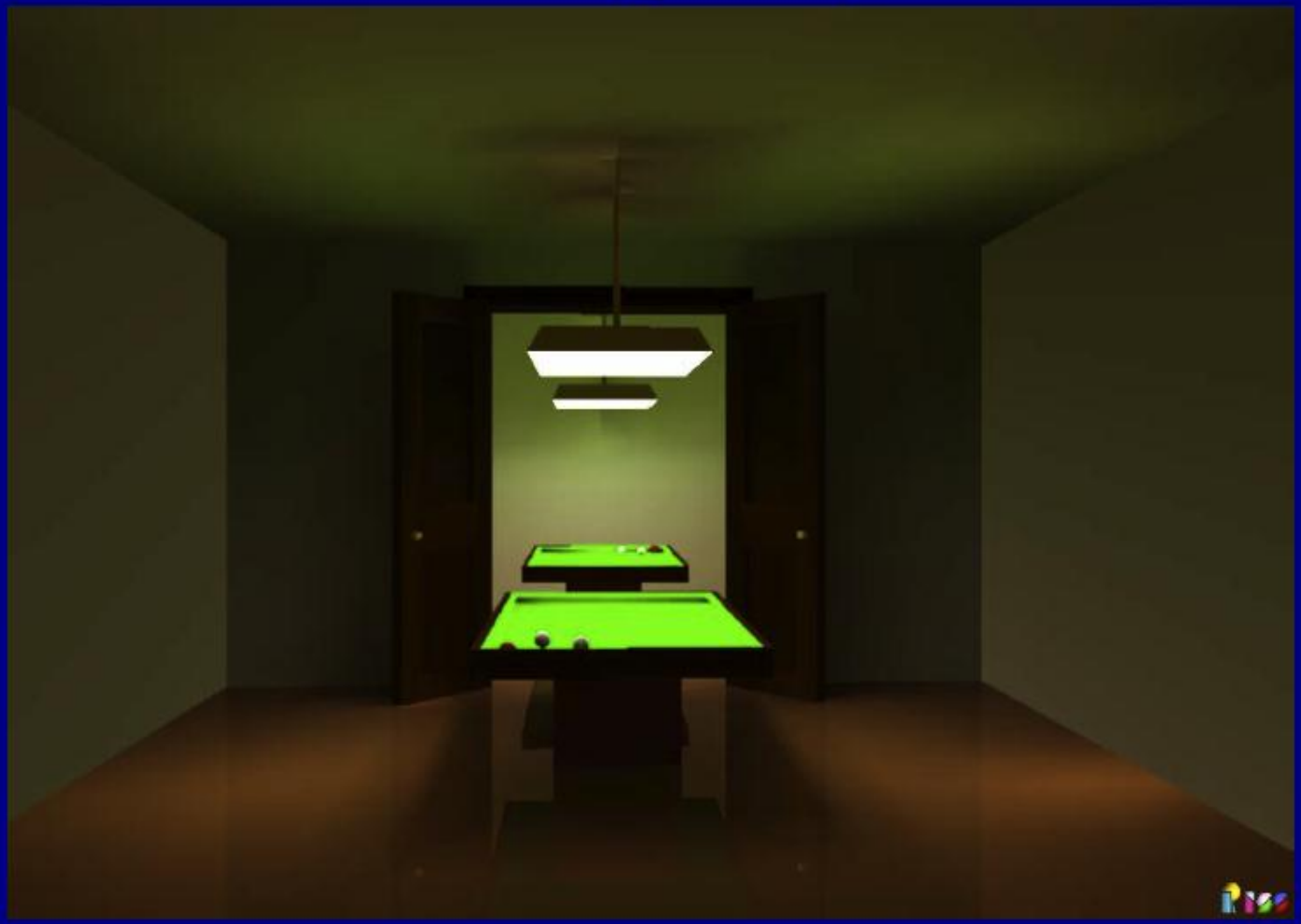
http://www.cg.tuwien.ac.at/research/rendering/rays-radio/

Second Pass Result
(radiosity info. not yet used, just raytracing)



http://www.cg.tuwien.ac.at/research/rendering/rays-radio/

Combined (Final) Result



http://www.cg.tuwien.ac.at/research/rendering/rays-radio/

Two-Pass Global Illumination: Evaluation

Very expensive. Takes the cost of radiosity added to the cost of raytracing and then throws even more calculations into the mix

Many approximations remain, particularly in specular -> diffuse and diffuse -> specular transport