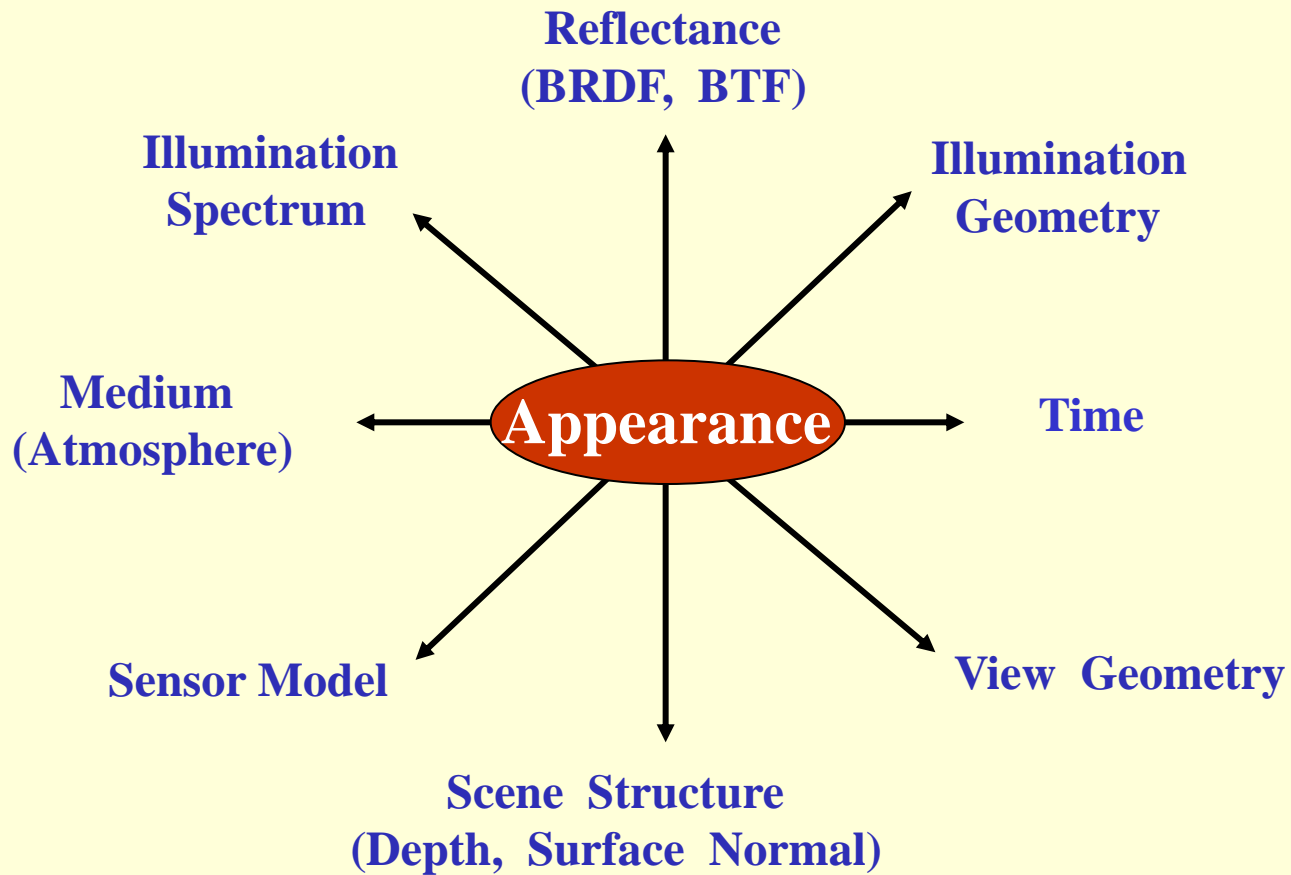


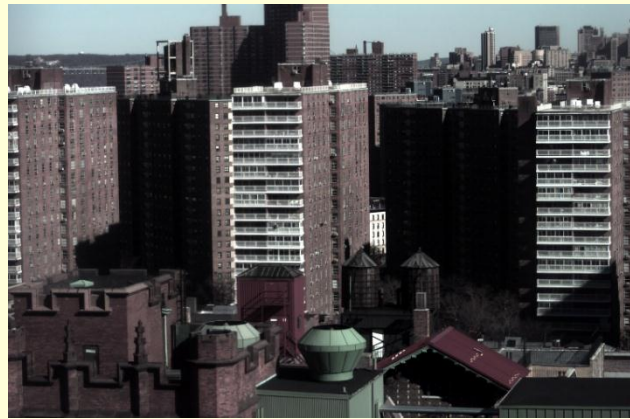
# Lighting and Shadows

Thanks to Langer-Zucker, Henrik Wann Jensen, Ravi Ramamoorthi, Hanrahan, Preetham

# Appearance of An Outdoor Scene



# Illumination Direction



**February 18<sup>th</sup> 2002, 10 AM  
Clear and Sunny**



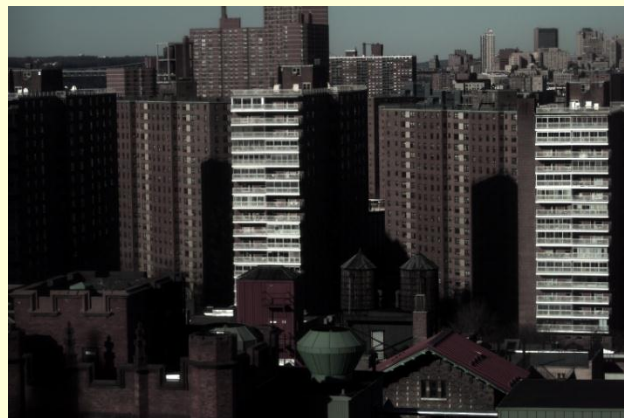
**February 18<sup>th</sup> 2002, 11 AM  
Clear and Sunny**



**February 18<sup>th</sup> 2002, 12 Noon  
Clear and Sunny**



**February 18<sup>th</sup> 2002, 2 PM  
Clear and Sunny**



**February 18<sup>th</sup> 2002, 3 PM  
Clear and Sunny**



**February 18<sup>th</sup> 2002, 4 PM  
Clear and Sunny**

# Illumination Spectra



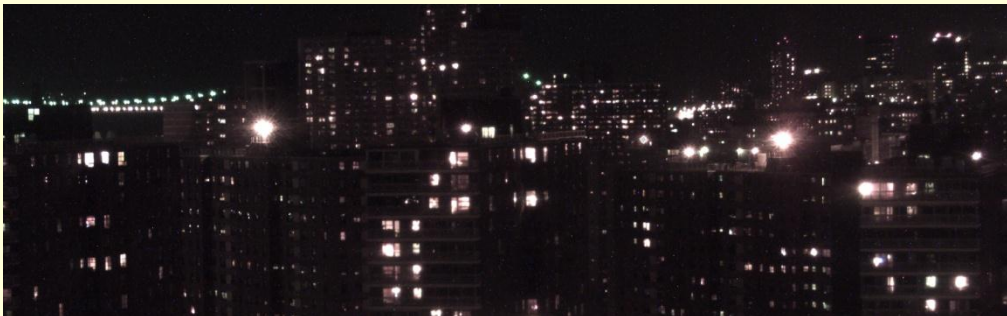
May 4<sup>th</sup> 2002, 6 AM  
Clear Day, **Sun Rise**



May 4<sup>th</sup> 2002, 12 Noon  
Clear Day, **Noon**



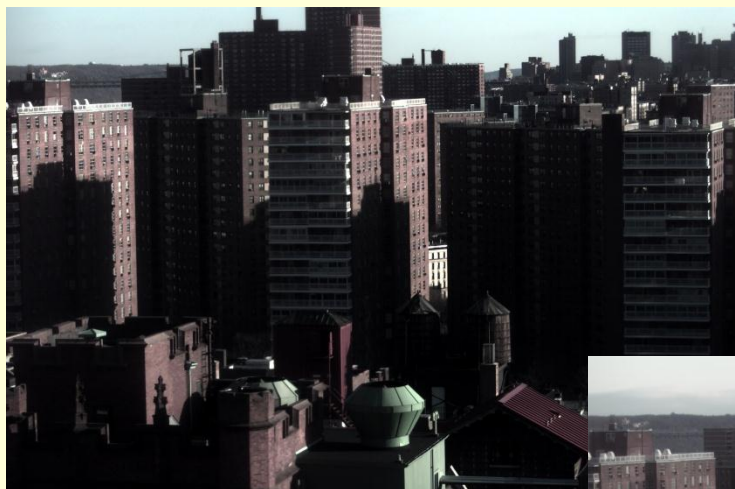
May 4<sup>th</sup> 2002, 6 PM  
Clear Day, **Sun Set**



May 4<sup>th</sup> 2002, 9 PM  
Clear **Night**



# Cloud Cover



March 22<sup>nd</sup> 2002, 7 AM  
Sunny, **No Clouds**



March 4<sup>th</sup> 2002, 7 AM  
Partly Sunny, **Partly Cloudy**



March 13<sup>th</sup> 2002, 7 AM  
**Overcast**

**Sharper Shadows**  
**Decreasing Cloud Cover**

# Weather Conditions



April 16<sup>th</sup> 2002, 3 PM  
Sunny, **Mild Haze**



April 12<sup>th</sup> 2002, 3 PM  
Overcast, **Light Rain**



April 19<sup>th</sup> 2002, 3 PM  
Overcast, **Dense Fog**



April 28<sup>th</sup> 2002, 3 PM  
Overcast, **Dense Mist**

# Visibility



April 28<sup>th</sup> 2002, 6 AM  
Rain & Mist, **Visibility 2.5 miles**  
0.1 inches Precipitation last hour



April 28<sup>th</sup> 2002, 9 AM  
Rain & Mist, **Visibility 1.5 miles**  
0.23 inches Precipitation last hour



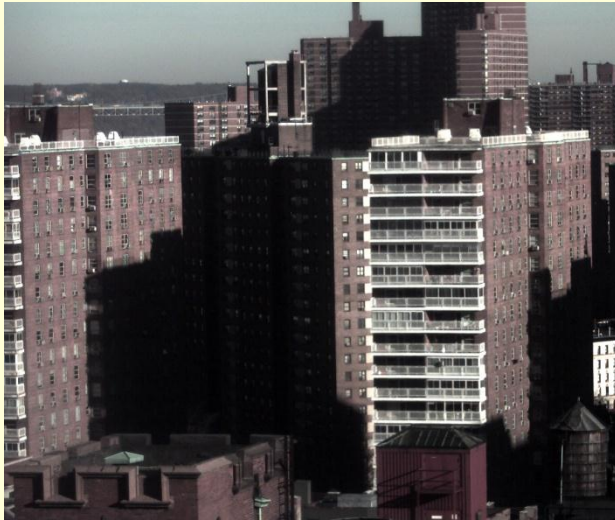
April 28<sup>th</sup> 2002, 12 Noon  
Light Rain & Mist, **Visibility 1.25 miles**  
0.08 inches Precipitation last hour



April 28<sup>th</sup> 2002, 3 PM  
Dense Mist, **Visibility 0.75 miles**  
0.02 inches Precipitation last hour



# Four Seasons ( New York )



**Winter**, January 4<sup>th</sup> 2002, 9 AM  
Clear and Sunny



**Fall**, September 9<sup>th</sup> 2001, 9 AM  
Clear and Sunny



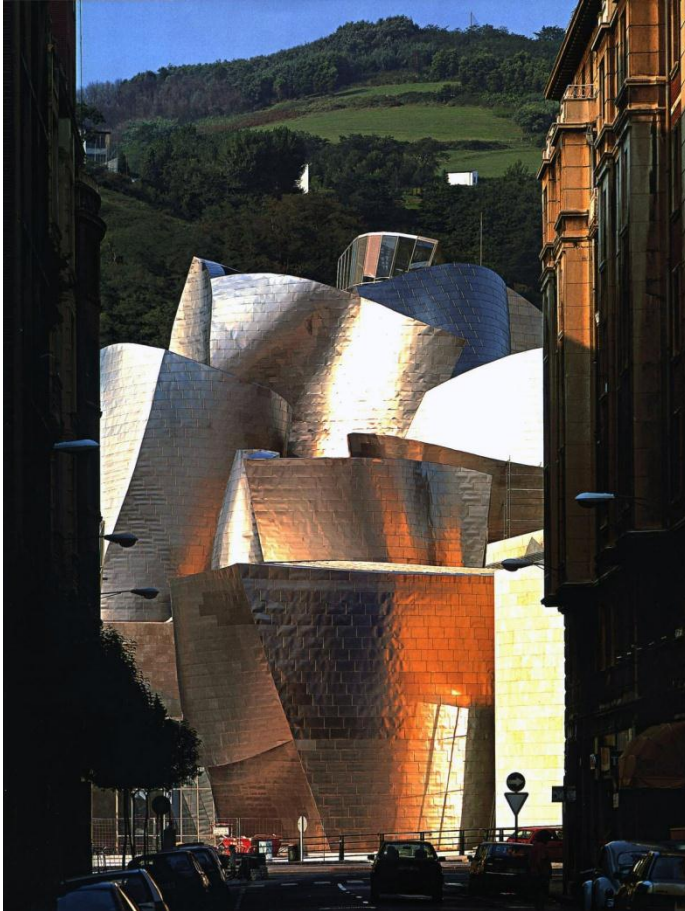
**Spring**, March 14<sup>th</sup> 2001, 9 AM  
Clear and Sunny



**Summer**, May 15<sup>th</sup> 2002, 9 AM  
Clear and Sunny

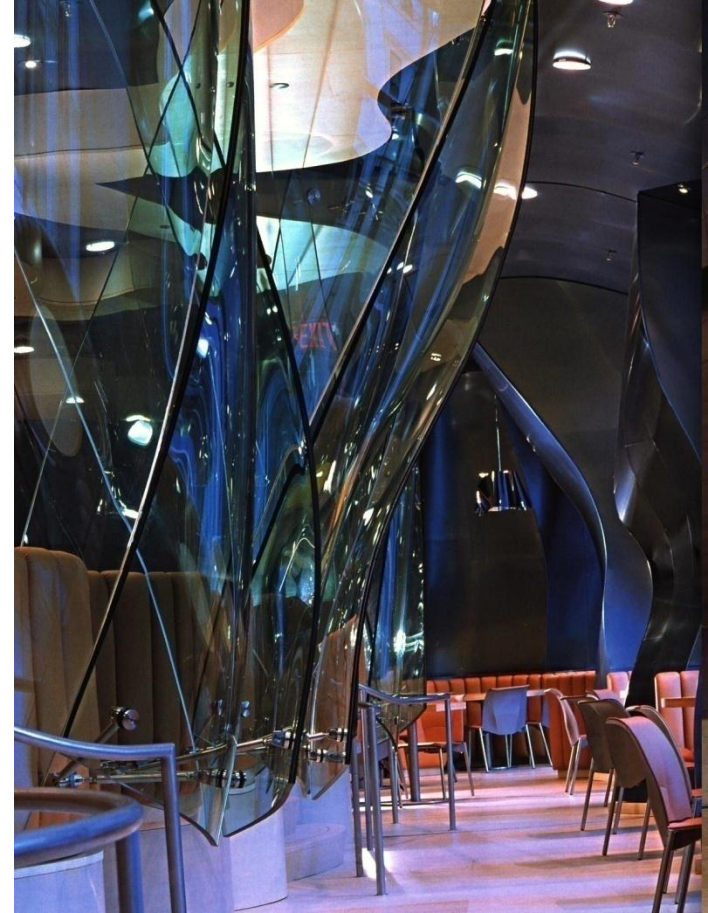


# Lighting Design



- From *Frank Gehry Architecture*, Ragheb ed. 2001

# Lighting Design



- From *Frank Gehry Architecture*, Ragheb ed. 2001

# Nomenclature for Lighting

Size: point  
line  
area  
volume

Distance: infinity  
near-field

Directionality: collimated  
divergent  
convergent

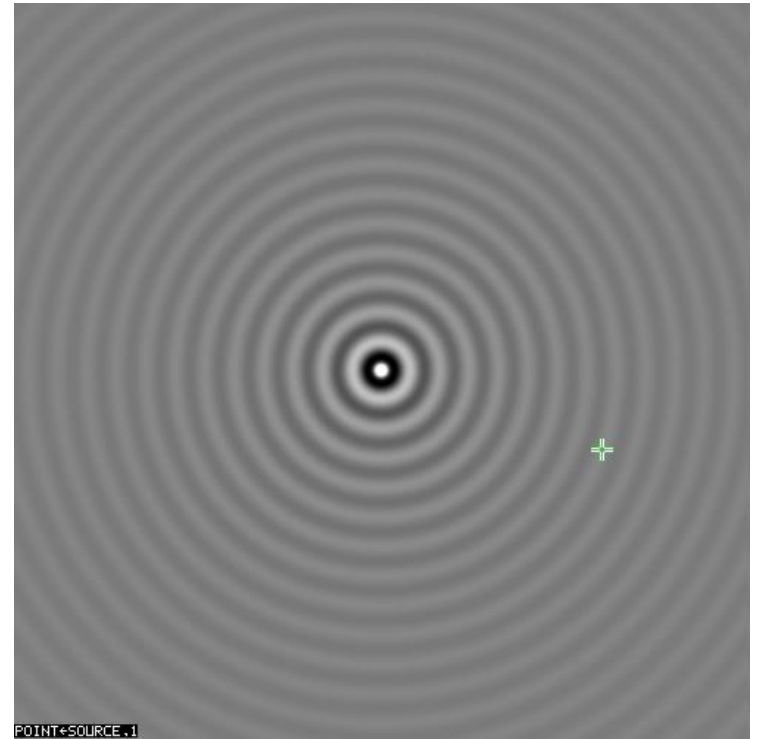
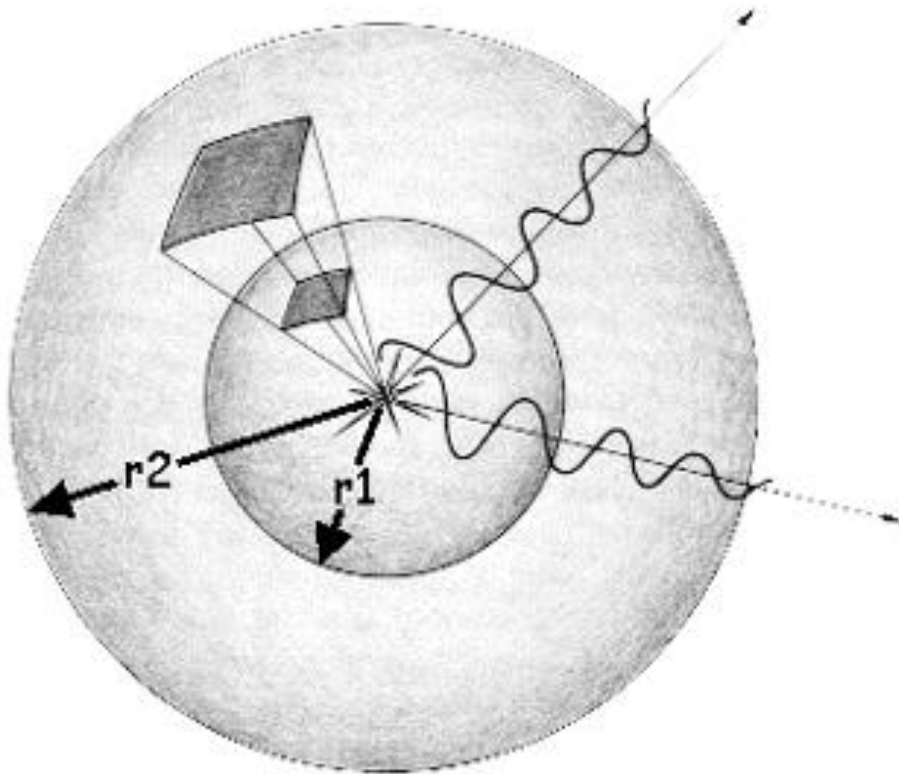
Temporal: static  
time-varying

Natural sun  
sky  
firefly  
moon

Artificial halogen  
fluorescent  
flash  
projector  
laser



# Isotropic Point Light Source

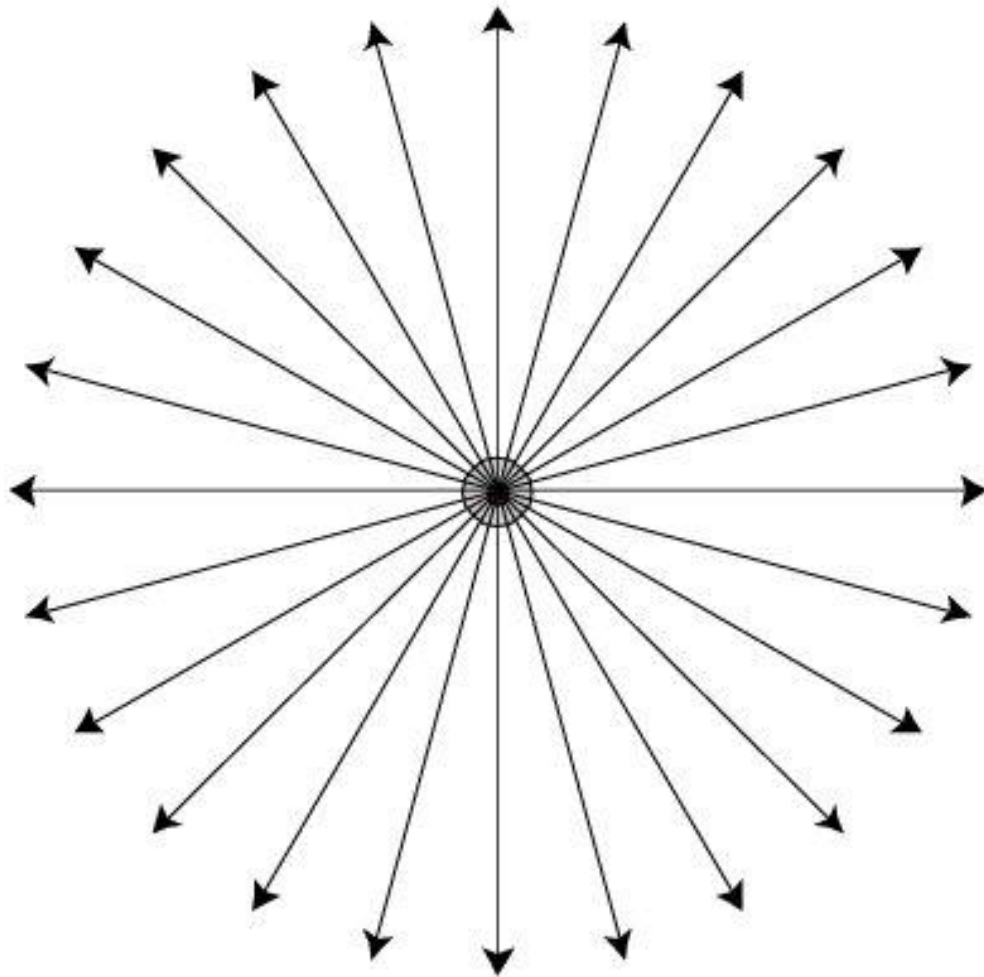


We see an inverse distance squared fall off in intensity.  
Here light does not weaken, but only spreads in a sphere.



# Isotropic Point Source

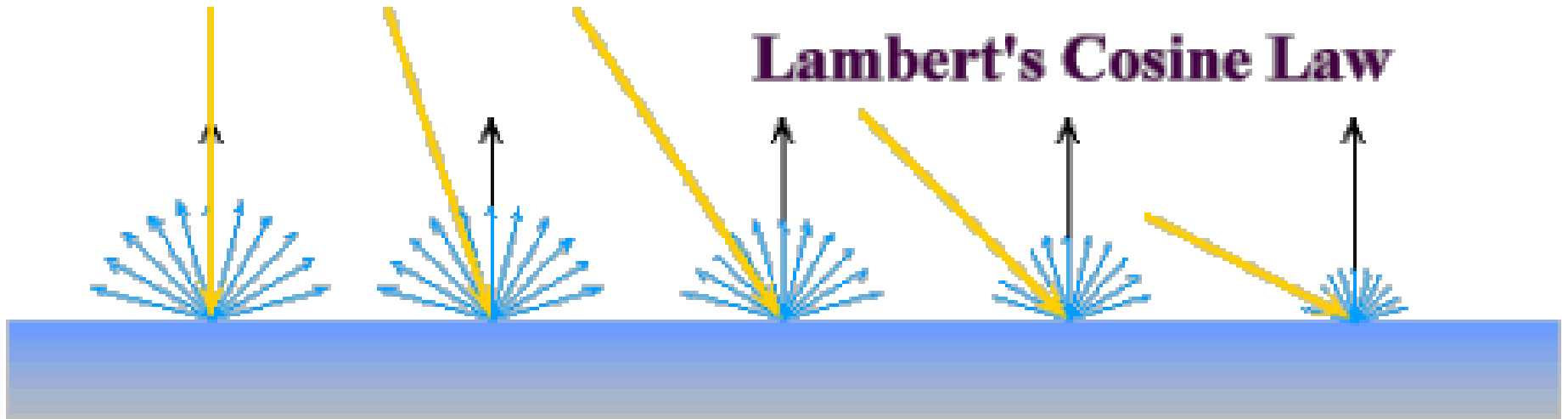
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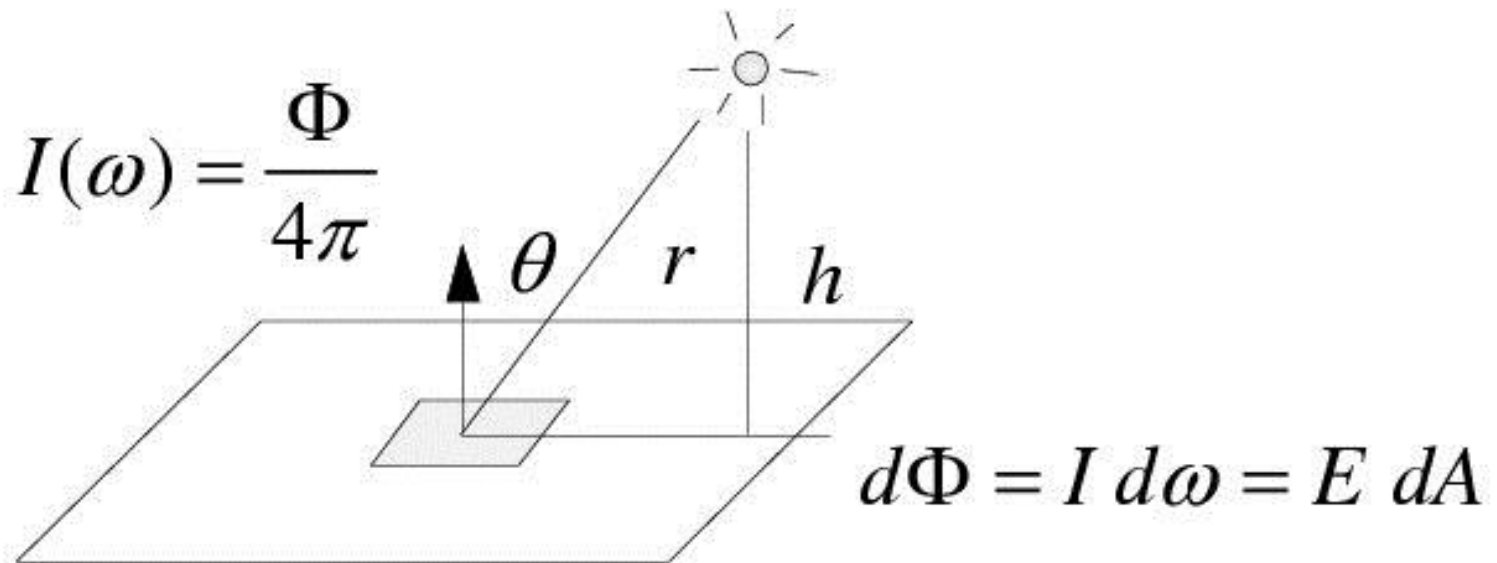
$$\begin{aligned}\Phi &= \int_{s^2} I d\omega \\ &= 4\pi I\end{aligned}$$

$$I = \frac{\Phi}{4\pi}$$

How much light falls on a surface?



# Illumination: Isotropic Point Source

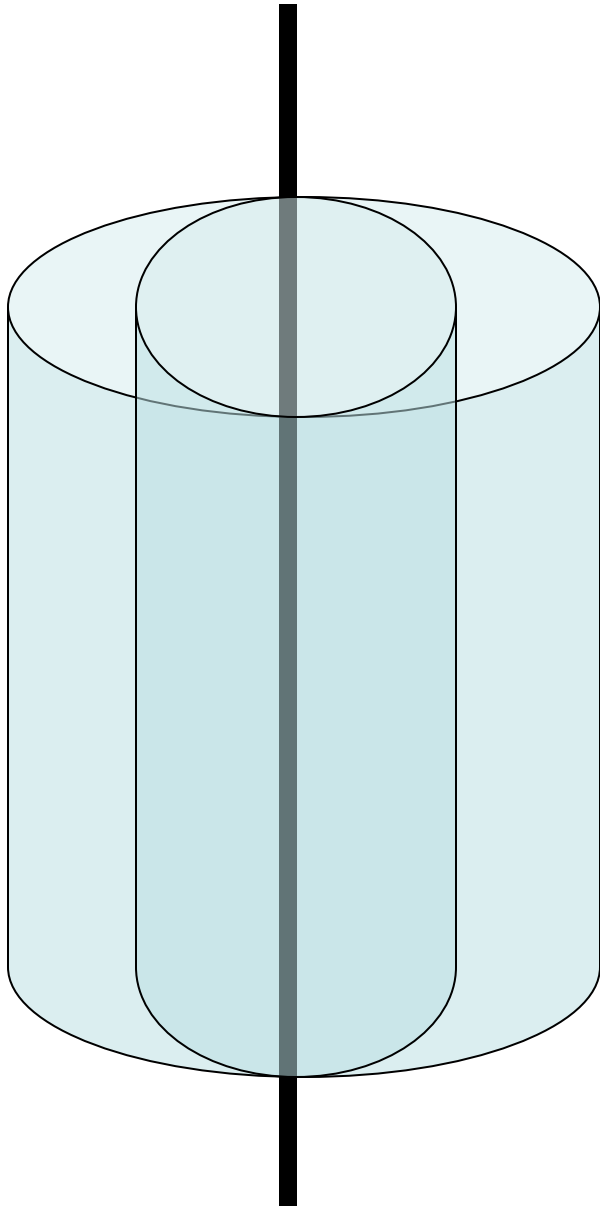


$$I d\omega = \frac{\Phi \cos \theta}{4\pi r^2} dA = E dA$$

$$E = \frac{\Phi \cos \theta}{4\pi r^2}$$

$$\frac{\Phi \cos \theta}{4\pi r^2} \Rightarrow \frac{\Phi \cos^3 \theta}{4\pi h^2}$$

# Infinite Line Source



Line source shows cylindrical symmetry.

The intensity fall-off is inversely proportional to distance from the line source. Why?

$$d\Phi = I d\omega = E dA$$



# Infinite Planar Area Source

- Assume every point on the plane is an isotropic point light source.
- We saw inverse squared fall off, inverse fall off...so, this must be...
- Intensity CONSTANT with respect to distance! WHY?

As distance increases,

$$d\Phi = I d\omega = E dA$$

Intensity from one point source decreases

But we add intensities from all point sources on the plane.

# Distant and Collimated Lighting

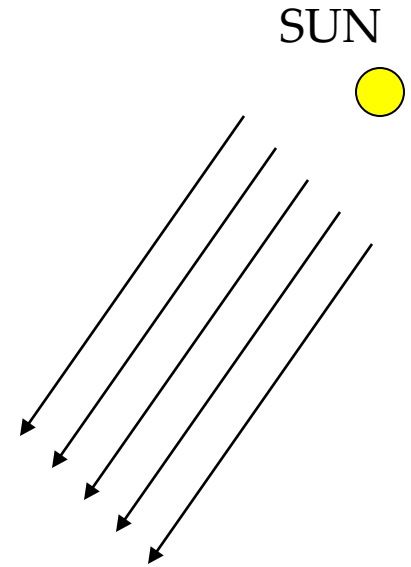
## Distant Lighting:

Essentially source at infinity

All surface points receive light from the same direction

Intensity fall must not be ignored!

Most vision and graphics algorithms assume this.

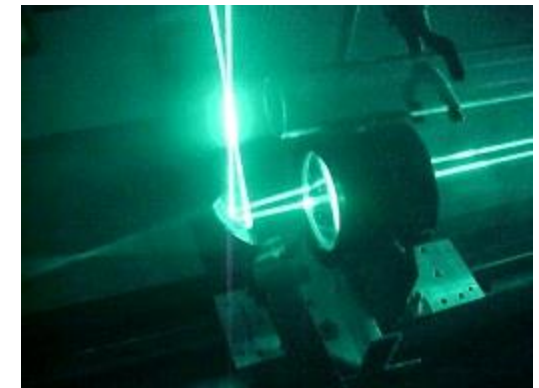


## Collimated:

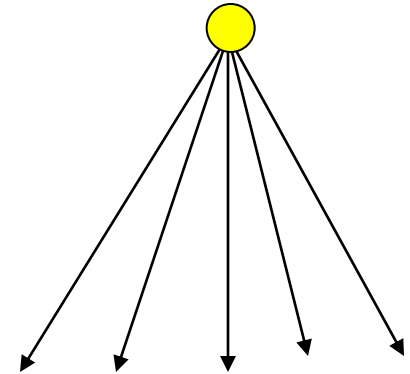
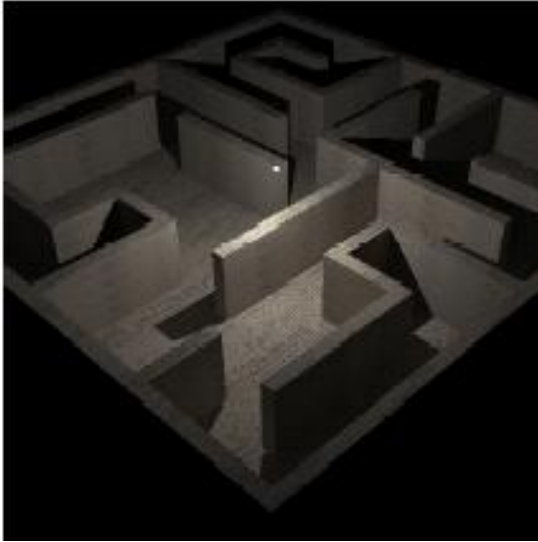
Parallel rays of light on the surface

Lasers (no fall off) - need not be at infinity

Lighting at infinity - (inverse squared fall off)



# Divergent and Near-field Lighting



- Every scene point can receive light from a different direction.
- Much harder to model.
- Examples: near by point sources, spot lights
- Assume distant lighting when size of scene is 10% of the distance to the source.

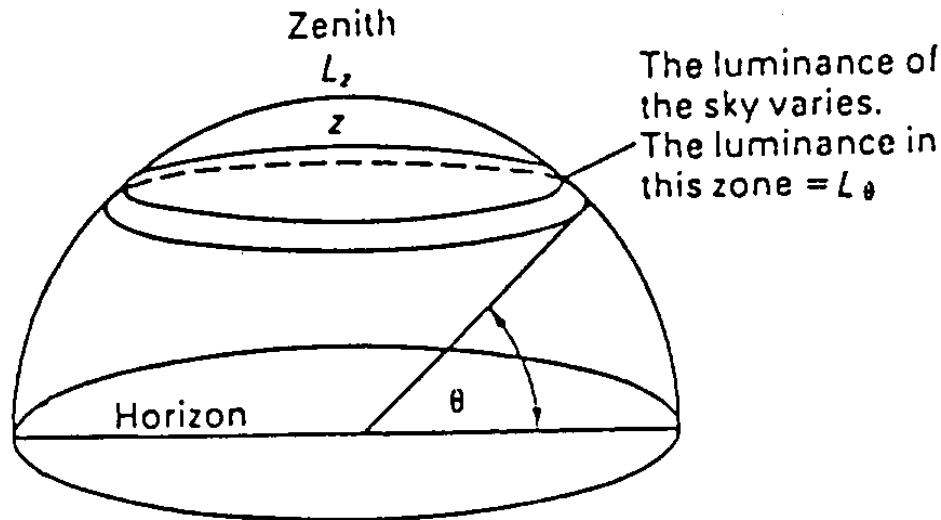
# Overcast Sky versus Clear Sky

Which is the brightest region in a overcast sky?

Which is the darkest?

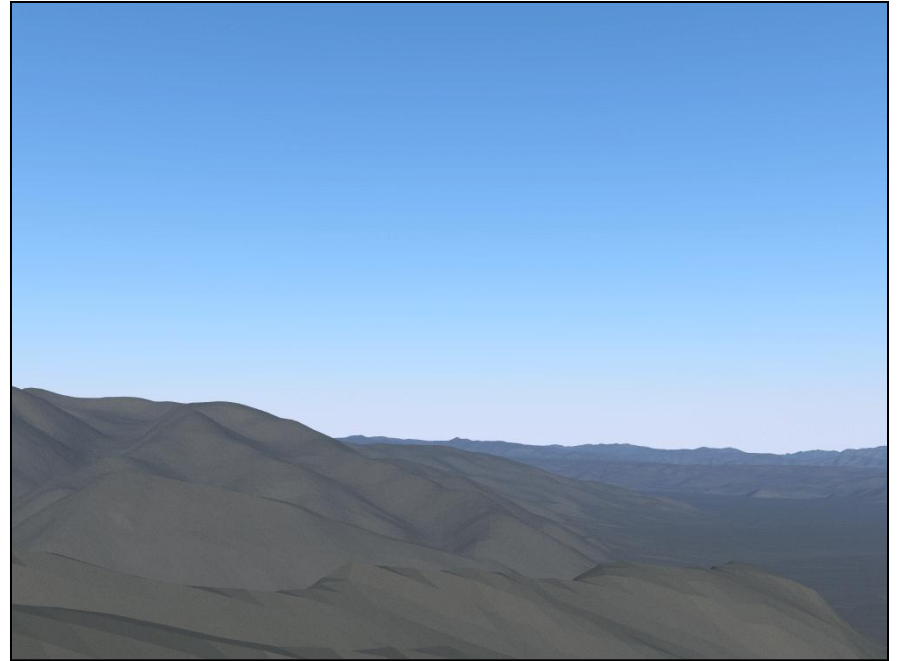
Which is the brightest region in a sunny sky (apart from the sun)?

Which is the darkest?





# Overcast Sky versus Clear Sky



Notice reversal of brightness in the two skies.

# Fluorescent versus Incandescent Lighting

## Fluorescent:

Less heat generated.

More efficient lighting for the same brightness.

Flickers continuously.

Shows sparse, spikes in spectrum.

## Incandescent:

Lots of heat generated.

Less efficient lighting for the same brightness.

No flickers.

Shows continuous spectrum.

# Is there a unified representation for light sources?



How do we compare the light from a street lamp to that from an overcast sky?

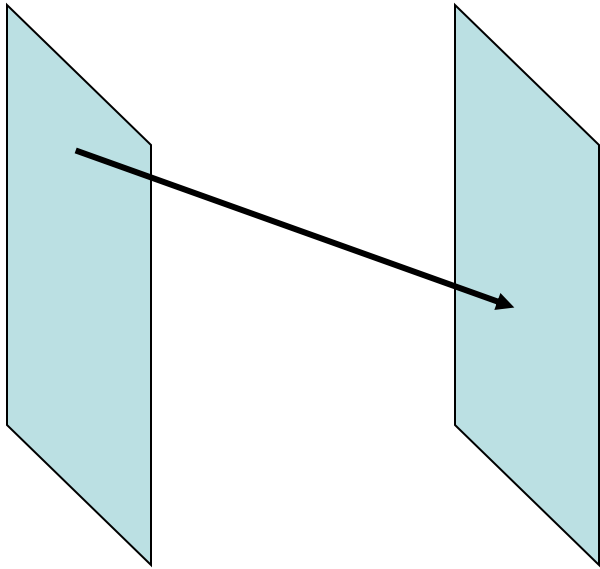
It is important to unify source representation so that algorithms may be developed for all sources instead of one per type of source.

Consider the SPACE of LIGHT RAYS!

# 4D Hypercube of Rays

(x,y)-plane

(p,q)-plane



- Assumes vacuum (no absorption or scattering)
- No fluorescence, phosphorescence

$$\mathcal{M}_{src} \equiv \left\{ (x, y, p, q) : x \in \left[-\frac{h_x}{2}, \frac{h_x}{2}\right], \right. \\ \left. y \in \left[-\frac{h_y}{2}, \frac{h_y}{2}\right], p \in \left[-\frac{h_p}{2}, \frac{h_p}{2}\right], q \in \left[-\frac{h_q}{2}, \frac{h_q}{2}\right] \right\}.$$

# Representation of Sources

Langer and Zucker, CVPR 97

$(x,y)$ -plane

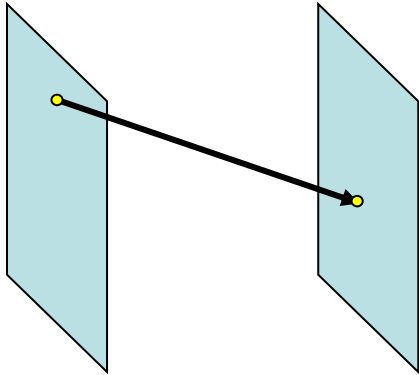
$(p,q)$ -plane

$(x,y)$ -plane

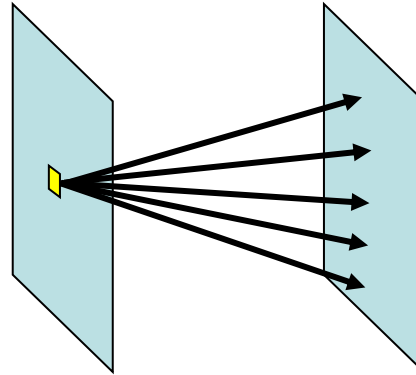
$(p,q)$ -plane

$(x,y)$ -plane

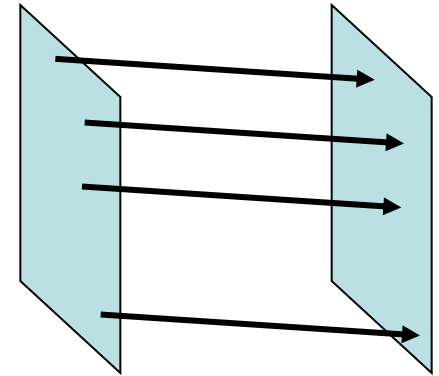
$(p,q)$ -plane



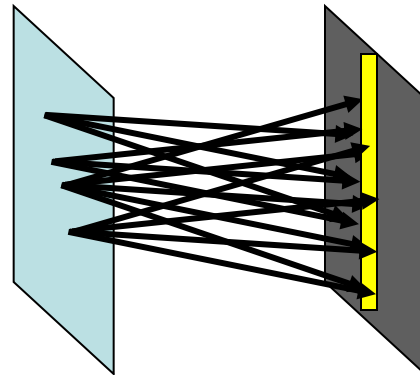
Laser beam – 0D



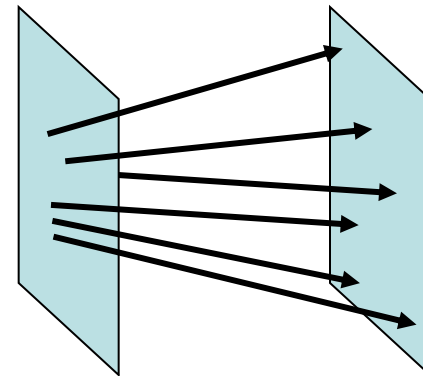
Point source – 2D



Distant Source (Sun) – 2D



Area source (Sky) with a crack in the door – 3D

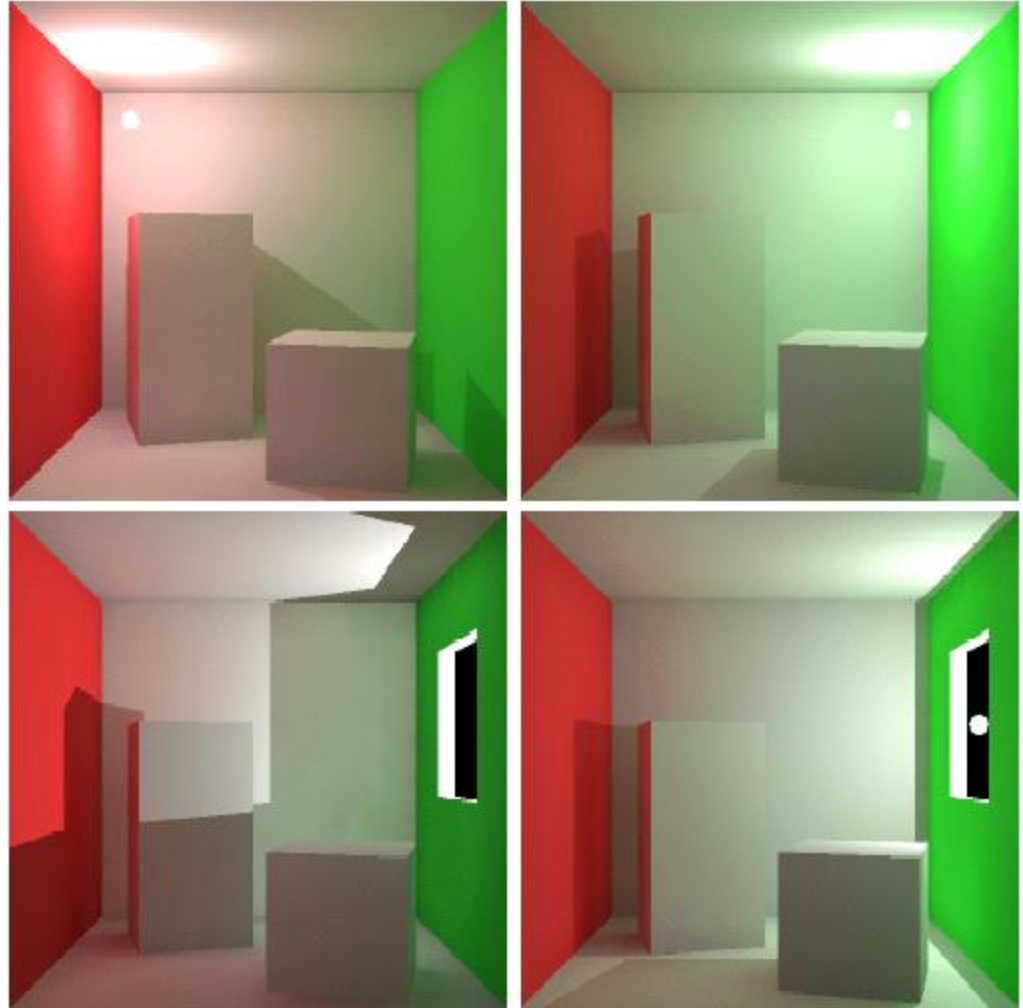
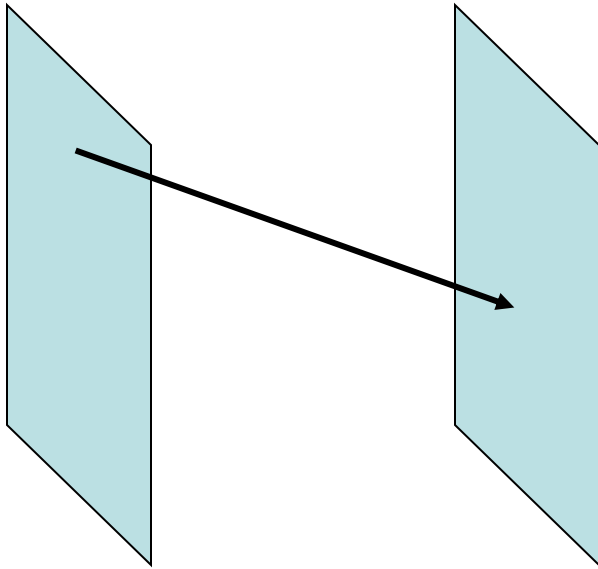


Area source (Sky) with door completely open – 4D

# Examples of sources

$(x,y)$ -plane

$(p,q)$ -plane





# What is a Light Source?

Is sky a source? If so, why not a white piece of paper?

Is a translucent object a source?

How to differentiate between source rays and non-source rays?

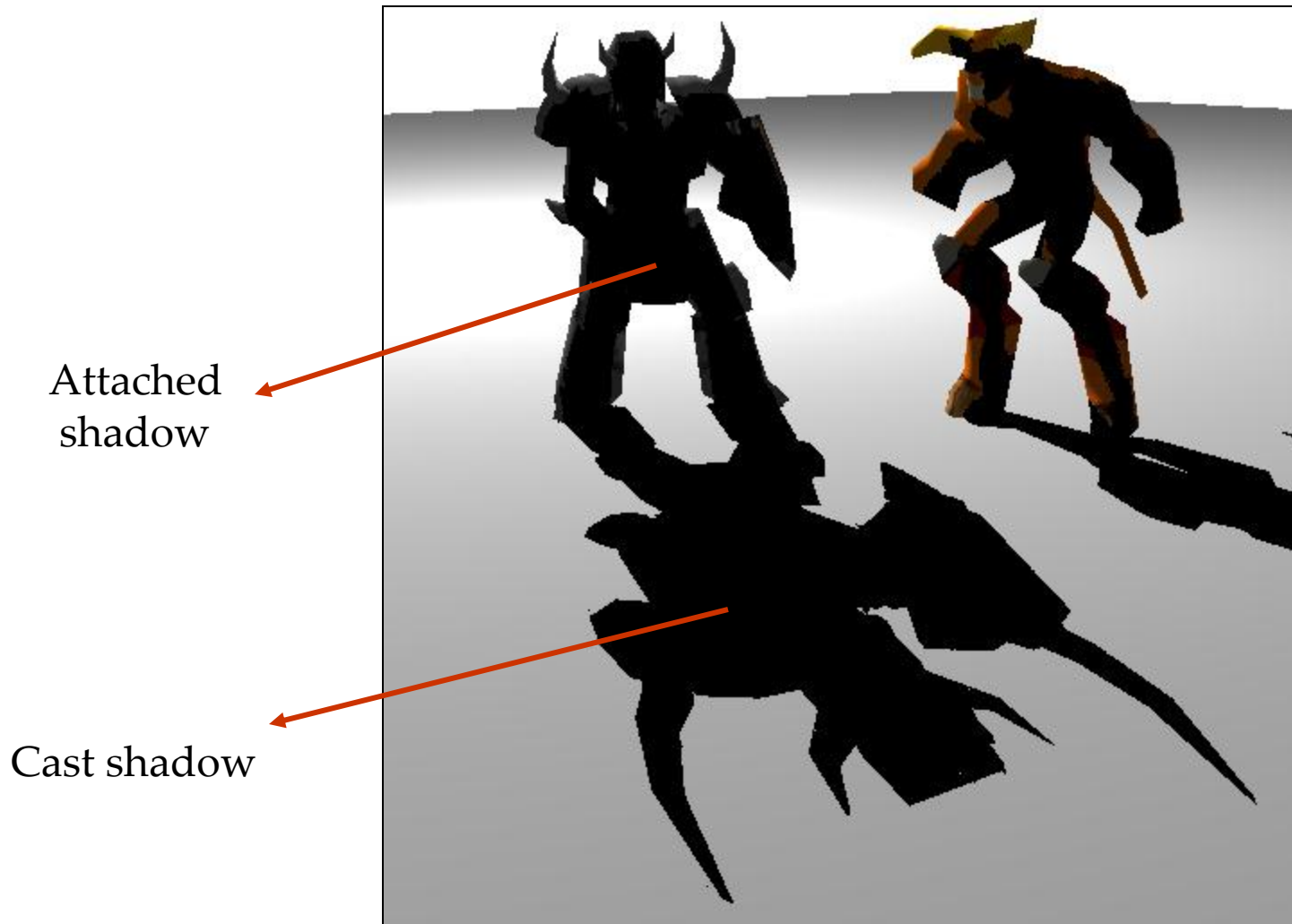
Define a minimum set of absorbants at the ends of rays so that the whole ray space is dark.

Shadows

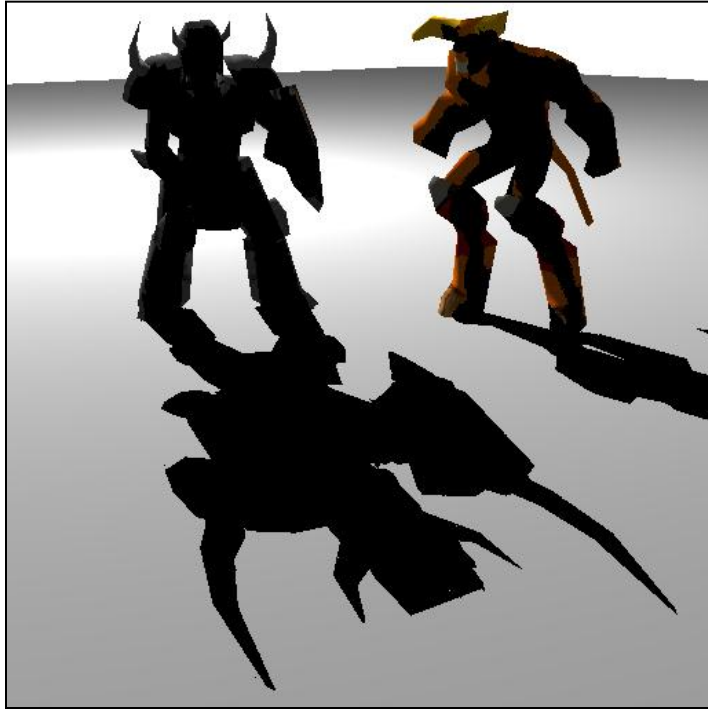




# Attached and Cast Shadows







*Sen, Cammarano, Hanrahan, 2003*

Very hard shadows

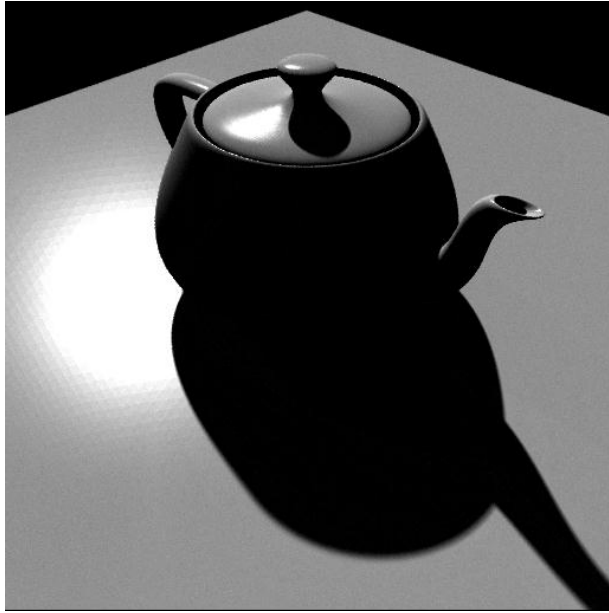


*Sloan, Kautz, Snyder 2002*

Very soft shadows



# All-Frequency Lighting and Shadows



**Teapot in Grace Cathedral**

# Sharper and Softer parts of Shadows



Point source model not good for rendering scenes.

