Spatial Data Structures

Hierarchical Bounding Volumes Grids Octrees BSP Trees



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*n*² computations

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*n*² computations

Spatial data-structures

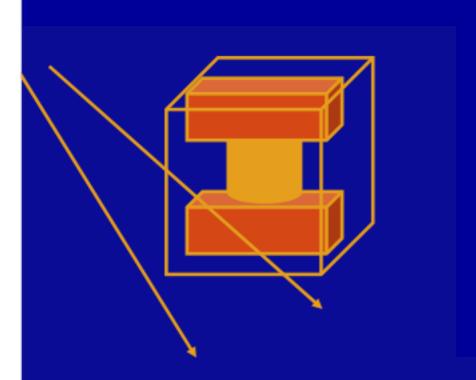


Spatial Data Structures

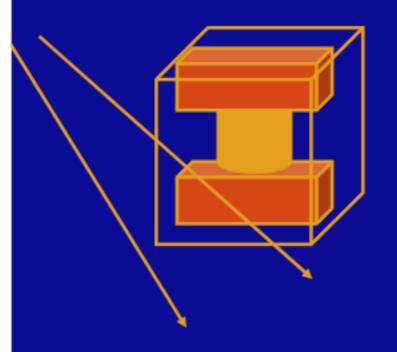
- We'll look at
 - Hierarchical bounding volumes
 - Grids
 - Octrees
 - K-d trees and BSP trees
- Good data structures can give speed up ray tracing by 10x or 100x

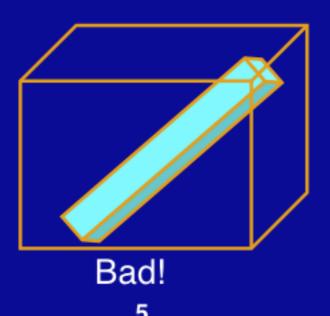
- Wrap things that are hard to check for intersection in things that are easy to check
 - Example: wrap a complicated polygonal mesh in a box
 - Ray can't hit the real object unless it hits the box
 - Adds some overhead, but generally pays for itself.

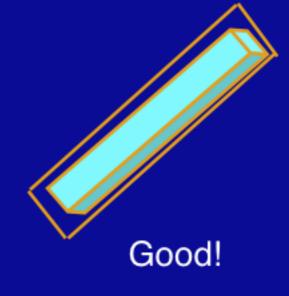
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 - box can be axis-aligned or not



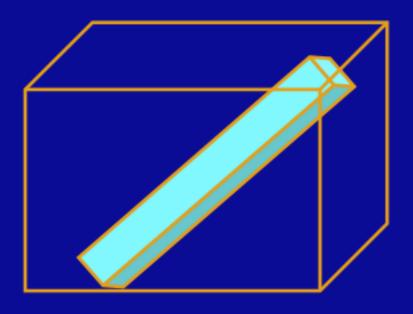
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- But you don't want expensive intersection tests!

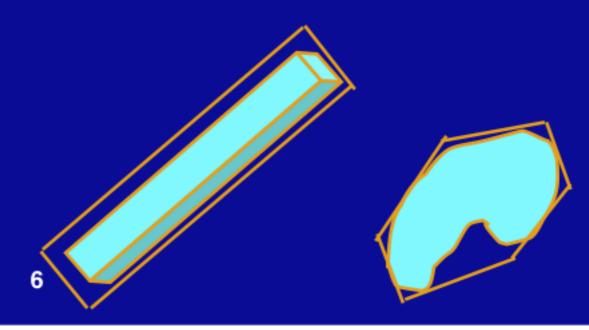






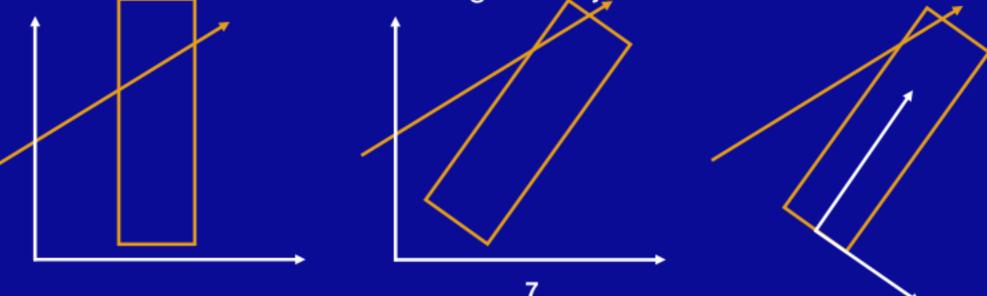
- You want a snug fit!
- But you don't want expensive intersection tests!
- Use the ratio of the object volume to the enclosed volume as a measure of fit.
- Cost = n*B + m*I
 - n is the number of rays tested against the bounding volume
 - B is the cost of each test (Do not need to compute exact intersection!)
 - m is the number of rays which actually hit the bounding volume
 - I is the cost of intersecting the object within



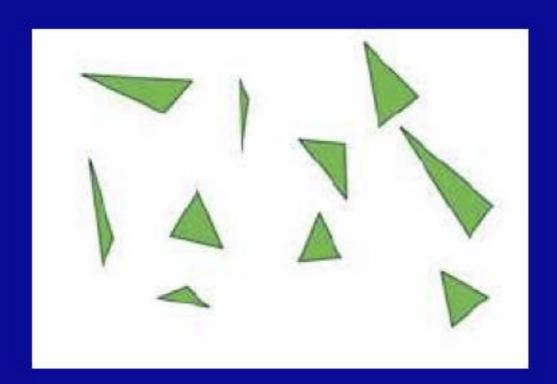


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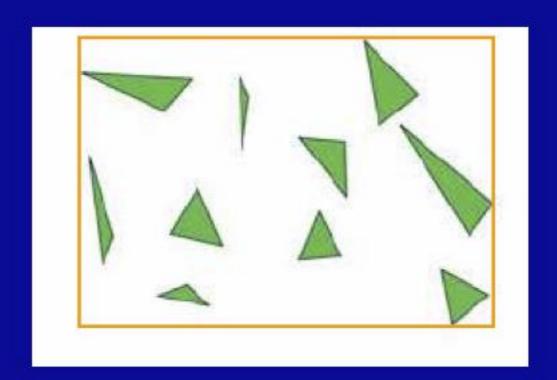
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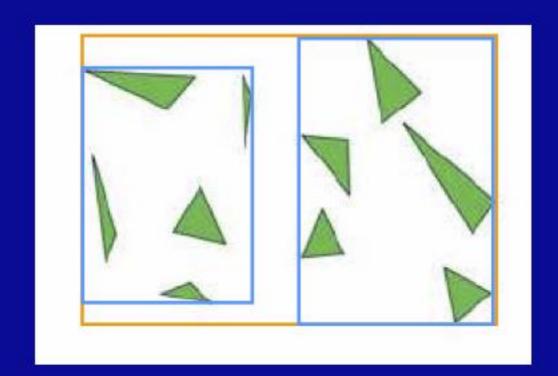
- Still need to check ray against every object --- O(n)
- Use tree data structure
 - Larger bounding volumes contain smaller ones

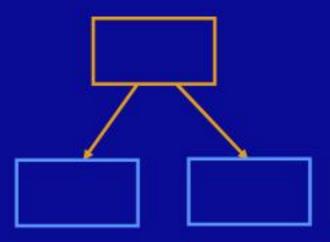


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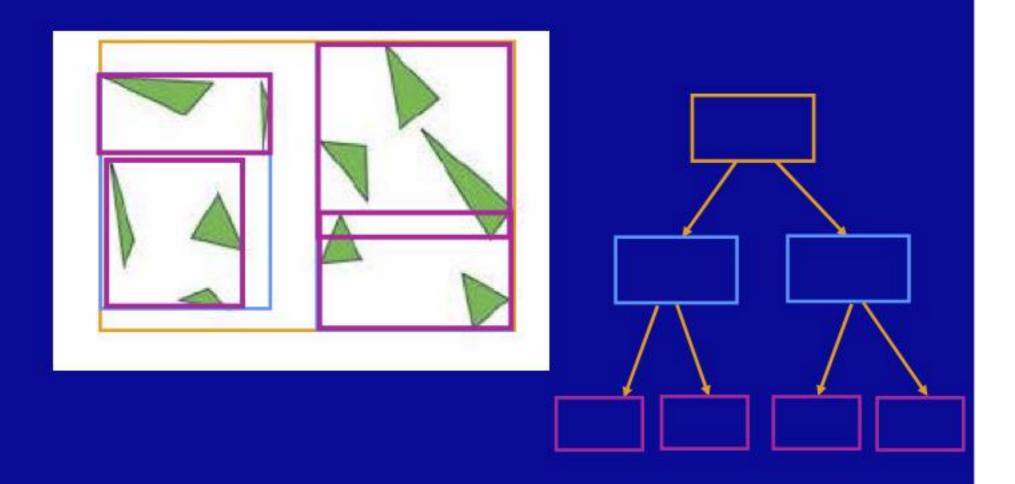


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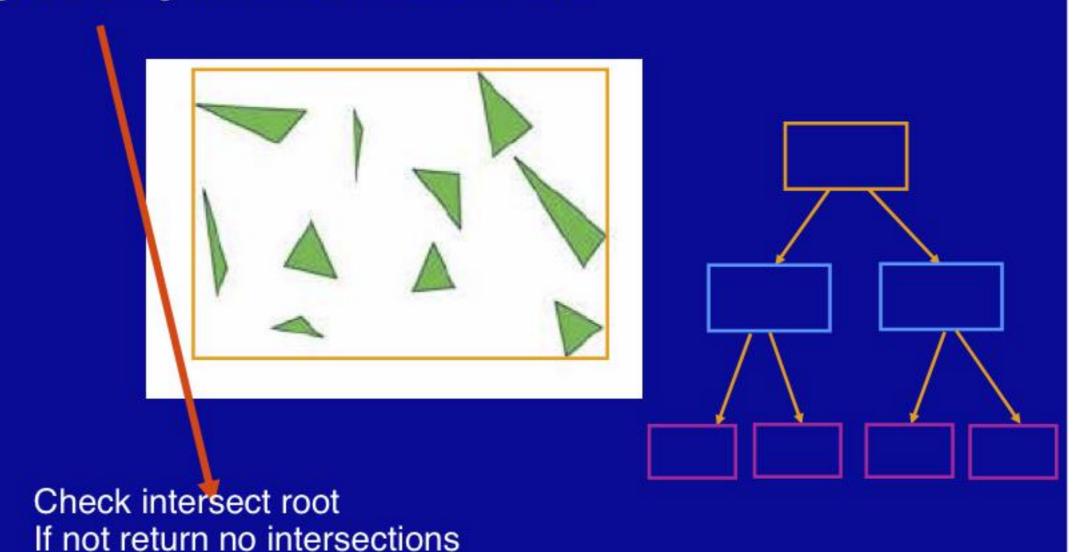




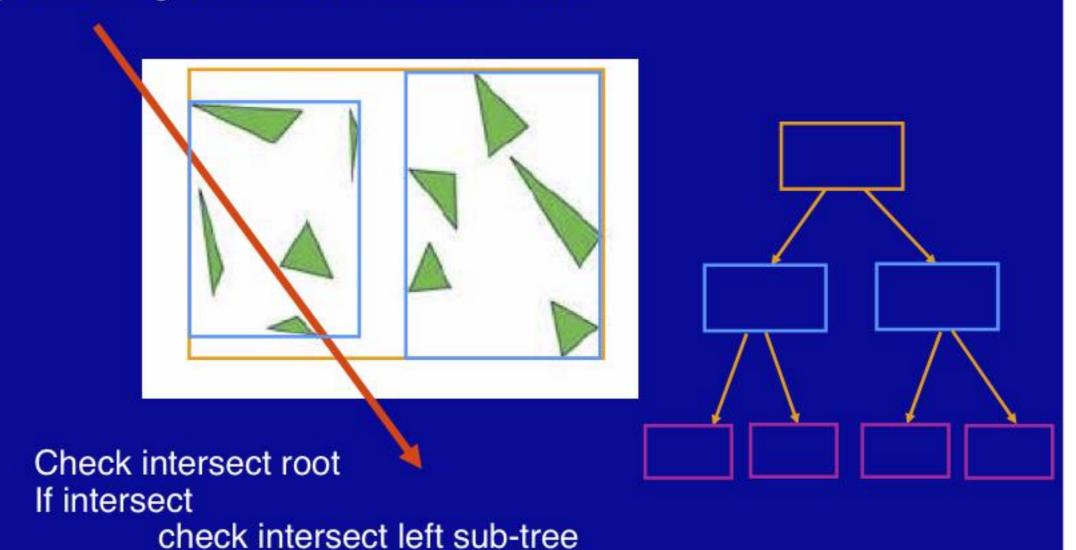
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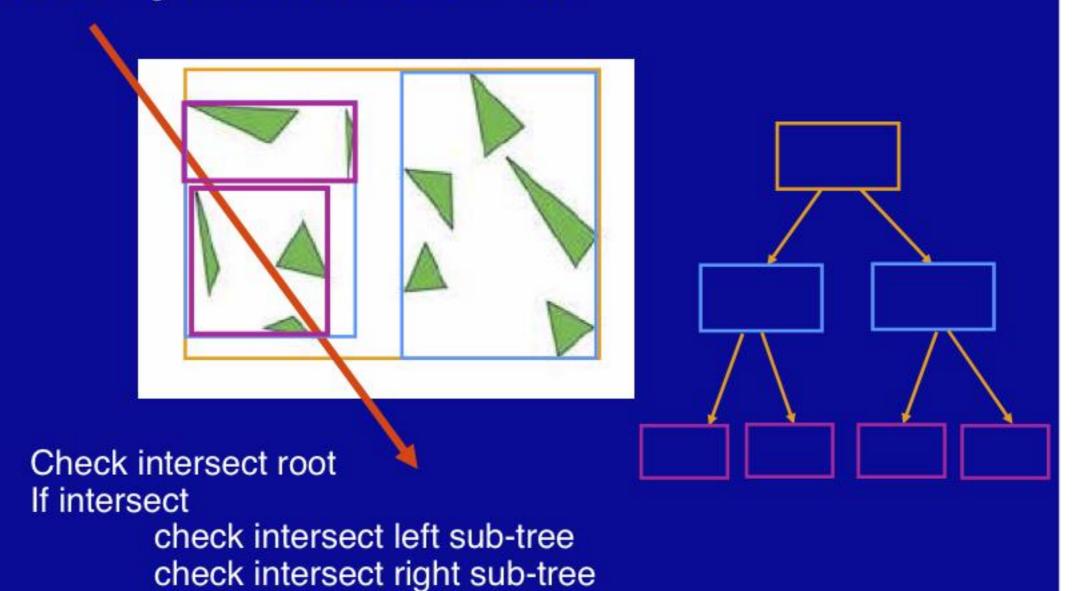


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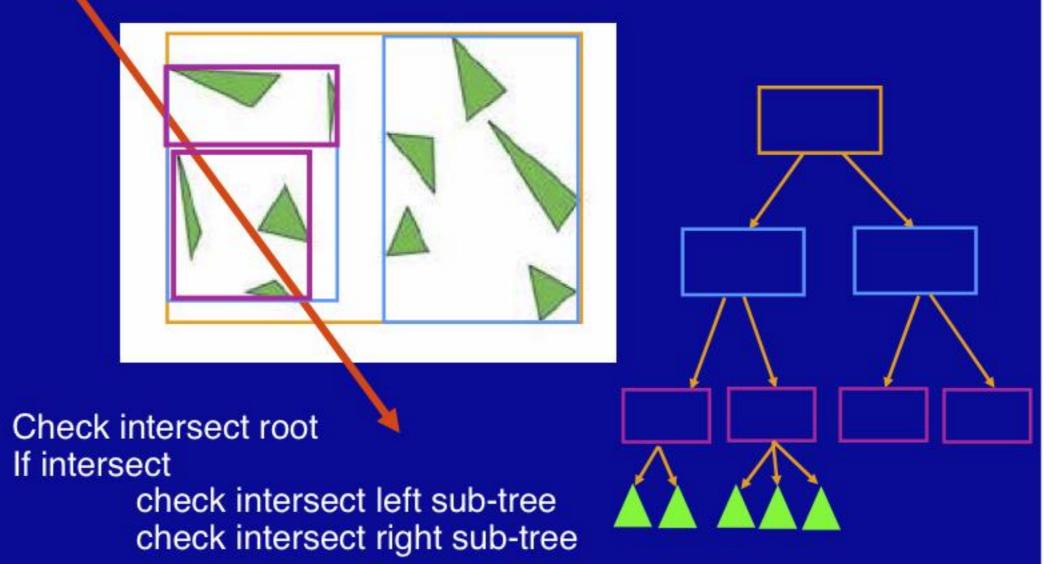


check intersect right sub-tree

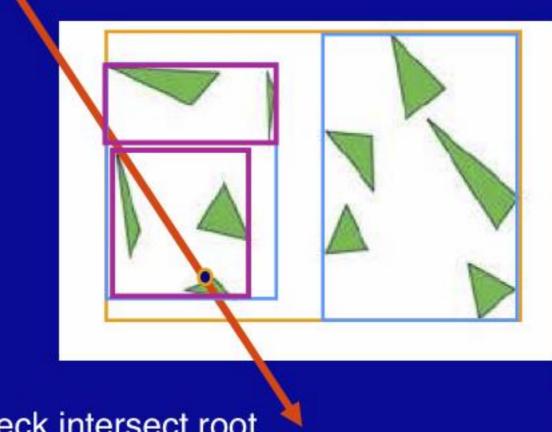
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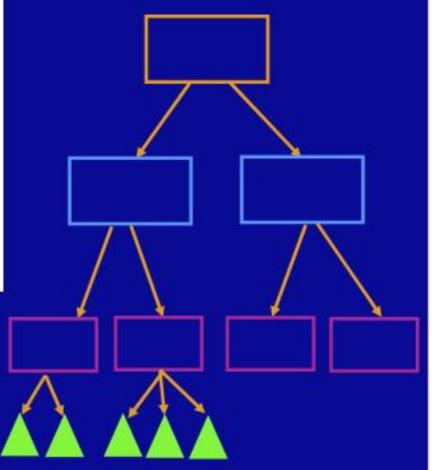


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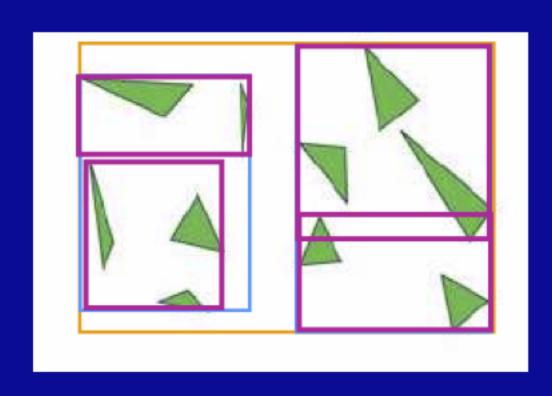


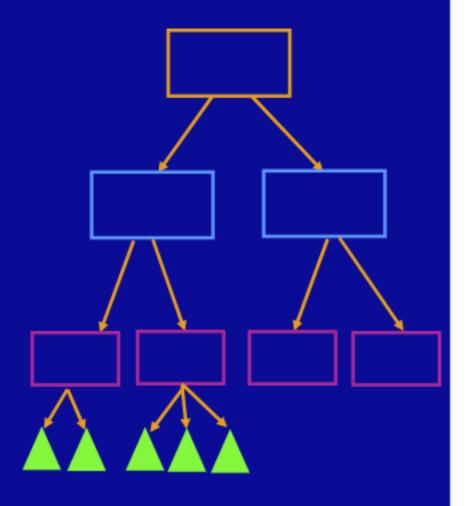
Check intersect root If intersect

check intersect left sub-tree check intersect right sub-tree

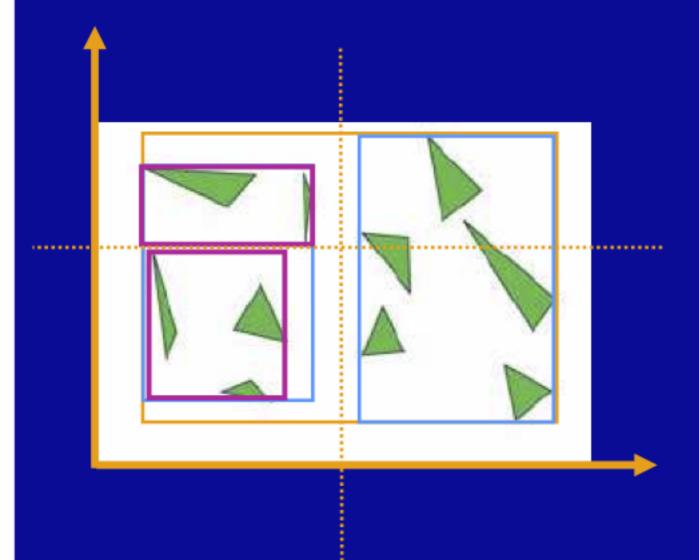


- Many ways to build a tree for the hierarchy
- Works well:
 - Binary
 - Roughly balanced
 - Boxes of sibling trees not overlap too much

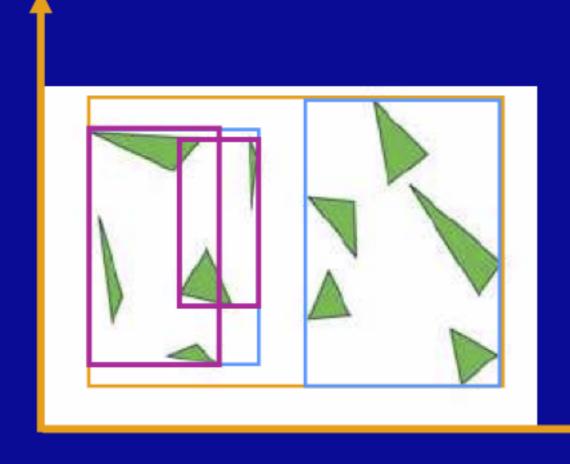




- Sort the surfaces along the axis before dividing into two boxes
- Carefully choose axis each time
- Choose axis that minimizes sum of volumes



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- Works well if you use good (appropriate) bounding volumes and hierarchy
- Should give O(log n) rather than O(n) complexity (n=# of objects)
- Can have multiple classes of bounding volumes and pick the best for each enclosed object

Hierarchical bounding volumes Spatial Subdivision

- Grids
- Octrees
- K-d trees and BSP trees

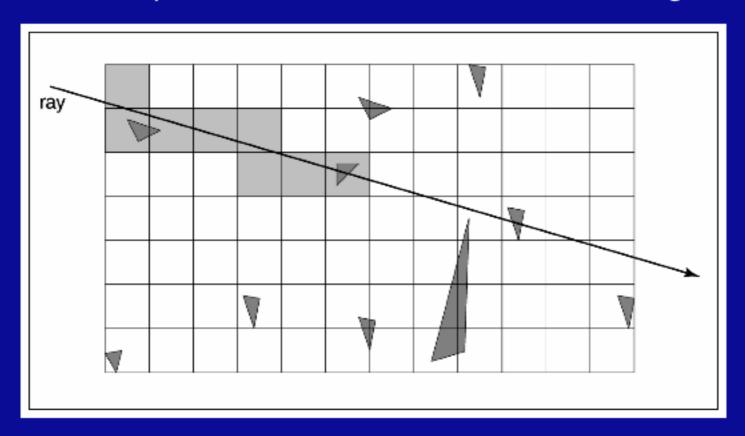
3D Spatial Subdivision

 Bounding volumes enclose the objects (objectcentric)

- Instead could divide up the space—the further an object is from the ray the less time we want to spend checking it
 - Grids
 - Octrees
 - K-d trees and BSP trees

Grids

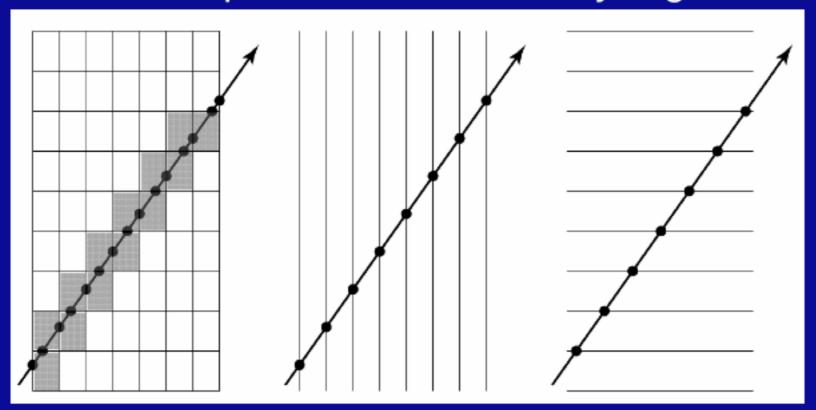
- Data structure: a 3-D array of cells (voxels) that tile space
 - Each cell points to list of all surfaces intersecting that cell



- Intersection testing:
 - Start tracing at cell where ray begins
 - Step from cell to cell, searching for the first intersection point
 - At each cell, test for intersection with all surfaces pointed to by that cell
 - If there is an intersection, return the closest one

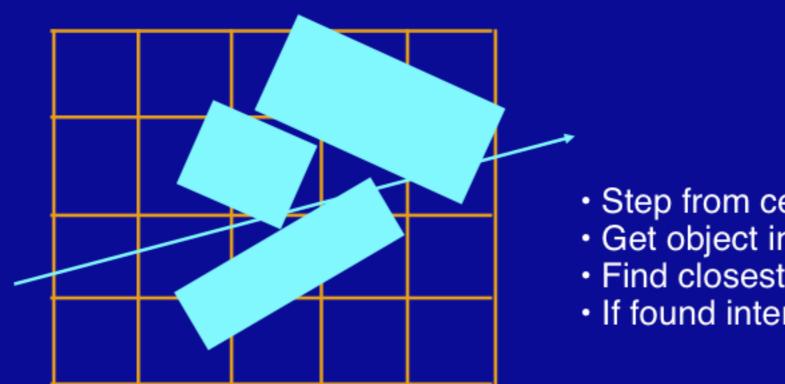
Grids

- Cells are traversed in an incremental fashion
- Hits of sets of parallel lines are very regular



More on Grids

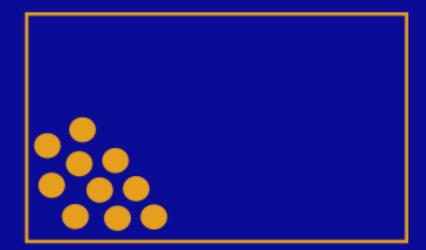
- Be Careful! The fact that a ray passes through a cell and hits an object doesn't mean the ray hit that object in that cell
- Optimization: cache intersection point and ray id in "mailbox" associated with each object



- Step from cell to cell
- Get object intersecting cell
- Find closest intersection
- If found intersection --- done

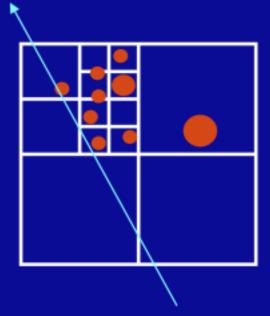
More on Grids

- Grids are a poor choice when the world is nonhomogeneous (clumpy)
 - many polygons clustered in a small space
- How many cells to use?
 - too few ⇒ many objects per cell ⇒ slow
 - too many \Rightarrow many empty cells to step through \Rightarrow slow
- Non-uniform spatial subdivision is better!



Octrees

- Quadtree is the 2-D generalization of binary tree
 - node (cell) is a square
 - recursively split into four equal sub-squares
 - stop when leaves get "simple enough"

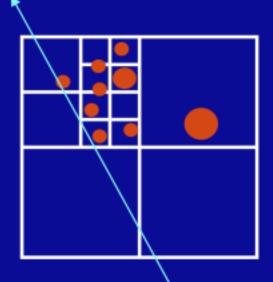


Octrees

- Quadtree is the 2-D generalization of binary tree
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 - stop when leaves get "simple enough"



- node (cell) is a cube, recursively split into eight equal sub-cubes
- for ray tracing:
 - stop subdivision based on number of objects
 - internal nodes store pointers to children, leaves store list of surfaces
- more expensive to traverse than a grid
- but an octree adapts to non-homogeneous scenes better



Which Data Structure is Best for Ray Tracing?

Grids

Easy to implement

Require a lot of memory

Poor results for inhomogeneous scenes

Octrees

Better on most scenes (more adaptive)

Spatial subdivision expensive for animations

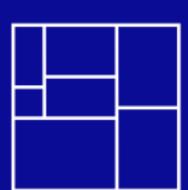
Hierarchical bounding volumes

Better for dynamic scenes

Natural for hierarchical objects

k-d Trees and BSP Trees

- Relax the rules for quadtrees and octrees:
- k-dimensional (k-d) tree
 - don't always split at midpoint
 - split only one dimension at a time (i.e. x or y or z)

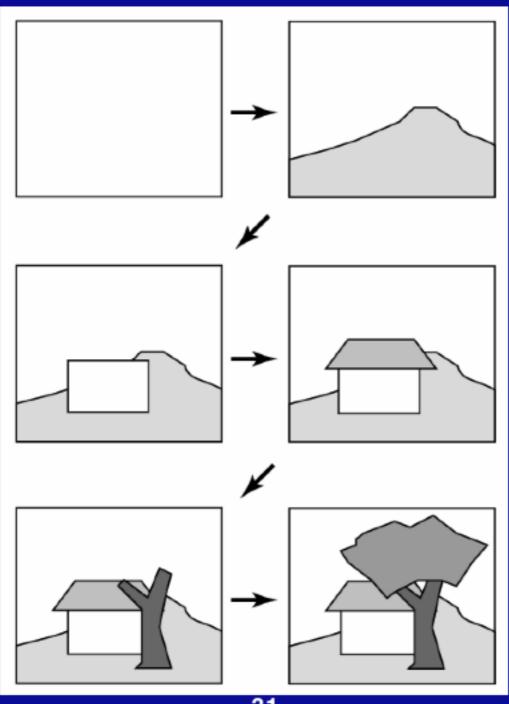


- binary space partitioning (BSP) tree
 - permit splits with any line
 - In 2-D space split with lines (most of our examples)
 - 3-D space split with planes
 - K-D space split with k-1 dimensional hyperplanes
- useful for Painter's algorithm (hidden surface removal)



Painters Algorithm

Hidden Surface Elimination

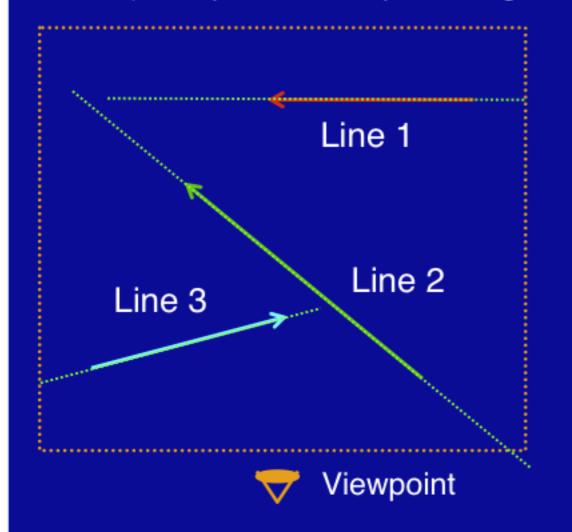


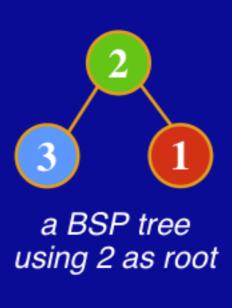
Painters Algorithm

- Need to sort objects back to front
- Order depends on the view point
- Partition objects using BSP tree
- View independent

Building a BSP Tree

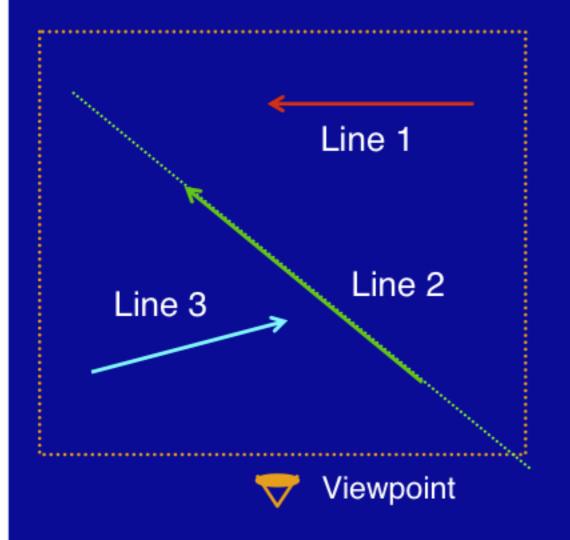
- Let's look at simple example with 3 line segments
- Arrowheads are to show left and right sides of lines.
- Using line 1 or 2 as root is easy.
- (examples from http://www.geocities.com/SiliconValley/2151/bsp.html)

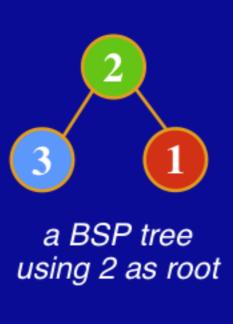




Drawing Objects

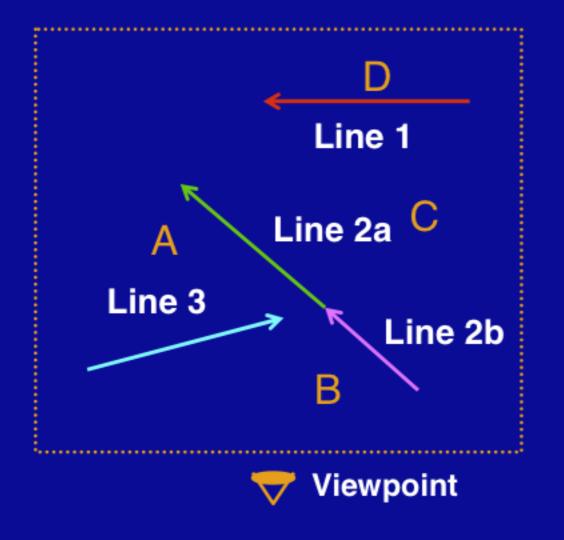
- Traverse the tree from the root
- If view point is on the left of the line --- traverse right sub-tree first
- Draw the root
- Traverse left sub-tree

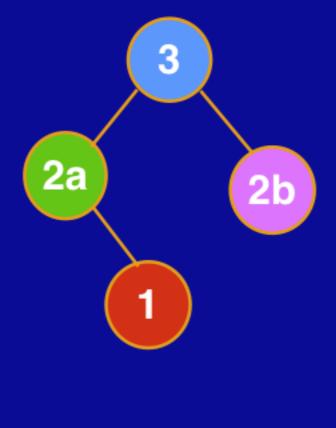




Building the Tree 2

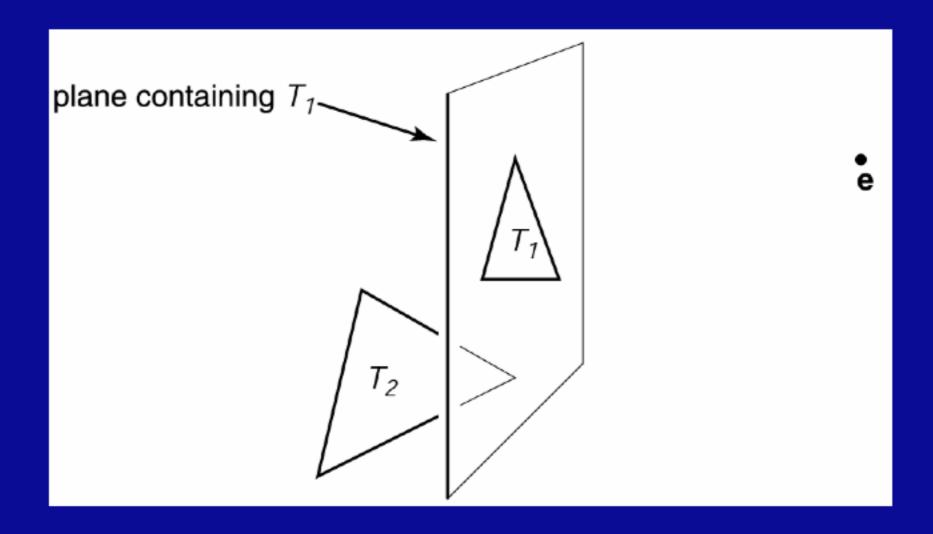
Using line 3 for the root requires a split





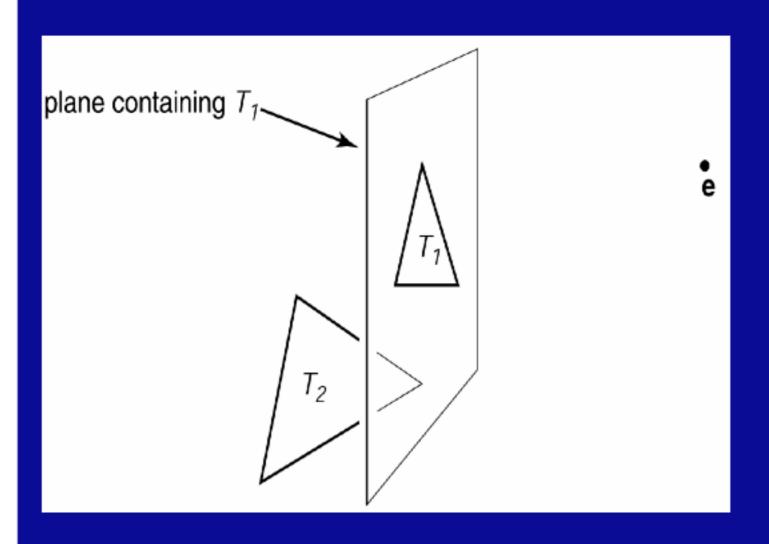
Triangles

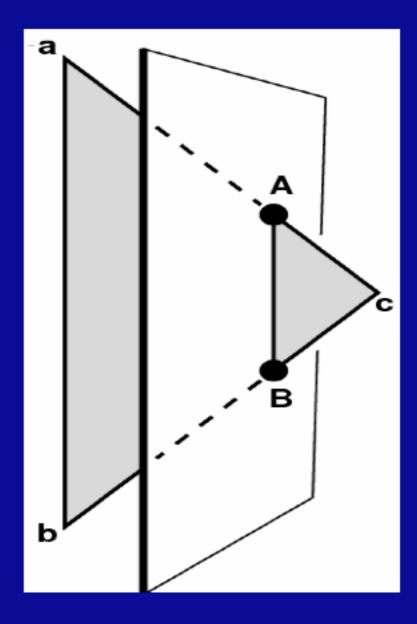
Use plane containing triangle T_1 to split the space If view point is on one side of the plane draw polygons on the other side first T_2 does not intersect plane of T_1



Triangles

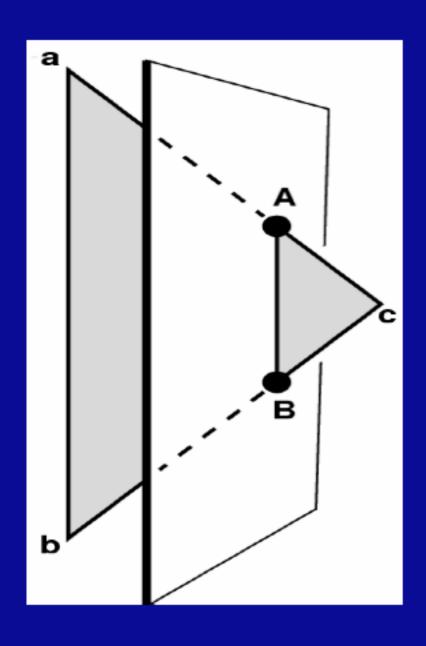
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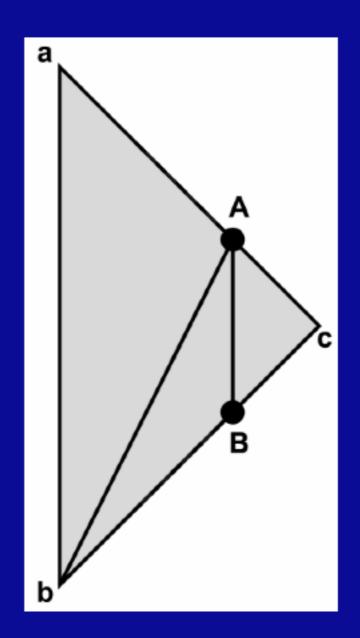




Triangles

Split Triangle





Building a Good Tree - the tricky part

- A naïve partitioning of n polygons will yield O(n³)
 polygons because of splitting!
- Algorithms exist to find partitionings that produce O(n²).
 - For example, try all remaining polygons and add the one which causes the fewest splits
 - Fewer splits -> larger polygons -> better polygon fill efficiency
- Also, we want a balanced tree.

Painter's Algorithm with BSP trees

- Build the tree
 - Involves splitting some polygons
 - Slow, but done only once for static scene
- Correct traversal lets you draw in back-to-front or frontto-back order for any viewpoint
 - Order is view-dependent
 - Pre-compute tree once
 - Do the "sort" on the fly
- Will not work for changing scenes

Drawing a BSP Tree

Each polygon has a set of coefficients:

```
Ax + By + Cz + D
```

Plug the coordinates of the viewpoint in and see:

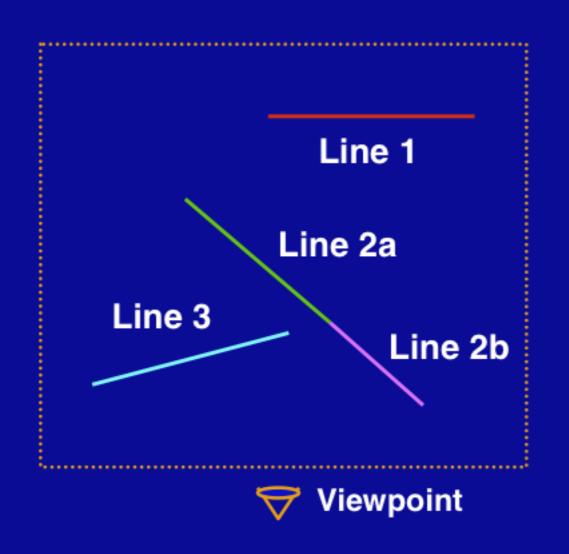
```
>0 : front side
<0 : back facing
=0 : on plane of polygon
```

- Back-to-front draw: inorder traversal, do farther child first
- Front-to-back draw: inorder traversal, do near child first

```
front_to_back(tree, viewpt) {
   if (tree == null) return;
   if (positive_side_of(root(tree), viewpt)) {
      front_to_back(positive_branch(tree, viewpt);
      display_polygon(root(tree));
      front_to_back(negative_branch(tree, viewpt);
   }
   else { ...draw negative branch first...}
}
```

Drawing Back to Front

Use Painter's Algorithm for hidden surface removal



Steps:

-Draw objects on far side of line 3

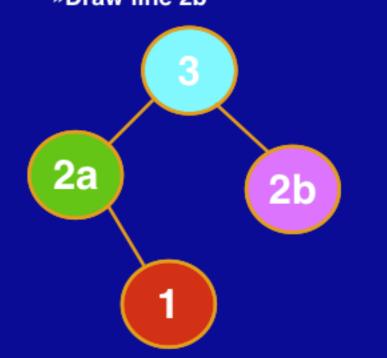
»Draw objects on far side of line 2a

-Draw line 1

»Draw line 2a

-Draw line 3

-Draw objects on near side of line 3
»Draw line 2b



Demos

BSP Tree construction

http://symbolcraft.com/graphics/bsp/index.html

KD Tree construction

http://www.cs.umd.edu/~brabec/quadtree/index.html

Real-time and Interactive Ray Tracing

The OpenRT Real-Time Ray-Tracing Project http://www.openrt.de/index.php

- Interactive ray tracing via space subdivision http://www.cs.utah.edu/~reinhard/egwr/
- Interactive ray tracing with good hardware http://www.cs.utah.edu/vissim/projects/raytracing/