Andrew login ID: ____________________________
Full Name: ________________________________

CS 15-213, Fall 2007

Exam 1

Wednesday October 17, 2007

Instructions:

• Make sure that your exam is not missing any sheets, then write your full name and Andrew login ID on the front.

• Write your answers in the space provided below the problem. If you make a mess, clearly indicate your final answer.

• The exam has a maximum score of XX points.

• The problems are of varying difficulty. The point value of each problem is indicated. Pile up the easy points quickly and then go back to the harder problems.

• This exam is OPEN BOOK. You may use any books or notes you like. Calculators are allowed, but no other electronic devices. Good luck!

<table>
<thead>
<tr>
<th>1 (8):</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 (8):</td>
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<tr>
<td>3 (8):</td>
</tr>
<tr>
<td>4 (6):</td>
</tr>
<tr>
<td>5 (8):</td>
</tr>
<tr>
<td>6 (8):</td>
</tr>
<tr>
<td>7 (10):</td>
</tr>
</tbody>
</table>

TOTAL (XX):
Problem 1. (8 points):
Assume we are running code on an IA32 machine, which has a 32-bit word size and uses two’s complement arithmetic for signed integers. Consider the following definitions:

```c
int x = foo();
unsigned ux = x;
```

Fill in the empty boxes in the table below. For each of the C expressions in the first column, either:

- State that it is true of all possible values returned by `foo()`, or
- Give an example where it is not true.

<table>
<thead>
<tr>
<th>Puzzle</th>
<th>True / Counterexample</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>x &lt; 0 ⇒ (x*2) &lt; 0</code></td>
<td>False (TMin)</td>
</tr>
<tr>
<td><code>x &lt; 0 ⇒ (x-1) &lt; 0</code></td>
<td></td>
</tr>
<tr>
<td><code>x &gt;= 0 ⇒ ((x ^ (x&gt;&gt;31))) &lt;= 0</code></td>
<td></td>
</tr>
<tr>
<td><code>x &gt; 0 ⇒ (x+ux) &gt; 0U</code></td>
<td></td>
</tr>
<tr>
<td><code>x &lt; 0 ⇒ (~x+1) &gt; 0</code></td>
<td></td>
</tr>
<tr>
<td><code>(~(x&gt;&gt;31)+1) == (x&lt;0)</code></td>
<td></td>
</tr>
<tr>
<td><code>(-(x^x) &amp; x) == 0</code></td>
<td></td>
</tr>
<tr>
<td><code>(~(ux&gt;&gt;31) &amp; ux) != ux</code></td>
<td></td>
</tr>
<tr>
<td><code>x &gt;= 0 ⇒ -(~x &gt;&gt; 1) + 1) &gt; 0</code></td>
<td></td>
</tr>
</tbody>
</table>
Problem 2. (8 points):
Consider the following 5-bit floating point representation based on the IEEE floating point format. This format does not have a sign bit – it can only represent nonnegative numbers.

- There are \( k = 3 \) exponent bits. The exponent bias is 3.
- There are \( n = 2 \) fraction bits.

Numeric values are encoded as a value of the form \( V = M \times 2^E \), where \( E \) is exponent after biasing, and \( M \) is the significand value. The fraction bits encode the significand value \( M \) using either a denormalized (exponent field 0) or a normalized representation (exponent field nonzero).

Below, you are given some decimal values, and your task it to encode them in floating point format. If rounding is necessary, you should use round-to-even, as you did in Lab 1 for the float_i2f puzzle. In addition, you should give the rounded value of the encoded floating point number. Give these as whole numbers (e.g., 17) or as fractions in reduced form (e.g., 3/4).

<table>
<thead>
<tr>
<th>Value</th>
<th>Floating Point Bits</th>
<th>Rounded value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( 9/32 )</td>
<td>0 0 1 0 0</td>
<td>1/4</td>
</tr>
<tr>
<td>( 7/8 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( 15/16 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( 9 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( 10 )</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
**Problem 3. (8 points):**

Consider the following C function’s x86-64 assembly code:

```
# On entry %edi = n
#
0000000000004004a8 <foo>:
4004a8:  b8 00 00 00 00              mov $0x0,%eax
4004ad:  83 ff 01                     cmp $0x1,%edi
4004b0:  7e 1a                        jle 4004cc <foo+0x24>
4004b2:  01 f8                        add %edi,%eax
4004b4:  ba 00 00 00 00              mov $0x0,%edx
4004b9:  39 fa                        cmp %edi,%edx
4004bb:  7d 08                        jge 4004c5 <foo+0x1d>
4004bd:  01 d0                        add %edx,%eax
4004bf:  ff c2                        inc %edx
4004c1:  39 fa                        cmp %edi,%edx
4004c3:  7c f8                        jl 4004bd <foo+0x15>
4004c5:  ff cf                        dec %edi
4004c7:  83 ff 01                     cmp $0x1,%edi
4004ca:  7f e6                        jg 4004b2 <foo+0x1a>
4004cc:  f3 c3                       repz retq  # treat repz as a no-op
```

Please fill in the corresponding C code:

```
int foo (int n) {
    int a, i;

    a = 0;
    for (; n > _____; _____) {
        a = a + _____;
        for (i = _____; i < _____; _____)
            a = a + _____;
    }
    return _____;
}
```
Problem 4. (6 points):

Consider the C code below, where $H$ and $J$ are constants declared with `#define`.

```c
int array1[H][J];
int array2[J][H];

int copy_array(int x, int y) {
    array2[y][x] = array1[x][y];
    return 1;
}
```

Suppose the above C code generates the following x86-64 assembly code:

```assembly
# On entry:
#   %edi = x
#   %esi = y
#
copy_array:
    movslq %esi, %rsi
    movslq %edi, %rdi
    movq %rsi, %rax
    salq $7, %rax
    subq %rsi, %rax
    leaq (%rdi, %rdi, 2), %rdi
    addq %rdi, %rdi
    movl array1(,%rdi,4), %edx
    movl %edx, array2(,%rax,4)
    movl $1, %eax
    ret
```

What are the values of $H$ and $J$?

$H =$

$J =$
**Problem 5. (6 points):**
Consider the following C declarations:

```c
typedef struct {
    int x;
    int y;
    int sensor_id;
} Sensor;

typedef struct {
    int sensor_id;
    double data;
} Data;

typedef struct {
    Sensor *sensor;
    char status;
} Sensor_Status;

Sensor sensor;
Data data;
Sensor_Status status_array[10];
```

For all of the following, **assume x86-64 alignment.**

A. What is the total allocated space for `sensor`? __________ bytes

B. What is the total wasted space for `sensor`? __________ bytes

C. What is the total allocated space for `data`? __________ bytes

D. What is the total wasted space for `data`? __________ bytes

E. What is the total allocated space for `status_array`? __________ bytes

F. What is the total wasted space for `status_array`? __________ bytes
Problem 6. (8 points):
Consider the following data structure declarations:

```c
struct node {
    struct data d;
    struct node *next;
};
```

```c
struct data {
    int x;
    char str[6];
};
```

Below are given four C functions and four x86-64 code blocks. Next to each of the x86-64 code blocks, write the name of the C function that it implements.

```c
int alpha(struct node *ptr) {
    return ptr->d.x;
}
```

```assemble
movq 16(%rdi), %rax
addq $4, %rax
ret
```

```c
char *beta(struct node *ptr) {
    ptr = ptr->next;
    return ptr->d.str;
}
```

```assemble
movq (%rdi), %rax
ret
```

```c
char gamma (struct node *ptr) {
    return ptr->d.str[4];
}
```

```assemble
movl (%rdi), %eax
ret
```

```c
int *delta (struct node *ptr) {
    struct data *dp =
        (struct data *) ptr;
    return &dp->x;
}
```

```assemble
movsbl 8(%rdi),%eax
ret
```
Reverse Engineering Switch Code

The next problem concerns the code generated by GCC for a function involving a switch statement. Following a bounds check, the code uses a jump to index into the jump table

\[
400476: \text{ff 24 d5 a0 05 40 00 jmpq } *0x4005a0(,%rdx,8)
\]

Using GDB, we extract the 8-entry jump table as:

- \(0x4005a0\): 0x0000000000400480 0x0000000000400491
- \(0x4005b0\): 0x0000000000400480 0x0000000000400496
- \(0x4005c0\): 0x0000000000400480 0x0000000000400489
- \(0x4005d0\): 0x0000000000400485 0x0000000000400496

The following block of disassembled code implements the branches of the switch statement

\[
\begin{align*}
400480: & \text{48 8d 04 3f lea } (%rdi,%rdi,1),%rax \\
400484: & \text{c3 retq} \\
400485: & \text{48 0f af f7 imul } %rdi,%rsi \\
400489: & \text{48 89 f8 mov } %rdi,%rax \\
40048c: & \text{48 21 f0 and } %rsi,%rax \\
40048f: & \text{90 nop} \\
400490: & \text{c3 retq} \\
400491: & \text{48 8d 04 37 lea } (%rdi,%rsi,1),%rax \\
400495: & \text{c3 retq} \\
400496: & \text{48 8d 46 ff lea } 0xffffffffffffffff(%rsi),%rax \\
40049a: & \text{c3 retq}
\end{align*}
\]
Problem 7. (10 points):
Fill in the blank portions of the C code below to reproduce the function corresponding to this object code. You can assume that the first entry in the jump table is for the case when \( s \) equals 0. Parameters \( a, b, \) and \( s \) are passed in registers %rdi, %rsi, and %rdx, respectively.

```c
long fun(long a, long b, long s)
{
    long result = 0;
    switch (s) {
    case ___:
    case ___:
        result = _____;
        break;
    case ___:
        b = _____;
        /* Fall through */
    case ___:
        result = _____;
        break;
    case ___:
        result = _____;
        break;
    default:
        result = _____;
    }
    return result;
}
```
Problem 8. (16 points):

Consider a computer with an 8-bit address space and an associative 64-byte data cache, with a LRU replacement policy. Assume that the cache is 2-way set associative and has 8-byte cache lines. The boxes below represent the bit-format of a physical address. In each box, indicate which field that bit represents (it’s possible that a field doesn’t exist). Here are the fields:

CO The byte offset within the cache line
CI The cache (set) index
CT The cache tag

<table>
<thead>
<tr>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
<th>0</th>
</tr>
</thead>
</table>

The table below on the left shows a trace of load addresses accessed in the data cache. Below on the right is a list of possible final states of the cache, showing the hex value of the tag for each cache line in each set. Which is the correct final cache state? How many of the loads were hits? Assume that initially all cache lines are invalid (represented by X), and that **sets are filled from left to right**.

<table>
<thead>
<tr>
<th>Load No.</th>
<th>Hex Address</th>
<th>Binary Address</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1a</td>
<td>0001 1010</td>
</tr>
<tr>
<td>2</td>
<td>55</td>
<td>0101 0101</td>
</tr>
<tr>
<td>3</td>
<td>e6</td>
<td>1110 0110</td>
</tr>
<tr>
<td>4</td>
<td>53</td>
<td>0101 0011</td>
</tr>
<tr>
<td>5</td>
<td>77</td>
<td>0111 0111</td>
</tr>
<tr>
<td>6</td>
<td>28</td>
<td>0010 1000</td>
</tr>
<tr>
<td>7</td>
<td>94</td>
<td>1001 0100</td>
</tr>
<tr>
<td>8</td>
<td>a6</td>
<td>1010 0110</td>
</tr>
<tr>
<td>9</td>
<td>75</td>
<td>0111 0101</td>
</tr>
<tr>
<td>10</td>
<td>c7</td>
<td>1100 0111</td>
</tr>
<tr>
<td>11</td>
<td>56</td>
<td>0101 0110</td>
</tr>
</tbody>
</table>

(a)  
<table>
<thead>
<tr>
<th>Set 3</th>
<th>Set 2</th>
<th>Set 1</th>
<th>Set 0</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>X</td>
<td>4</td>
<td>2</td>
</tr>
<tr>
<td>1</td>
<td>X</td>
<td>6</td>
<td>5</td>
</tr>
</tbody>
</table>

(b)  
<table>
<thead>
<tr>
<th>Set 3</th>
<th>Set 2</th>
<th>Set 1</th>
<th>Set 0</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>X</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>1</td>
<td>X</td>
<td>6</td>
<td>5</td>
</tr>
</tbody>
</table>

(c)  
<table>
<thead>
<tr>
<th>Set 3</th>
<th>Set 2</th>
<th>Set 1</th>
<th>Set 0</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>X</td>
<td>2</td>
<td>4</td>
</tr>
<tr>
<td>1</td>
<td>X</td>
<td>6</td>
<td>5</td>
</tr>
</tbody>
</table>

(d)  
<table>
<thead>
<tr>
<th>Set 3</th>
<th>Set 2</th>
<th>Set 1</th>
<th>Set 0</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>X</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>1</td>
<td>X</td>
<td>7</td>
<td>6</td>
</tr>
</tbody>
</table>

(e)  
<table>
<thead>
<tr>
<th>Set 3</th>
<th>Set 2</th>
<th>Set 1</th>
<th>Set 0</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>X</td>
<td>4</td>
<td>2</td>
</tr>
<tr>
<td>1</td>
<td>X</td>
<td>7</td>
<td>6</td>
</tr>
</tbody>
</table>

(f)  
<table>
<thead>
<tr>
<th>Set 3</th>
<th>Set 2</th>
<th>Set 1</th>
<th>Set 0</th>
</tr>
</thead>
<tbody>
<tr>
<td>X</td>
<td>0</td>
<td>5</td>
<td>2</td>
</tr>
<tr>
<td>1</td>
<td>3</td>
<td>7</td>
<td>6</td>
</tr>
</tbody>
</table>

(g)  
<table>
<thead>
<tr>
<th>Set 3</th>
<th>Set 2</th>
<th>Set 1</th>
<th>Set 0</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>2</td>
<td>4</td>
<td>2</td>
</tr>
<tr>
<td>1</td>
<td>3</td>
<td>5</td>
<td>6</td>
</tr>
</tbody>
</table>

Correct final state: _____  Number of hits: _____
**Problem 9. (7 points):**
Consider the C code below:

```c
int forker(int x) {
    int pid;

    printf("A");
    if (x > 0) {
        pid = fork();
        printf("B");
        if (pid == 0) {
            printf("C");
        } else {
            waitpid(pid, NULL, 0);
            printf("D");
            if (x == 5) {
                pid = fork();
                if (pid != 0) {
                    exit(8);
                }
                printf("E");
            }
        }
    }
    printf("F");
    exit(4);
}
```

Consider each of the following outputs and circle the ones that could be produced by the code above (after all processes are terminated).

AA

ABCDEF

ABCBFDF

ABCBDF

ABCBFDE

ABCFBDF

ABBCFDEF