



## Example Floating Point Problem

### Problem 1:

consider the following 7-bit floating point representation based on the IEEE floating point format:

- There is a sign bit in the most significant bit.
- The next  $k = 3$  bits are the exponent. The exponent bias is 3.
- The last  $n = 3$  bits are the fractional part.

Numeric values are encoded in this format as a value of the form  $V = (-1)^s \times M \times 2^E$ , where  $s$  is the sign bit,  $E$  is exponent after biasing, and  $M$  is the significand.

### Part I

Answer the following problems using either decimal (e.g., 1.375) or fractional (e.g., 11/8) representations for numbers that are not integers.

A. For denormalized numbers:

- (a) What is the value  $E$  of the exponent after biasing? \_\_\_\_\_
- (b) What is the largest value  $M$  of the significand? \_\_\_\_\_

B. For normalized numbers:

- (a) What is the smallest value  $E$  of the exponent after biasing? \_\_\_\_\_
- (b) What is the largest value  $E$  of the exponent after biasing? \_\_\_\_\_
- (c) What is the largest value  $M$  of the significand? \_\_\_\_\_

### Part II

Fill in the blank entries in the following table giving the encodings for some interesting numbers.

Description	$E$	$M$	$V$	Binary Encoding
Zero		0	0	0 000 0000
Smallest Positive (nonzero)				
Largest denormalized				
Smallest positive normalized				
One			1	
Largest finite number				
NaN	—	—	NaN	
Infinity	—	—	$+\infty$	

**Recommended Book Practice Problems:** 2.33, 2.34, 2.37  
Solutions are at the end of the chapter.