CS 15-213, Spring 2009
Exam 2
Tuesday, April 7th, 2009

Instructions:

• Make sure that your exam is not missing any sheets, then write your full name, Andrew login ID, and recitation section (A–J) on the front.

• Do not write any part of your answers outside of the space given below each question. Write clearly and at a reasonable size. If we have trouble reading your handwriting you will receive no credit on that problem.

• The exam has a maximum score of 100 points.

• The problems are of varying difficulty. The point value of each problem is indicated. Pile up the easy points quickly and then come back to the harder problems.

• This exam is OPEN BOOK. You may use any books or notes you like. No calculators or other electronic devices are allowed.

• Good luck!

| 1 (20):          |
|                 |
| 2 (15):         |
|                 |
| 3 (15):         |
|                 |
| 4 (15):         |
|                 |
| 5 (10):         |
|                 |
| 6 (25):         |
|                 |
| TOTAL (100):    |
Problem 1. (20 points):
In this problem, you will perform cache analysis for three code sequences. Assume a very small direct mapped 16 byte data cache with two cache lines. We assume a float requires 4 bytes. Drawing the cache helps.

For each code sequence, we assume a cold cache and that the array $X$ is cache aligned (that is, $X[0]$ is loaded into the the beginning of the first cache line. All other variables are held in registers.

Recall that miss rate is defined as $\frac{\#\text{misses}}{\#\text{accesses}}$.

1. Code 1:

   ```c
   float X[8], t = 0;
   for(int j = 0; j < 2; j++)
       for(int i = 0; i < 8; i++)
           t += X[i];
   ```

   Answer the following:
   (a) Miss rate:
   (b) What types of types of locality does this code have with respect to this cache?

2. Code 2:

   ```c
   float X[8], t = 0;
   for(int j = 0; j < 2; j++)
       {
           for(int i = 0; i < 7; i += 2)
               t += X[i];
           for(int i = 1; i < 8; i += 2)
               t += X[i];
       }
   ```

   Answer the following:
   (a) Miss rate:
   (b) What types of types of locality does this code have with respect to this cache?

3. Code 3:

   ```c
   float X[8], float t = 0;
   for(i = 0; i < 2; i++)
       for(k = 0; k < 2; k++)
           for(j = 0; j < 4; j++)
               t += X[j + i * 4];
   ```
Answer the following:

(a) Miss rate:

(b) What types of locality does this code have with respect to this cache?

4. Changing Cache:

All three code fragments above perform the same computation. Assume you could change the code any way you want to perform the same computation and also change the cache as you wish.

(a) What is the minimum number of cache misses achievable?

(b) How would the cache look like to achieve this?
Problem 2. (15 points):

1. If a direct mapped cache is 8KB in size, and has 32 byte cache blocks, how many lines are there in each set?
   (a) 256
   (b) 64
   (c) 32
   (d) 1

2. You have a 32-bit virtual memory system with 4KB page frames, with a TLB with 4 sets, each of which is 8-way set associative. How many bits of the virtual address form the TLBi (TLB index)?
   (a) 2
   (b) 4
   (c) 8
   (d) 12

3. Which of these features in a system best justifies the use of a two level page table structure, as opposed to a one level page table structure?
   (a) Small page sizes
   (b) Frequent memory accesses
   (c) High degree of spatial locality in programs
   (d) Sparse memory usage patterns

4. Which section of an ELF file contains the compiled functions from a program?
   (a) .data
   (b) .rodata
   (c) .text
   (d) .bss

5. Which of the following is true?
   (a) Every signal that is sent is also received
   (b) Signals are always received immediately since they cause an interrupt
   (c) Signals can only be received after a context switch
   (d) Signals can only be received upon returning from system mode
6. Consider a theoretical computer architecture with 50-bit virtual addresses and 16kb pages. What is the maximum number of levels of page tables that could be used in the virtual memory system?

   (a) 16
   (b) 36
   (c) 2
   (d) 50

7. Which blocks the signal SIGKILL?

   (a) signal(SIGKILL, SIG_IGN);
   (b) sigfillset(&set); sigprocmask(SIG_BLOCK, set);
   (c) a and b
   (d) none of the above

8. Which of the following will reduce the number of compulsory (cold) cache misses in a program?

   (a) Increasing the associativity
   (b) Increasing line size
   (c) Both a & b
   (d) None of the above

9. Linkers can take as input which of the following file types? (circle all correct answers)

   (a) .c
   (b) .o
   (c) .a
   (d) .s

10. Blocking matrix-matrix multiplication can increase what type(s) of locality?

    (a) Temporal
    (b) Spatial
    (c) Both

11. Give two functions that don’t return (two completely different functions, not variations of one).
Problem 3. (15 points):
Suppose we have the following two .c files:

```c
alarm.c

int counter;

void sigalrm_handler (int num) {
    counter += 1;
}

int main (void) {
    signal(SIGALRM, &sigalrm_handler);
    counter = 2;
    alarm(1);
    sleep(1);
    counter -= 3;
    exit(counter);
    return 0;
}

fork.c

int counter;

void sigchld_handler(int num) {
    int i;
    wait(&i);
    counter += WEXITSTATUS(i);
}

int main (void) {
    signal(SIGCHLD, &sigchld_handler);
    counter = 3;
    if (!fork()) {
        counter++;
        execl("alarm", "alarm", NULL);
    }
    sleep(2);
    counter *= 3;
    printf("%d\n", counter);
    exit(0);
}
```

Assume that all system calls succeed and that all C arithmetic statements are atomic.
The files are compiled as follows:
gcc -o alarm alarm.c
gcc -o fork fork.c
Suppose we run ./fork at the terminal. What are the possible outputs to the terminal?
Problem 4. (15 points):
Harry Q. Bovik builds and runs a C program from the following two files:

main.c:

#include <stdio.h>

long a = 1;
const long b = 2;
long c;
long d = -1;

int main(int argc, char *argv[]) {
    printf("a: %p\n b: %p\n c: %p\n d: %p\n", &a, &b, &c, &d);
    printf("%ld", c);
    return 0;
}

data.c:

unsigned int c[2] = {...};

And sees this output:

a: 0x601020
b: 0x400650
c: 0x601030
d: 0x601028
4294967297

Harry was expecting the variables to be in order, one after another. Obviously, he was very wrong. Help him figure out what’s happening using your knowledge of linking and executable layouts. Be specific but concise with your answers.

(a) How many symbols does main.c generate in the executable program’s symbol table?

(b) What are the strong symbols from main.c, and what are the weak symbols from main.c?
(c) Note the address of b. Why is it far removed from the addresses of the other variables?

(d) Why is c located after d in memory, even though it’s before d in Harry’s program?

(e) Note the output given by the final printf. Was Harry compiling and running the code on x86 or x86-64? How do you know?

(f) Given that $4294967297 = 2^{32} + 1$, what would be output by

```
printf("{%d, %d}\n", c[0], c[1]);
```

if it were executed in data.c?
Problem 5. (10 points):
Assume a System that has

1. A two way set associative TLB
2. A TLB with 8 total entries
3. \(2^8\) byte page size
4. \(2^{16}\) bytes of virtual memory
5. one (or more) boats

<table>
<thead>
<tr>
<th>Index</th>
<th>Tag</th>
<th>Frame Number</th>
<th>Valid</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0x27</td>
<td>0xC6</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>0x29</td>
<td>0x73</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>0x11</td>
<td>0xFF</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>0x0A</td>
<td>0xEC</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>0x29</td>
<td>0xCD</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>0x3A</td>
<td>0xAB</td>
<td>1</td>
</tr>
<tr>
<td>3</td>
<td>0x32</td>
<td>0xFB</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>0x23</td>
<td>0x46</td>
<td>0</td>
</tr>
</tbody>
</table>

Use the TLB to fill in the table. Strike out anything that you don’t have enough information to fill in.

<table>
<thead>
<tr>
<th>Virtual Address</th>
<th>Physical Address</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x8F0F</td>
<td></td>
</tr>
<tr>
<td></td>
<td>0x4690</td>
</tr>
<tr>
<td>0x2933</td>
<td>0x7300</td>
</tr>
<tr>
<td>0x2839</td>
<td></td>
</tr>
</tbody>
</table>
Problem 6. (25 points):

Suppose a processor can support up to 64-bits of physical memory, but for binary backwards-compatibility uses 32-bit virtual addresses. You have been assigned the task of designing a virtual memory scheme for this processor.

You must meet the following requirements:

1. The scheme must be able to map any 32-bit virtual address to any 64-bit physical address.
2. The scheme must use a 16KB page size.

You must meet the following performance constraints in addition to the above requirements:

1. The scheme must minimize the number of physical memory accesses needed to resolve a virtual address (that is, the scheme must minimize the number of levels of page tables).
2. The size of a page table at any level must not exceed 512 bytes.

This is your design. You may specify anything not already defined, including the size of page tables, the size of page table entries, etc. Design your system, and then answer the following questions:

How many levels of page tables are there?

What is the size of the table at each level?
Show the mapping of the bits of a virtual address to each level. To illustrate the notation we expect, please follow the convention shown in the example below (the mapping for standard two-level Intel x86-32 virtual memory). Notice that the first set of bits maps into the top level page table, the second set maps into the second level page table, etc.

```
31 30 29 28 27 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0
+---------------------------------------+---------------------------------------+---------------------------------------|
| VPN 1 | VPN 2 | OFFSET |
+---------------------------------------+---------------------------------------+---------------------------------------|
```

Draw your mapping here:

```
31 30 29 28 27 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0
+---------------------------------------+---------------------------------------+---------------------------------------|
|                                      |                                      |                                      |
+---------------------------------------+---------------------------------------+---------------------------------------|
```

What is the size of a page table entry at each level?