Andrew login ID:________________________
Full Name:__________________________
Recitation Section:____________________

CS 15-213, Spring 2008
Exam 1
Tue. February 26, 2008

Instructions:

• Make sure that your exam is not missing any sheets, then write your full name, Andrew login ID, and recitation section (A–H) on the front.

• Write your answers in the space provided below the problem. If you make a mess, clearly indicate your final answer.

• The exam has a maximum score of 70 points.

• The problems are of varying difficulty. The point value of each problem is indicated. Pile up the easy points quickly and then come back to the harder problems.

• This exam is OPEN BOOK. You may use any books or notes you like. No calculators or other electronic devices are allowed.

• Good luck!

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1 (8):</td>
<td></td>
</tr>
<tr>
<td>2 (8):</td>
<td></td>
</tr>
<tr>
<td>3 (10):</td>
<td></td>
</tr>
<tr>
<td>4 (9):</td>
<td></td>
</tr>
<tr>
<td>5 (8):</td>
<td></td>
</tr>
<tr>
<td>6 (8):</td>
<td></td>
</tr>
<tr>
<td>7 (11):</td>
<td></td>
</tr>
<tr>
<td>8 (8):</td>
<td></td>
</tr>
<tr>
<td>TOTAL (70):</td>
<td></td>
</tr>
</tbody>
</table>
Problem 1. (8 points):

For this problem, assume the following:

- We are running code on a 6-bit machine using two’s complement arithmetic for signed integers.
- short integers are encoded using 3 bits.
- Sign extension is performed whenever a short is casted to an int
- Right shifts of ints are arithmetic.

Fill in the empty boxes in the table below. The following definitions are used in the table:

```c
int a = -29;
short b = (short)a;
unsigned ua = a;
int x = -21;
short y = (short)x;
unsigned ux = x;
```

Note: You need not fill in entries marked with “—”.

<table>
<thead>
<tr>
<th>Expression</th>
<th>Decimal Representation</th>
<th>Binary Representation</th>
</tr>
</thead>
<tbody>
<tr>
<td>—</td>
<td>27</td>
<td></td>
</tr>
<tr>
<td>—</td>
<td></td>
<td>100100</td>
</tr>
<tr>
<td>x</td>
<td></td>
<td></td>
</tr>
<tr>
<td>y</td>
<td></td>
<td></td>
</tr>
<tr>
<td>ux</td>
<td></td>
<td></td>
</tr>
<tr>
<td>a &gt;&gt; 2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>ua &gt;&gt; 2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>b &lt;&lt; 1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>–TMin</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Problem 2. (8 points):

Part A

Fill in the blanks in the table below with the number described in the first column of each row. You can give your answers as unexpanded simple arithmetic expressions (such as $15^{213} + 42$); you should not have trouble fitting your answers into the space provided.

<table>
<thead>
<tr>
<th>Description</th>
<th>Number</th>
</tr>
</thead>
<tbody>
<tr>
<td>int x=1; float * f = (float *) &amp;x; What is the value of f?</td>
<td></td>
</tr>
<tr>
<td>int x=-1; float * f = (float *) &amp;x; What is the value of f?</td>
<td></td>
</tr>
<tr>
<td>Smallest positive integer that cannot be represented as a 32-bit float</td>
<td></td>
</tr>
</tbody>
</table>

Part B

Assume we are running code on an IA32 machine, which has a 32-bit word size and uses two’s complement arithmetic for signed integers. Consider the following definition:

```c
int x = foo();
```

Fill in the empty boxes in the table below. For each of the C expressions in the first column, either:

- State that it is true of all argument values, or
- Give an example where it is not true.

<table>
<thead>
<tr>
<th>Puzzle</th>
<th>True / Counterexample</th>
</tr>
</thead>
<tbody>
<tr>
<td>$x &lt; 0 \Rightarrow -x &gt; 0$</td>
<td></td>
</tr>
<tr>
<td>$x \wedge \lnot x &lt; 0$</td>
<td></td>
</tr>
<tr>
<td>$(x \wedge (x &gt;&gt; 31)) + 1 &gt; 0$</td>
<td></td>
</tr>
<tr>
<td>$((!!x) &lt;&lt; 31) &gt;&gt; 31) &amp; x == x$</td>
<td></td>
</tr>
</tbody>
</table>
Problem 3. (10 points):
Consider an 8-bit IEEE floating-point representation with:

- 1 sign bit
- 3 exponent bits (therefore the bias $B = 2^{3-1} - 1 = 3$)
- 4 mantissa bits

A. Fill in the blanks in the following table. Express numerical values as fractions (e.g., $277/512$).

<table>
<thead>
<tr>
<th>Number</th>
<th>Bit representation</th>
</tr>
</thead>
<tbody>
<tr>
<td>3/8</td>
<td></td>
</tr>
<tr>
<td>$-\infty$</td>
<td></td>
</tr>
<tr>
<td>9/2</td>
<td>0 010 0101</td>
</tr>
</tbody>
</table>

B. Give the bit representation and numerical value of the largest number representable in this format as a denormalized floating-point number.

C. Give the bit representation and numerical value of the largest number representable in this format as a normalized floating-point number.
Problem 4. (9 points):
Consider the following x86-64 assembly code:

```
# on entry: %rdi = n, %rsi = A
000000000040056e <bar>:
40056e: 41 b8 00 00 00 00 mov $0x0,%r8d
400574: 41 b9 00 00 00 00 mov $0x0,%r9d
40057d: 7d 30 jge 4005af <bar+0x41>
40057f: ba 00 00 00 00 mov $0x0,%edx
400584: 39 fa cmp %edi,%edx
400586: 7d 1f jge 4005a7 <bar+0x39>
400588: 49 63 c1 movslq %r9d,%rax
40058b: 48 8b 0c c6 mov (%rsi,%rax,8),%rcx
40058f: 48 63 c2 movslq %edx,%rax
400592: 8b 04 81 mov (%rcx,%rax,4),%eax
400595: 41 0f af c1 imul %r9d,%eax
40059b: 41 0f af c2 imul %edx,%eax
40059f: 48 98 cltq
4005a1: 49 01 c0 add %rax,%r8
4005a3: ff c2 inc %edx
4005a5: 39 fa cmp %edi,%edx
4005a7: 7c e8 jl 40058f <bar+0x21>
4005aa: 41 39 f9 cmp %edi,%r9d
4005ad: 7c d0 jl 40057f <bar+0x11>
4005af: 4c 89 c0 mov %r8,%rax
4005b2: c3 retq
```

Fill in BOTH of the blanks below for the corresponding C code.

```c
long bar(int n, ________________ A) { // Fill in type of A
    long sum = 0;
    int i,j;
    for (i = 0; i < n; i++) {
        for(j = 0; j < n; j++)
            sum += _____________________; // Fill in expression
    }
    return sum;
}
```
Problem 5. (8 points):
Consider the C code below, where \( H \) and \( J \) are constants declared with `#define`.

```c
int array1[H][J];
int array2[J][H];

int copy_array(int x, int y) {
    array2[y][x] = array1[x][y];
    return 1;
}
```

Suppose the above C code generates the following x86-64 assembly code:

```assembly
# On entry:
# %edi = x
# %esi = y

# copy_array:
    movslq %edi,%rdi
    movslq %esi,%rsi
    movq %rdi, %rax
    leaq (%rsi,%rsi,8), %rdx
    salq $5, %rax
    subq %rdi, %rax
    addq %rdi, %rdx
    leaq (%rsi,%rax,2), %rax
    movl array1(,%rax,4), %eax
    movl %eax, array2(,%rdx,4)
    movl $1, %eax
    ret
```

What are the values of \( H \) and \( J \)?

\( H = \)

\( J = \)
Problem 6. (8 points):
Consider the following data structure declaration:

```c
struct node{
    char x;
    int array[2];
    int idx;
    struct node *next;
};
```

Below are given four C functions and four x86-64 code blocks.

```c
char *mon(struct node *ptr){
    return &ptr->x;
}
```

```c
int tue(struct node *ptr){
    return ptr->array[ptr->idx];
}
```

```c
void wed(struct node *ptr){
    ptr->idx = ptr->array[1];
    return;
}
```

```c
char thu(struct node *ptr){
    ptr = ptr->next;
    return ptr->x;
}
```

In the following table, next to the name of each x86-64 code block, write the name of the C function that it implements.

<table>
<thead>
<tr>
<th>Code Block</th>
<th>Function Name</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td></td>
</tr>
<tr>
<td>B</td>
<td></td>
</tr>
<tr>
<td>C</td>
<td></td>
</tr>
<tr>
<td>D</td>
<td></td>
</tr>
</tbody>
</table>
Problem 7. (11 points):

The next problem concerns code generated by GCC for a function involving a switch statement. The code uses a jump to index into the jump table:

```
400518: ff 24 d5 40 06 40 00 jmpq *0x400640(%rdx,8)
```

Using GDB, we extract the 8-entry jump table as:

```
0x400640: 0x0000000000400527
0x400648: 0x0000000000400525
0x400650: 0x0000000000400531
0x400658: 0x000000000040051f
0x400660: 0x0000000000400525
0x400668: 0x0000000000400525
0x400670: 0x000000000040052a
0x400678: 0x0000000000400531
```

The following block of disassembled code implements the branches of the switch statement:

```
# on entry: %rdi = a, %rsi = b, %rdx = c
400510: 31 c0 xor %eax,%eax
400512: 48 83 fa 07 cmp $0x7,%rdx
400516: 77 0d ja 400525 <_Z4testlll+0x15>
400518: ff 24 d5 40 06 40 00 jmpq *0x400640(%rdx,8)
40051f: 48 89 f0 mov %rsi,%rax
400522: 48 29 f8 sub %rdi,%rax
400525: f3 c3 repz retq # repz is a no-op here
400527: 48 01 f7 add %rsi,%rdi
40052a: 48 89 f8 mov %rdi,%rax
40052d: 48 31 f0 xor %rsi,%rax
400530: c3 retq
400531: 48 8d 46 2a lea 0x2a(%rsi),%rax
400535: c3 retq
```
Fill in the blank portions of C code below to reproduce the function corresponding to this object code. You can assume that the first entry in the jump table is for the case when `c` equals 0.

```c
long test(long a, long b, long c)
{
    long answer = _____;
    switch(c)
    {
        case ___:
            answer = _____;
            break;
        case ___:
        case ___:
            answer = _____;
            break;
        case ___:
            a = _____;
            /* Fall through */
        case ___:
            answer = _____;
            break;
        default:
            answer = _____;
    }

    return answer;
}
```
Problem 8. (8 points):

```c
struct BOOKLIST {
    char a;
    short US;
    char b;
    short CA;
    char c;
    double EU;
    char d;
    int UK;
} booklist;
```

A. Show how the struct above would appear on a 32 bit Windows machine (primitives of size k are k byte aligned). Label the bytes that belong to the various fields with their names and clearly mark the end of the struct. Use hatch marks to indicate bytes that are allocated in the struct but are not used.

[Diagram of memory allocation for part A]

B. Rearrange the above fields in `booklist` to conserve the most space in the memory below. Label the bytes that belong to the various fields with their names and clearly mark the end of the struct. Use hatch marks to indicate bytes that are allocated in the struct but are not used.

[Diagram of memory allocation for part B]

C. How many bytes of the struct are wasted in part A?

D. How many bytes of the struct are wasted in part B?