Machine-Level Programming II: Arithmetic & Control

15-213 / 18-213: Introduction to Computer Systems
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Today

- **Complete addressing mode, address computation (leal)**
- Arithmetic operations
- Control: Condition codes
- Conditional branches
- While loops

Complete Memory Addressing Modes

- **Most General Form**
- **D(Rb,Ri,S)   Mem[Reg[Rb]+S*Reg[Ri]+ D]**
  - D: Constant "displacement" 1, 2, or 4 bytes
  - Rb: Base register: Any of 8 integer registers
  - Ri: Index register: Any, except for `%esp`
    - Unlikely you'd use `%ebp`, either
  - S: Scale: 1, 2, 4, or 8 (why these numbers?)

- **Special Cases**
- **(Rb,Ri)   Mem[Reg[Rb]+Reg[Ri]]**
- **D(Rb,Ri)   Mem[Reg[Rb]+Reg[Ri]+D]**
- **(Rb,Ri,S)   Mem[Reg[Rb]+S*Reg[Ri]]**

Address Computation Examples

%edx	0xf000
%ecx	0x0100

Expression	Address Computation	Address
0x8(%edx)		
(%edx,%ecx)		
(%edx,%ecx,4)		
0x80(,%edx,2)		

Address Computation Instruction

- **`leal` Src,Dest**
  - Src is address mode expression
  - Set Dest to address denoted by expression

- **Uses**
  - Computing addresses without a memory reference
    - E.g., translation of `p = &x[i];`
  - Computing arithmetic expressions of the form x + k*y
    - k = 1, 2, 4, or 8

- **Example**

```
int mul12(int x)
{
  return x*12;
}
```

Converted to ASM by compiler:

```
leal (%eax,%eax,2), %eax   ;t <- x+x*2
sall $2, %eax              ;return t<<2
```

Today

- Complete addressing mode, address computation (leal)
- **Arithmetic operations**
- Control: Condition codes
- Conditional branches
- While loops

Some Arithmetic Operations

- **Two Operand Instructions:**

Format		Computation	
`addl`	Src,Dest	Dest = Dest + Src	
`subl`	Src,Dest	Dest = Dest - Src	
`imull`	Src,Dest	Dest = Dest * Src	
`sall`	Src,Dest	Dest = Dest << Src	Also called shll
`sarl`	Src,Dest	Dest = Dest >> Src	Arithmetic
`shrl`	Src,Dest	Dest = Dest >> Src	Logical
`xorl`	Src,Dest	Dest = Dest ^ Src	
`andl`	Src,Dest	Dest = Dest & Src	
`orl`	Src,Dest	Dest = Dest | Src	

- **Watch out for argument order!**
- **No distinction between signed and unsigned int (why?)**

Some Arithmetic Operations

- **One Operand Instructions**

`incl`	Dest	Dest = Dest + 1
`decl`	Dest	Dest = Dest - 1
`negl`	Dest	Dest = - Dest
`notl`	Dest	Dest = ~Dest

- **See book for more instructions**

Arithmetic Expression Example

```
int arith(int x, int y, int z)
{
  int t1 = x+y;
  int t2 = z+t1;
  int t3 = x+4;
  int t4 = y * 48;
  int t5 = t3 + t4;
  int rval = t2 * t5;
  return rval;
}
```

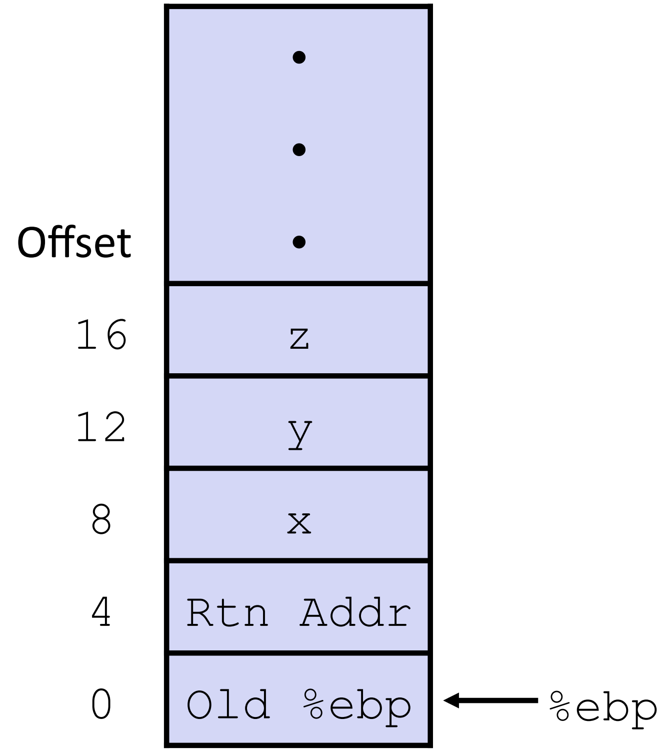
```
arith:
  pushl  %ebp                  } Set
  movl   %esp, %ebp            } Up

  movl   8(%ebp), %ecx         }
  movl   12(%ebp), %edx        }
  leal   (%edx,%edx,2), %eax   }
  sall   $4, %eax              } Body
  leal   4(%ecx,%eax), %eax    }
  addl   %ecx, %edx            }
  addl   16(%ebp), %edx        }
  imull  %edx, %eax            }

  popl   %ebp                  } Finish
  ret                          }
```

Understanding `arith`

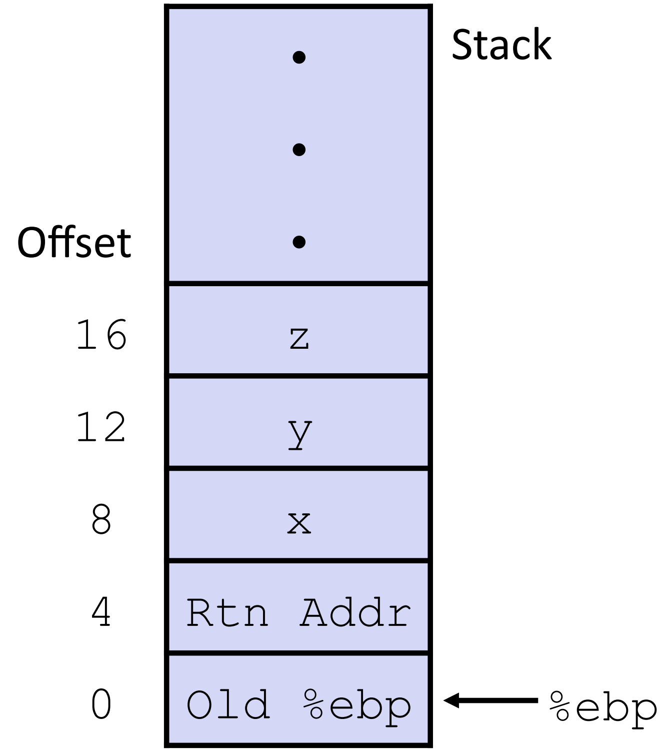
```
int arith(int x, int y, int z)
{
  int t1 = x+y;
  int t2 = z+t1;
  int t3 = x+4;
  int t4 = y * 48;
  int t5 = t3 + t4;
  int rval = t2 * t5;
  return rval;
}
```




```
movl   8(%ebp), %ecx
movl   12(%ebp), %edx
leal   (%edx,%edx,2), %eax
sall   $4, %eax
leal   4(%ecx,%eax), %eax
addl   %ecx, %edx
addl   16(%ebp), %edx
imull  %edx, %eax
```

Understanding `arith`

```
int arith(int x, int y, int z)
{
  int t1 = x+y;
  int t2 = z+t1;
  int t3 = x+4;
  int t4 = y * 48;
  int t5 = t3 + t4;
  int rval = t2 * t5;
  return rval;
}
```




```
movl   8(%ebp), %ecx          # ecx = x
movl   12(%ebp), %edx         # edx = y
leal   (%edx,%edx,2), %eax    # eax = y*3
sall   $4, %eax               # eax *= 16 (t4)
leal   4(%ecx,%eax), %eax     # eax = t4 +x+4 (t5)
addl   %ecx, %edx             # edx = x+y (t1)
addl   16(%ebp), %edx         # edx += z (t2)
imull  %edx, %eax             # eax = t2 * t5 (rval)
```

Observations about `arith`

```
int arith(int x, int y, int z)
{
  int t1 = x+y;
  int t2 = z+t1;
  int t3 = x+4;
  int t4 = y * 48;
  int t5 = t3 + t4;
  int rval = t2 * t5;
  return rval;
}
```

- Instructions in different order from C code
- Some expressions require multiple instructions
- Some instructions cover multiple expressions
- Get exact same code when compile:
- `(x+y+z)*(x+4+48*y)`

```
movl   8(%ebp), %ecx          # ecx = x
movl   12(%ebp), %edx         # edx = y
leal   (%edx,%edx,2), %eax    # eax = y*3
sall   $4, %eax               # eax *= 16 (t4)
leal   4(%ecx,%eax), %eax     # eax = t4 +x+4 (t5)
addl   %ecx, %edx             # edx = x+y (t1)
addl   16(%ebp), %edx         # edx += z (t2)
imull  %edx, %eax             # eax = t2 * t5 (rval)
```

Another Example

```
int logical(int x, int y)
{
  int t1 = x^y;
  int t2 = t1 >> 17;
  int mask = (1<<13) - 7;
  int rval = t2 & mask;
  return rval;
}
```

```
logical:
    pushl %ebp            } Set
    movl %esp,%ebp        } Up

    movl 12(%ebp),%eax    }
    xorl 8(%ebp),%eax     } Body
    sarl $17,%eax         }
    andl $8185,%eax       }

    popl %ebp             } Finish
    ret                   }
```

```
movl 12(%ebp),%eax    # eax = y
xorl 8(%ebp),%eax     # eax = x^y        (t1)
sarl $17,%eax         # eax = t1>>17     (t2)
andl $8185,%eax       # eax = t2 & mask (rval)
```

Another Example

```c
int logical(int x, int y)
{
  int t1 = x^y;
  int t2 = t1 >> 17;
  int mask = (1<<13) - 7;
  int rval = t2 & mask;
  return rval;
}
```

```
logical:
    pushl %ebp
    movl %esp,%ebp

    movl 12(%ebp),%eax
    xorl 8(%ebp),%eax
    sarl $17,%eax
    andl $8185,%eax

    popl %ebp
    ret
```

Set Up

Body

Finish

```
movl 12(%ebp),%eax      # eax = y
xorl 8(%ebp),%eax       # eax = x^y        (t1)
sarl $17,%eax           # eax = t1>>17     (t2)
andl $8185,%eax         # eax = t2 & mask (rval)
```

Another Example

```c
int logical(int x, int y)
{
  int t1 = x^y;
  int t2 = t1 >> 17;
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  int rval = t2 & mask;
  return rval;
}
```

```
logical:
    pushl %ebp
    movl %esp,%ebp

    movl 12(%ebp),%eax
    xorl 8(%ebp),%eax
    sarl $17,%eax
    andl $8185,%eax

    popl %ebp
    ret
```

Set Up

Body

Finish

```
movl 12(%ebp),%eax    # eax = y
xorl 8(%ebp),%eax     # eax = x^y        (t1)
sarl $17,%eax         # eax = t1>>17     (t2)
andl $8185,%eax       # eax = t2 & mask (rval)
```

Another Example

```
int logical(int x, int y)
{
  int t1 = x^y;
  int t2 = t1 >> 17;
  int mask = (1<<13) - 7;
  int rval = t2 & mask;
  return rval;
}
```

$2^{13} = 8192$, $2^{13} - 7 = 8185$

```
logical:
    pushl %ebp
    movl %esp,%ebp

    movl 12(%ebp),%eax
    xorl 8(%ebp),%eax
    sarl $17,%eax
    andl $8185,%eax

    popl %ebp
    ret
```

Set Up

Body

Finish

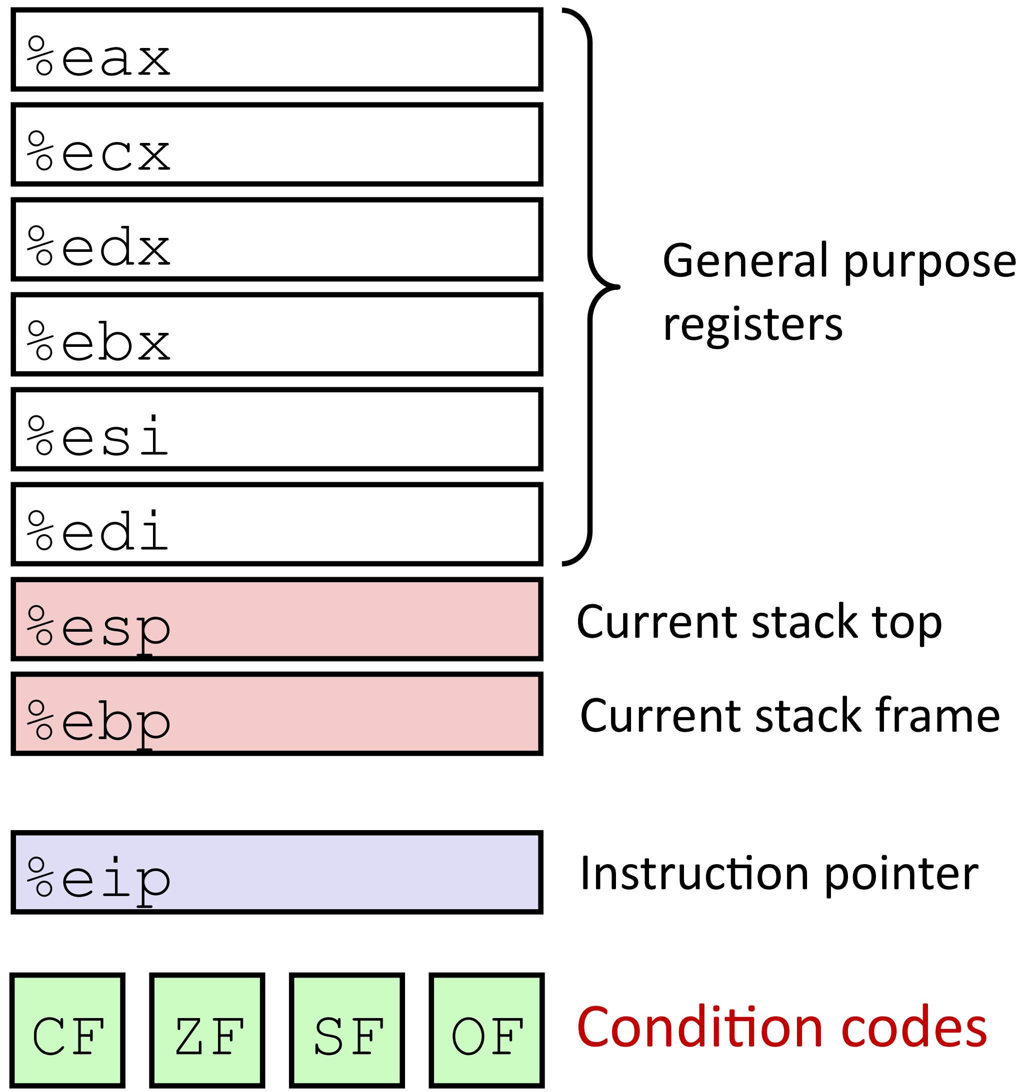
```
movl 12(%ebp),%eax      # eax = y
xorl 8(%ebp),%eax       # eax = x^y          (t1)
sarl $17,%eax           # eax = t1>>17       (t2)
andl $8185,%eax         # eax = t2 & mask (rval)
```

Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- **Control: Condition codes**
- Conditional branches
- Loops

Processor State (IA32, Partial)

- **Information about currently executing program**
  - Temporary data
    (`%eax`, …)
  - Location of runtime stack
    (`%ebp`,`%esp`)
  - Location of current code control point
    (`%eip`, …)
  - Status of recent tests
    (CF, ZF, SF, OF)



Condition Codes (Implicit Setting)

- **Single bit registers**
  - CF Carry Flag (for unsigned) SF Sign Flag (for signed)
  - ZF Zero Flag OF Overflow Flag (for signed)
- **Implicitly set (think of it as side effect) by arithmetic operations**

  Example: `addl/addq` Src,Dest ↔ `t = a+b`

  CF set if carry out from most significant bit (unsigned overflow)

  ZF set if `t == 0`

  SF set if `t < 0` (as signed)

  OF set if two's-complement (signed) overflow

  `(a>0 && b>0 && t<0) || (a<0 && b<0 && t>=0)`
- **Not set by `lea` instruction**
- **Full documentation (IA32), link on course website**

Condition Codes (Explicit Setting: Compare)

- **Explicit Setting by Compare Instruction**
  - `cmpl/cmpq` Src2, Src1
  - `cmpl b,a` like computing `a-b` without setting destination

  - CF set if carry out from most significant bit (used for unsigned comparisons)
  - ZF set if `a == b`
  - SF set if `(a-b) < 0` (as signed)
  - OF set if two's-complement (signed) overflow
  `(a>0 && b<0 && (a-b)<0) || (a<0 && b>0 && (a-b)>0)`

Condition Codes (Explicit Setting: Test)

- **Explicit Setting by Test instruction**
  - `testl`/`testq` Src2, Src1

    `testl b,a` like computing `a&b` without setting destination

  - Sets condition codes based on value of Src1 & Src2
  - Useful to have one of the operands be a mask

  - ZF set when `a&b == 0`
  - SF set when `a&b < 0`

Reading Condition Codes

- **SetX Instructions**
  - Set low-order byte to 0 or 1 based on combinations of condition codes
  - Does not alter remaining 3 bytes

SetX	Condition	Description
`sete`	`ZF`	Equal / Zero
`setne`	`~ZF`	Not Equal / Not Zero
`sets`	`SF`	Negative
`setns`	`~SF`	Nonnegative
`setg`	`~(SF^OF)&~ZF`	Greater (Signed)
`setge`	`~(SF^OF)`	Greater or Equal (Signed)
`setl`	`(SF^OF)`	Less (Signed)
`setle`	`(SF^OF)|ZF`	Less or Equal (Signed)
`seta`	`~CF&~ZF`	Above (unsigned)
`setb`	`CF`	Below (unsigned)

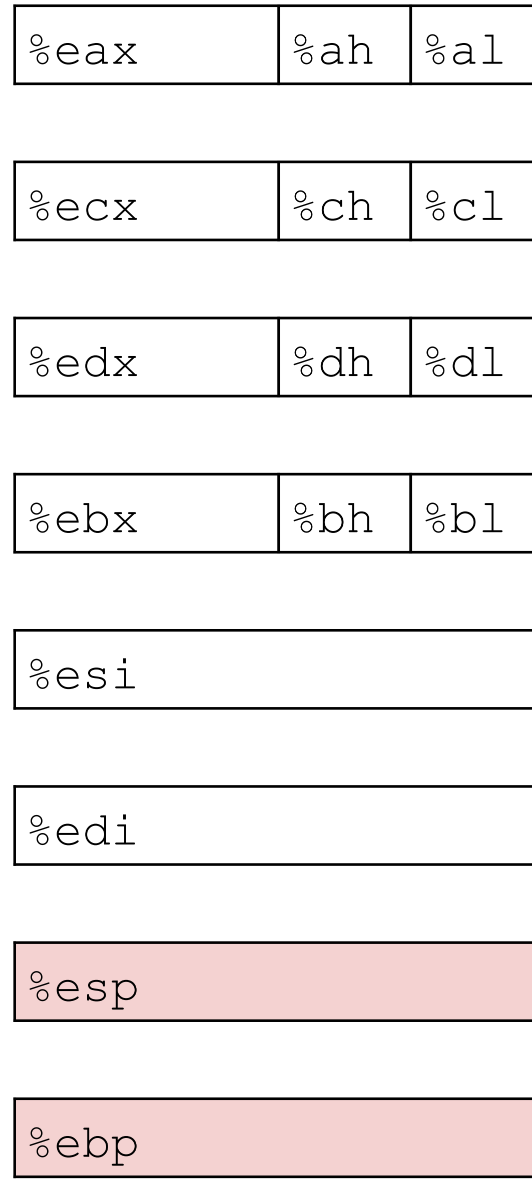
Reading Condition Codes (Cont.)

- **SetX Instructions:**
  - Set single byte based on combination of condition codes
- **One of 8 addressable byte registers**
  - Does not alter remaining 3 bytes
  - Typically use `movzbl` to finish job

```
int gt (int x, int y)
{
  return x > y;
}
```

Body

```
movl 12(%ebp),%eax    # eax = y
cmpl %eax,8(%ebp)     # Compare x : y
setg %al              # al = x > y
movzbl %al,%eax       # Zero rest of %eax
```



Reading Condition Codes: x86-64

- **SetX Instructions:**
  - Set single byte based on combination of condition codes
  - Does not alter remaining 3 bytes

```
int gt (long x, long y)
{
  return x > y;
}
```

```
long lgt (long x, long y)
{
  return x > y;
}
```

Bodies

```
cmpl %esi, %edi
setg %al
movzbl %al, %eax
```

```
cmpq %rsi, %rdi
setg %al
movzbl %al, %eax
```

Is `%rax` zero?

Yes: 32-bit instructions set high order 32 bits to 0!

Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- x86-64
- Control: Condition codes
- **Conditional branches & Moves**
- Loops

Jumping

- **jX Instructions**
  - Jump to different part of code depending on condition codes

jX	Condition	Description
`jmp`	`1`	Unconditional
`je`	`ZF`	Equal / Zero
`jne`	`~ZF`	Not Equal / Not Zero
`js`	`SF`	Negative
`jns`	`~SF`	Nonnegative
`jg`	`~(SF^OF)&~ZF`	Greater (Signed)
`jge`	`~(SF^OF)`	Greater or Equal (Signed)
`jl`	`(SF^OF)`	Less (Signed)
`jle`	`(SF^OF)|ZF`	Less or Equal (Signed)
`ja`	`~CF&~ZF`	Above (unsigned)
`jb`	`CF`	Below (unsigned)

Conditional Branch Example

```
int absdiff(int x, int y)
{
    int result;
    if (x > y) {
      result = x-y;
    } else {
      result = y-x;
    }
    return result;
}
```

```
absdiff:
    pushl   %ebp                 Setup
    movl    %esp, %ebp
    movl    8(%ebp), %edx        Body1
    movl    12(%ebp), %eax
    cmpl    %eax, %edx
    jle     .L6
    subl    %eax, %edx           Body2a
    movl    %edx, %eax
    jmp .L7
.L6:
    subl %edx, %eax              Body2b
.L7:
    popl %ebp                    Finish
    ret
```

Conditional Branch Example (Cont.)

```c
int goto_ad(int x, int y)
{
  int result;
  if (x <= y) goto Else;
  result = x-y;
  goto Exit;
Else:
  result = y-x;
Exit:
  return result;
}
```

```
absdiff:
    pushl   %ebp               Setup
    movl    %esp, %ebp
    movl    8(%ebp), %edx
    movl    12(%ebp), %eax
    cmpl    %eax, %edx         Body1
    jle     .L6
    subl    %eax, %edx
    movl    %edx, %eax         Body2a
    jmp .L7
.L6:
    subl %edx, %eax            Body2b
.L7:
    popl %ebp
    ret                        Finish
```

- **C allows "goto" as means of transferring control**
  - Closer to machine-level programming style
- **Generally considered bad coding style**

Conditional Branch Example (Cont.)

```
int goto_ad(int x, int y)
{
  int result;
  if (x <= y) goto Else;
  result = x-y;
  goto Exit;
Else:
  result = y-x;
Exit:
  return result;
}
```

```
absdiff:
    pushl   %ebp                 Setup
    movl    %esp, %ebp
    movl    8(%ebp), %edx        Body1
    movl    12(%ebp), %eax
    cmpl    %eax, %edx
    jle     .L6
    subl    %eax, %edx           Body2a
    movl    %edx, %eax
    jmp .L7
.L6:
    subl %edx, %eax              Body2b
.L7:
    popl %ebp                    Finish
    ret
```

Conditional Branch Example (Cont.)

```
int goto_ad(int x, int y)
{
  int result;
  if (x <= y) goto Else;
  result = x-y;
  goto Exit;
Else:
  result = y-x;
Exit:
  return result;
}
```

```
absdiff:
    pushl   %ebp            } Setup
    movl    %esp, %ebp
    movl    8(%ebp), %edx   } Body1
    movl    12(%ebp), %eax
    cmpl    %eax, %edx
    jle     .L6
    subl    %eax, %edx      } Body2a
    movl    %edx, %eax
    jmp .L7
.L6:
    subl %edx, %eax         } Body2b
.L7:
    popl %ebp               } Finish
    ret
```

Conditional Branch Example (Cont.)

```
int goto_ad(int x, int y)
{
  int result;
  if (x <= y) goto Else;
  result = x-y;
  goto Exit;
Else:
  result = y-x;
Exit:
  return result;
}
```

```
absdiff:
    pushl   %ebp
    movl    %esp, %ebp                Setup
    movl    8(%ebp), %edx
    movl    12(%ebp), %eax
    cmpl    %eax, %edx
    jle     .L6                       Body1
    subl    %eax, %edx
    movl    %edx, %eax                Body2a
    jmp .L7
.L6:
    subl %edx, %eax                   Body2b
.L7:
    popl %ebp                         Finish
    ret
```

General Conditional Expression Translation

C Code

```
val = Test ? Then_Expr : Else_Expr;
```

```
val = x>y ? x-y : y-x;
```

Goto Version

```
  nt = !Test;
  if (nt) goto Else;
  val = Then_Expr;
  goto Done;
Else:
  val = Else_Expr;
Done:
  . . .
```

- Test is expression returning integer
  - = 0 interpreted as false
  - ≠ 0 interpreted as true
- Create separate code regions for then & else expressions
- Execute appropriate one

Using Conditional Moves

- **Conditional Move Instructions**
  - Instruction supports:

    if (Test) Dest ← Src
  - Supported in post-1995 x86 processors
  - GCC does not always use them
    - Wants to preserve compatibility with ancient processors
    - Enabled for x86-64
    - Use switch `-march=686` for IA32
- **Why?**
  - Branches are very disruptive to instruction flow through pipelines
  - Conditional move do not require control transfer

C Code

```
val = Test
    ? Then_Expr
    : Else_Expr;
```

Goto Version

```
  tval = Then_Expr;
  result = Else_Expr;
  t = Test;
  if (t) result = tval;
  return result;
```

Conditional Move Example: x86-64

```
int absdiff(int x, int y)  {
    int result;
    if (x > y) {
        result = x-y;
    } else {
        result = y-x;
    }
    return result;
}
```

x in %edi

y in %esi

```
absdiff:
  movl    %edi, %edx
  subl    %esi, %edx   # tval = x-y
  movl    %esi, %eax
  subl    %edi, %eax   # result = y-x
  cmpl    %esi, %edi   # Compare x:y
  cmovg   %edx, %eax   # If >, result = tval
  ret
```

Bad Cases for Conditional Move

Expensive Computations

```
val = Test(x) ? Hard1(x) : Hard2(x);
```

- **Both values get computed**
- **Only makes sense when computations are very simple**

Risky Computations

```
val = p ? *p : 0;
```

- Both values get computed
- May have undesirable effects

Computations with side effects

```
val = x > 0 ? x*=7 : x+=3;
```

- Both values get computed
- Must be side-effect free

Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- x86-64
- Control: Condition codes
- Conditional branches and moves
- **Loops**

"Do-While" Loop Example

C Code

```
int pcount_do(unsigned x)
{
  int result = 0;
  do {
    result += x & 0x1;
    x >>= 1;
  } while (x);
  return result;
}
```

Goto Version

```
int pcount_do(unsigned x)
{
  int result = 0;
loop:
  result += x & 0x1;
  x >>= 1;
  if (x)
    goto loop;
  return result;
}
```

- **Count number of 1's in argument x ("popcount")**
- **Use conditional branch to either continue looping or to exit loop**

"Do-While" Loop Compilation

Goto Version

```
int pcount_do(unsigned x)  {
  int result = 0;
loop:
  result += x & 0x1;
  x >>= 1;
  if (x)
    goto loop;
  return result;
}
```

- **Registers:**

%edx	x
%ecx	result

```
  movl   $0, %ecx      #   result = 0
.L2:                   # loop:
  movl   %edx, %eax
  andl   $1, %eax      #   t = x & 1
  addl   %eax, %ecx    #   result += t
  shrl   %edx          #   x >>= 1
  jne    .L2           #   If !0, goto loop
```

General "Do-While" Translation

C Code

```
do
   Body
   while (Test);
```

Goto Version

```
loop:
   Body
   if (Test)
      goto loop
```

- **Body:**
```
{
   Statement1;
   Statement2;
     …
   Statementn;
}
```

- **Test returns integer**
  - = 0 interpreted as false
  - ≠ 0 interpreted as true

"While" Loop Example

C Code

```
int pcount_while(unsigned x) {
  int result = 0;
  while (x) {
    result += x & 0x1;
    x >>= 1;
  }
  return result;
}
```

Goto Version

```
int pcount_do(unsigned x)  {
  int result = 0;
  if (!x) goto done;
loop:
  result += x & 0x1;
  x >>= 1;
  if (x)
    goto loop;
done:
  return result;
}
```

- **Is this code equivalent to the do-while version?**

General "While" Translation

While version

```
while (Test)
  Body
```

Do-While Version

```
  if (!Test)
    goto done;
  do
    Body
    while(Test);
done:
```

Goto Version

```
  if (!Test)
    goto done;
loop:
  Body
  if (Test)
    goto loop;
done:
```

"For" Loop Example

C Code

```
#define WSIZE 8*sizeof(int)
int pcount_for(unsigned x) {
  int i;
  int result = 0;
  for (i = 0; i < WSIZE; i++) {
    unsigned mask = 1 << i;
    result += (x & mask) != 0;
  }
  return result;
}
```

- Is this code equivalent to other versions?

"For" Loop Form

General Form

```
for (Init; Test; Update )

    Body
```

```
for (i = 0; i < WSIZE; i++) {
    unsigned mask = 1 << i;
    result += (x & mask) != 0;
  }
```

Init

```
i = 0
```

Test

```
i < WSIZE
```

Update

```
i++
```

Body

```
{
  unsigned mask = 1 << i;
  result += (x & mask) != 0;
}
```

"For" Loop → While Loop

For Version

```
for (Init; Test; Update )

    Body
```

While Version

```
Init;

while (Test ) {

    Body

    Update;

}
```

"For" Loop → … → Goto

For Version

```
for (Init; Test; Update )
    Body
```

While Version

```
Init;
while (Test ) {
    Body
    Update;
}
```

```
  Init;
  if (!Test)
    goto done;
  do
    Body
    Update
  while(Test);
done:
```

```
  Init;
  if (!Test)
    goto done;
loop:
  Body
  Update
  if (Test)
    goto loop;
done:
```

"For" Loop Conversion Example

Goto Version

C Code

```
#define WSIZE 8*sizeof(int)
int pcount_for(unsigned x) {
  int i;
  int result = 0;
  for (i = 0; i < WSIZE; i++) {
    unsigned mask = 1 << i;
    result += (x & mask) != 0;
  }
  return result;
}
```

```
int pcount_for_gt(unsigned x) {
  int i;
  int result = 0;
  i = 0;
  if (!(i < WSIZE))
    goto done;
 loop:
  {
    unsigned mask = 1 << i;
    result += (x & mask) != 0;
  }
  i++;
  if (i < WSIZE)
    goto loop;
 done:
  return result;
}
```

Init

! Test

Body

Update

Test

- Initial test can be optimized away

Summary

- **Today**
  - Complete addressing mode, address computation (`leal`)
  - Arithmetic operations
  - Control: Condition codes
  - Conditional branches & conditional moves
  - Loops
- **Next Time**
  - Switch statements
  - Stack
  - Call / return
  - Procedure call discipline