Recitation 15

PASL

15.1 Announcements

- PASLLab is due Friday afternoon.
- We will likely be having a final review sometime on Wednesday, May 4. Keep your ears open for more details.
- The final exam is on Friday, May 6, 1:00-4:00pm.

15.2 map_flatten

Let's begin by downloading the files rec15.hpp and rec15-bench.cpp. You can put these in the top directory of PASLLab. Then, edit PASLLab's Makefile to add rec15-bench.cpp to the list of programs, i.e.

```
PROGRAMS=\
   sandbox.cpp \
   check.cpp \
   bench.cpp \
   rec15-bench.cpp # add me here.
   # don't forget the slash on the previous line.
```

Task 15.1. Using PASL primitives, implement the function

where, at a high-level, the goal is to compute

```
flatten \langle f(x) : x \in xs \rangle.
```

You should assume that the function arguments are typed as follows, where f(xs[i]) is a pointer to the front of an array of length g(xs[i]).

```
f: value\_type \rightarrow value\_type*
g: value\_type \rightarrow long
```

The first step is to determine the offsets of the subarrays in the output. We can compute this by mapping g across the input followed by a plus-scan. Note that we're using the fusioned form of scan_excl here, which performs a map for us.

```
auto plus = [] (value_type a, value_type b) { return a + b; };
auto offsets = scan_excl(plus, g, 01, xs);
```

The output of a scan_excl is a struct containing two fields, partials and total. The former is an sparray the same length as the input which contains each exclusive prefix sum, while the latter is the sum of the entire input. Therefore we can go ahead and allocate the result array, since we know its length.

```
sparray result = sparray(offsets.total);
```

Next, we'd like to map f across the input to discover each subarray, then write these subarrays to result. This can be accomplished with two nested parallel_for loops. So, we'll need to declare two granularity controllers (for now, lets just call these C1 and C2). After this step, we simply return the result array.

```
par::parallel_for(C1, OL, xs.size(), [&] (long i) {
  value_type* elems = f(xs[i]);
  par::parallel_for(C2, OL, g(xs[i]), [&] (long j) {
    result[offsets.partials[i] + j] = elems[j];
  });
});
```

Note that parallel_for assumes that the code body given to it is constant-time, which is not true for the outer loop. So, we need to write a complexity function. The complexity function given to a parallel_for is assumed to take two parameters which describe a range of iterations of the for-loop, and return the complexity of that entire range. Note that any particular iteration i of our loop has a complexity of g(xs[i]), but in general, a range of iterations $[\ell, h)$ has complexity

$$\sum_{i=\ell}^{h-1} \mathsf{g}\left(\mathsf{xs}\left[i\right]\right).$$

These ranges can be easily calculated using the output of the scan we computed earlier. Our complexity function therefore looks like the following:

The completed code is given below.

Algorithm 15.2. map_flatten in PASL loop_controller_type C1("map_flatten_1"); loop_controller_type C2("map_flatten_2"); template <class Map func, class Size func> sparray map_flatten(const Map_func& f, const Size_func& g, const sparray& xs) { long n = xs.size();auto plus = [] (value_type a, value_type b) { return a + b; }; auto offsets = scan_excl(plus, q, OL, xs); sparray result = sparray(offsets.total); auto complexity = [&] (long lo, long hi) { long upper = (hi == n) ? offsets.total : offsets.partials[hi]; return upper - offsets.partials[lo]; par::parallel_for (C1, complexity, OL, n, [&] (long i) { value_type* elems = f(xs[i]); par::parallel_for (C2, OL, g(xs[i]), [&] (long j) { result[offsets.partials[i] + j] = elems[j]; }); }); return result;

Remark 15.3. These controller declarations are technically not correct. We should really templatize the controllers over the classes Map_func and Size_func, just as map_flatten is. You can find examples of these kinds of declarations in the sparray.hpp source file.

Remark 15.4. Some of the techniques used here may also be useful when implementing BFS in PASLLab. Feel free to reuse any code from this recitation, although you may want to make some modifications...

15.3. INJECT 85

15.3 inject

Throughout the semester, we've largely kept the sequence function inject shrouded in mystery. Let's see how the magic works!

Task 15.5. Using PASL, implement the function

which returns the result of injecting into xs. We require that indices and updates be the same length, such that for each i, we attempt to write updates [i] at position indices [i] in xs. Note that you should not destructively modify xs.

If there are multiple updates specified at the same position, then all except the last should be ignored. (We want to match the behavior of inject as specified in the 15210 Library.)

Let's step back for a moment and review the *compare-and-swap* (CAS) operation. Given a memory location ℓ and two values x and y, this operation atomically performs the following:

- 1. Compare x against the contents of the memory location ℓ .
- 2. If they are equal, write y at ℓ and return true.
- 3. Otherwise, return false.

A simple extension of CAS is called a *priority update*¹. This operation takes a memory location ℓ and a value y and attempts to write y at ℓ , but only if y is "greater than" the current value stored at ℓ (we write "greater than" in quotes because we could really use any comparison function). We can implement a priority update as follows:

- 1. Load the contents of ℓ into x.
- 2. While y > x:
 - (a) If $CAS(\ell, x, y)$ then return.
 - (b) Otherwise, load the contents of ℓ into x.

Priority updates allow multiple threads to converge upon some "maximum" value stored at a shared memory location. We can use this for inject. If m is the number of updates, the general idea is this: for each $0 \le i < m$, perform a priority update at a location temp [indices [i]]

¹See http://www.eecs.berkeley.edu/~jshun/contention.pdf

where we attempt to write i. Notice that the largest i will be the last thing written at this location. For each position in the output, this effectively chooses which update will be written at that position.

The full code is shown below. Note that we allocate and initialize the temp array by filling it with invalid indices, to detect which positions in the output will not change from the input. We implement compare-and-swap using the builtin compare_exchange_strong operation provided by the C++ std::atomic class. This function is slightly different than the pseudocode given above. Specifically,

```
\ell.compare_exchange_strong(x,y)
```

requires that x is a reference. If the CAS fails, then the contents of ℓ will be written into x.

```
Algorithm 15.6. inject in PASL.
loop_controller_type C3("inject_contr_1");
loop_controller_type C4("inject_contr_2");
sparray inject(const sparray& xs,
               const sparray& indices,
               const sparray& updates) {
  long n = xs.size();
  long m = updates.size(); // must be equal to indices.size()
 const long NO_UPDATE = -1L;
  auto temp = my_malloc<std::atomic<long>>(n);
  par::parallel_for (C3, OL, n, [&] (long i) {
    temp[i].store(NO_UPDATE);
  });
  par::parallel_for (C4, OL, m, [&] (long i) {
   std::atomic<long>& cell = temp[indices[i]];
    long curr = cell.load();
    // below, curr is updated if the CAS fails
   while (i > curr && !cell.compare_exchange_strong(curr, i))
  });
  sparray result = tabulate([&] (long i) {
    long idx = temp[i].load();
    return idx == NO_UPDATE ? xs[i] : updates[idx];
  }, n);
 free (temp);
  return result;
```

15.4. BENCHMARKING 87

15.4 Benchmarking

Try running some speedup experiments! The two bench arguments are map_flatten and inject, respectively. For example, the following injects m randomly placed updates into an array length n. In the map_flatten benchmark, n is the initial array size, and m is the size of each subarray (so the output is length nm).

```
make rec15-bench.opt rec15-bench.baseline

./prun speedup -baseline "./rec15-bench.baseline" \
-parallel "./rec15-bench.opt -proc 1,5,10,15,20" \
-bench inject -n 100000,10000000 -m 100000000,200000000

./pplot speedup -series n,m
```