## 15-462 Computer Graphics I

Lecture 15

## Image Processing

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Blending
Display Color Models
Filters
Dithering
Image Compression
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## Blending

- Frame buffer
- Simple color model: R, G, B; 8 bits each
- $\alpha$-channel A, another 8 bits
- Alpha determines opacity, pixel-by-pixel
$-\alpha=1$ : opaque
$-\alpha=0$ : transparent
- Blend translucent objects during rendering
- Achieve other effects (e.g., shadows)


## Image Compositing

- Compositing operation
- Source: $\mathbf{s}=\left[\begin{array}{llll}s_{r} & s_{g} & s_{b} & s_{a}\end{array}\right]$
- Destination: $\mathbf{d}=\left[\begin{array}{llll}d_{r} & d_{g} & d_{b} & d_{a}\end{array}\right]$
$-\boldsymbol{b}=\left[\begin{array}{llll}b_{r} & b_{g} & b_{b} & b_{a}\end{array}\right]$ source blending factors
$-\mathbf{c}=\left[\begin{array}{llll}c_{r} & c_{g} & c_{b} & c_{a}\end{array}\right]$ destination blending factors
$-d^{\prime}=\left[b_{r} s_{r}+c_{r} d_{r} b_{g} s_{g}+c_{g} d_{g} b_{b} s_{b}+c_{b} d_{b} b_{a} s_{a}+c_{a} d_{a}\right]$
- Overlay $n$ images with equal weight
- Set $\alpha$-value for each pixel in each image to $1 / n$
- Source blending factor is " $\alpha$ "
- Destination blending factor is "1"


## Blending in OpenGL

- Enable blending
gIEnable(GL_BLEND);
- Set up source and destination factors
gIBlendFund(source_factor, dest_factor);
- Source and destination choices
- GL_ONE, GL_ZERO
- GL_SRC_ALPHA, GL_ONE_MINUS_SRC_ALPHA
- GL_DST_ALPHA, GL_ONE_MINUS_DST_ALPHA


## Blending Errors

- Operations are not commutative
- Operations are not idempotent
- Interaction with hidden-surface removal
- Polygon behind opaque one should be culled
- Translucent in front of others should be composited
- Solution: make z-buffer read-only for translucent polygons with glDepthMask(GL_FALSE);


## Antialiasing Revisited

- Single-polygon case first
- Set $\alpha$-value of each pixel to covered fraction
- Use destination factor of "1- $\alpha$ "
- Use source factor of " $\alpha$ "
- This will blend background with foreground
- Overlaps can lead to blending errors


## Antialiasing with Multiple Polygons

- Initially, background color $\mathbf{C}_{0}, \alpha_{0}=0$
- Render first polygon; color $\mathrm{C}_{1}$ fraction $\alpha_{1}$
$-\mathbf{C}_{\mathrm{d}}=\left(1-\alpha_{1}\right) \mathbf{C}_{0}+\alpha_{1} \mathbf{C}_{1}$
- $\alpha_{d}=\alpha_{1}$
- Render second polygon; assume fraction $\alpha_{2}$
- If no overlap (a), then
$-\mathbf{C}_{\mathrm{d}}^{\prime}=\left(1-\alpha_{2}\right) \mathbf{C}_{\mathrm{d}}+\alpha_{2} \mathbf{C}_{2}$
$-\alpha_{d}^{\prime}=\alpha_{1}+\alpha_{2}$


## Antialiasing with Overlap

- Now assume overlap (b)
- Average overlap is $\alpha_{1} \alpha_{2}$
- So $\alpha_{d}=\alpha_{1}+\alpha_{2}-\alpha_{1} \alpha_{2}$
- Make front/back decision for color as usual



## Antialiasing in OpenGL

- Avoid explicit $\alpha$-calculation in program
- Enable both smoothing and blending
gIEnable(GL_POINT_SMOOTH);
gIEnable(GL_LINE_SMOOTH);
gIEnable(GL_BLEND);
gIBlendFunc(GL_SRC_ALPHA, GL_ONE_MINUS_SRC_ALPHA);


## Outline

- Blending
- Display Color Models
- Filters
- Dithering
- Image Compression


## Displays and Framebuffers

- Image stored in memory as 2D pixel array, called framebuffer
- Value of each pixel controls color
- Video hardware scans the framebuffer at 60 Hz
- Depth of framebuffer is information per pixel
- 1 bit: black and white display (cf. Smithsonian)
-8 bit: 256 colors at any given time via colormap
-16 bit: 5, 6,5 bits (R,G,B), $2^{16}=65,536$ colors
-24 bit: $8,8,8$ bits (R,G,B), $2^{24}=16,777,216$ colors


## Fewer Bits: Colormaps

- Colormaps typical for 8 bit framebuffer depth
- With screen 1024 * $768=786432=0.75 \mathrm{MB}$
- Each pixel value is index into colormap
- Colormap is array of RGB values, 8 bits each
- All $2^{24}$ colors can be represented
- Only $2^{8}=256$ at a time
- Poor approximation of full color
- Who owns the colormap?
- Colormap hacks: affect image w/o changing framebuffer (only colormap)


## More Bits: Graphics Hardware

- 24 bits: RGB
-     + 8 bits: A ( $\alpha$-channel for opacity)
-     + 16 bits: $Z$ (for hidden-surface removal)
-     * 2: double buffering for smooth animation
- = 96 bits
- For 1024 * 768 screen: 9 MB


## Image Processing

- 2D generalization of signal processing
- Image as a two-dimensional signal
- Point processing: modify pixels independently
- Filtering: modify based on neighborhood
- Compositing: combine several images
- Image compression: space-efficient formats
- Other topics (not in this course)
- Image enhancement and restoration
- Computer vision


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## Point Processing

- Input: $a(x, y)$; Output: $b(x, y)=f(a(x, y))$
- Useful for contrast adjustment, false colors
- Examples for grayscale, $0 \leq \mathrm{v} \leq 1_{f(v)}$
$-f(v)=v$ (identity)
$-f(v)=1-v$ (negate image)
$-f(v)=v^{p}, p<1$ (brighten)
$-f(v)=v^{p}, p>1$ (darken)
- Gamma correction compensates monitor brightness loss


## Gamma Correction Example

$\Gamma=1.0 ; f(v)=v$

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$\Gamma=0.5 ; f(v)=v^{1 / 0.5}=v^{2} \quad \Gamma=2.5 ; f(v)=v^{1 / 2.5}=v^{0.4}$

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## Signals and Filtering

- Audio recording is 1D signal: amplitude(t)
- Image is a 2D signal: color( $\mathrm{x}, \mathrm{y}$ )
- Signals can be continuous or discrete
- Raster images are discrete
- In space: sampled in $x$, $y$
- In color: quantized in value
- Filtering: a mapping from signal to signal


## Linear and Shift-Invariant Filters

- Linear with respect to input signal
- Shift-invariant with respect to parameter
- Convolution in 1D
$\begin{aligned} & -\mathrm{a}(\mathrm{t}) \text { is input signal } \\ & -\mathrm{b}(\mathrm{s}) \text { is output signal }\end{aligned} \quad b(s)=\sum_{t=-\infty}^{+\infty} a(t) h(s-t)$
- $\mathrm{h}(\mathrm{u})$ is filter
- Shorthand: $\mathrm{b}=\mathrm{a} \quad \mathrm{h}$ ( $=\mathrm{h} \quad \mathrm{a}$, as an aside)
- Convolution in 2D

$$
b(x, y)=\sum_{u=-\infty}^{+\infty} \sum_{v=-\infty}^{+\infty} a(u, v) h(x-u, y-v)
$$

## Filters with Finite Support

- Filter $h(u, v)$ is 0 except in given region
- Represent h in form of a matrix
- Example: $3 \times 3$ blurring filter
$\begin{array}{rll}b(x, y)=\frac{1}{9} & \begin{array}{lll}(a(x-1, y-1) & +a(x, y-1) & +a(x+1, y-1) \\ & +a(x-1, y) & +a(x, y) \\ & +a(x+1, y) \\ & +a(x-1, y+1) & +a(x, y+1) \\ & +a(x+1, y+1))\end{array}\end{array}$
- As function

$$
h(u, v)= \begin{cases}\frac{1}{9} & \text { if }-1 \leq u, v \leq 1 \\ 0 & \text { otherwise }\end{cases}
$$

- In matrix form

$$
\frac{1}{9}\left[\begin{array}{lll}
1 & 1 & 1 \\
1 & 1 & 1 \\
1 & 1 & 1
\end{array}\right]
$$

## Blurring Filters

- Average values of surrounding pixels
- Can be used for anti-aliasing
- Size of blurring filter should be odd
- What do we do at the edges and corners?
- For noise reduction, use median, not average
- Eliminates intensity spikes
- Non-linear filter


## Examples of Blurring Filter

Pictures have been removed for printing purposes due to a PowerPoint bug

## Example Noise Reduction

Pictures have been removed for printing due to a PowerPoint bug

## Edge Filters

- Discover edges in image
- Characterized by large gradient

$$
\nabla a=\left[\frac{\partial a}{\partial x} \frac{\partial a}{\partial y}\right], \quad|\nabla a|=\sqrt{\left(\frac{\partial a}{\partial x}\right)^{2}+\left(\frac{\partial a}{\partial y}\right)^{2}}
$$

- Approximate square root

$$
|\nabla a| \approx\left|\frac{\partial a}{\partial x}\right|+\left|\frac{\partial a}{\partial y}\right|
$$

- Approximate partial derivatives, e.g.

$$
\frac{\partial a}{\partial x} \approx a(x+1)-a(x-1)
$$

## Sobel Filter

- Edge detection filter, with some smoothing
- Approximate

$$
\frac{\partial}{\partial x} \approx\left[\begin{array}{lll}
-1 & 0 & 1 \\
-2 & 0 & 2 \\
-1 & 0 & 1
\end{array}\right], \quad \frac{\partial}{\partial y} \approx\left[\begin{array}{ccc}
1 & 2 & 1 \\
0 & 0 & 0 \\
-1 & -2 & -1
\end{array}\right]
$$

- Sobel filter is non-linear
- Square and square root (more exact computation)
- Absolute value (faster computation)


## Sample Filter Computation

- Part of Sobel filter, detects vertical edges

a

b


# Example of Edge Filter 

Images have been removed due to a PowerPoint bug

Original image Edge filter, then brightened

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## Dithering

- Compensates for lack of color resolution
- Give up spatial resolution for color resolution
- Eye does spatial averaging
- Black/white dithering to achieve gray scale
- Each pixel is black or white
- From far away, color determined by fraction of white
- For $3 \times 3$ block, 10 levels of gray scale



## Halftone Screens

- Regular patterns create some artefacts
- Avoid stripes
- Avoid isolated pixels (e.g. on laser printer)
- Monotonicity: keep pixels on at higher intensities
- Example of good $3 \times 3$ dithering matrix
- For intensity n , turn on pixels $0 . . \mathrm{n}-1$

$$
\left[\begin{array}{lll}
6 & 8 & 4 \\
1 & 0 & 3 \\
5 & 2 & 7
\end{array}\right]
$$

## Floyd-Steinberg Error Diffusion

- Approximation without fixed resolution loss
- Scan in raster order
- At each pixel, draw least error output value
- Divide error into 4 different fractions
- Add the error fractions into adjacent, unwritten pixels



## Floyd-Steinberg Example

Images have been removed due to a PowerPoint bug

Gray Scale Ramp
-Some worms
-Some checkerboards
-Enhance edges

## Color Dithering

- Example: 8 bit framebuffer
- Set color map by dividing 8 bits into 3,3,2 for RGB
- Blue is deemphasized since we see it less well
- Dither RGB separately
- Works well with Floyd-Steinberg
- Assemble results into 8 bit index into colormap
- Generally looks good


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## Image Compression

- Exploit redundancy
- Coding: some pixel values more common
- Interpixel: adjacent pixels often similar
- Psychovisual: some color differences imperceptible
- Distinguish lossy and lossless methods


## Some Image File Formats

|  | Depth | File Size | Comments |
| :--- | :--- | :--- | :--- |
| JPEG | 24 | Small | Lossy compression |
| TIFF | 8,24 | Medium | Good general purpose |
| GIF | $1,4,8$ | Medium | Popular, but 8 bit |
| PPM | 24 | Big | Easy to read/write |
| EPS | $1,2,4,8,24$ | Huge | Good for printing |

## Image Sizes

- 1024*1024 at 24 bits uses 3 MB
- Encyclopedia Britannica at 300 pixels/inch and 1 bit/pixes requires 25 gigabytes ( 25 K pages)
- 90 minute movie at $640 \times 480,24$ bits per pixels, 24 frames per second requires 120 gigabytes
- Applications: HDTV, DVD, satellite image transmission, medial image processing, fax, ...


## Exploiting Coding Redundancy

- Not limited to images (text, other digital info)
- Exploit nonuniform probabilities of symbols
- Entropy as measure of information content
$-\mathrm{H}=-\Sigma_{\mathrm{i}} \operatorname{Prob}\left(\mathrm{s}_{\mathrm{i}}\right) \log _{2}\left(\operatorname{Prob}\left(\mathrm{~s}_{\mathrm{i}}\right)\right)$
- If source is independent random variable need H bits
- Idea:
- More frequent symbols get shorter code strings
- Best with high redundancy (= low entropy)
- Common algorithms
- Huffman coding
- LZW coding (gzip)


## Huffman Coding

- Codebook is precomputed and static
- Use probability of each symbol to assign code
- Map symbol to code
- Store codebook and code sequence
- Precomputation is expensive
- What is "symbol" for image compression?


## Lempel-Ziv-Welch (LZW) Coding

- Compute codebook on the fly
- Fast compression and decompression
- Can tune various parameters
- Both Huffman and LZW are lossless


## Exploiting Interpixel Redundancy

- Neighboring pixels are correlated
- Spatial methods for low-noise image
- Run-length coding:
- Alternate values and run-length
- Good if horizontal neighbors are same
- Can be 1D or 2D (e.g. used in fax standard)
- Quadtrees:
- Recursively subdivide until cells are constant color
- Region encoding:
- Represent boundary curves of color-constant regions
- Combine methods
- Not good on natural images directly


## Improving Noise Tolerance

- Predictive coding:
- Predict next pixel based on prior ones
- Output difference to actual
- Fractal image compression
- Describe image via recursive affine transformation
- Transform coding
- Exploit frequency domain
- Example: discrete cosine transform (DCT)
- Used in JPEG
- Transform coding for lossy compression


## Discrete Cosine Transform

- Used for lossy compression (as in JPEG)
$F(u, v)=c(u) c(v) \sum_{x=0}^{n-1} \sum_{y=0}^{n-1} f(x, y) \cos \frac{(2 x+1) u \pi}{2 n} \cos \frac{(2 y+1) v \pi}{2 n}$
where $c(u)=1 / \sqrt{n}$ if $u=0, c(u)=\sqrt{2 / n}$ otherwise
- JPEG (Joint Photographic Expert Group)
- Subdivide image into $\mathrm{n} \times \mathrm{n}$ blocks ( $\mathrm{n}=8$ )
- Apply discrete cosine transform for each block
- Quantize, zig-zag order, run-length code coefficients
- Use variable length coding (e.g. Huffman)
- Many natural images can be compressed to 4 bits/pixels with little visible error


## Summary

- Display Color Models
- 8 bit (colormap), 24 bit, 96 bit
- Filters
- Blur, edge detect, sharpen, despeckle
- Dithering
- Floyd-Steinberg error diffusion
- Image Compression
- Coding, interpixel, psychovisual redundancy
- Lossless vs. lossy compression


## Preview

- Assignment 5 due Thursday
- Assignment 6 out Thursday
- Thursday: Ray Tracing

