15-122: Principles of Imperative Computation

Lab 2: A Reversal of Fortune  Tom Cortina, Nivedita Chopra

Setup: Copy the lab code from our public directory to your private directory:

```
% cd private/15122
% cp -R /afs/andrew/course/15/122/misc/lab-integers .
% cd lab-integers
```

You should write your code in a file, `reverse.c0`, in the directory `lab-integers`.

Grading: You will work through (1.a) and (1.b) as a group. Finish (1.c) for lab credit, and (1.d) for potentially more credit. Show your TA that you’ve passed the tests when you complete these parts. You can work on these problems with your neighbors and compare notes and solutions!

Manipulating integers with a loop

For these two tasks, you’ll need to use a loop to manipulate integers. We can identify two ways of manipulating integers in C0:

- The mathematical operations of multiplication (`a * b`), division (`a / b`), modulo (`a % b`), addition (`a + b`), subtraction (`a - b`), and negation (`-a`).
- The bitwise operations bitwise-and (`a & b`), bitwise-or (`a | b`), bitwise-xor (`a ^ b`), bitwise negation (`~a`), left shift (`a << b`) and right-shift (`a >> b`).

We don’t always think about these operations as distinct categories! Sometimes, for instance, we think about `a << b` as the mathematical operation `a \times 2^b`. But for this assignment we will make the distinction.

(1.a) Our first task will be to reverse the digits in a seven-digit decimal number (a number with fewer digits will be treated as having leading zeros). There’s more than one way to do this! The three examples below show one way of reversing a number using a loop on the variable `i`:

<table>
<thead>
<tr>
<th>i</th>
<th>x</th>
<th>y</th>
<th>i</th>
<th>x</th>
<th>y</th>
<th>i</th>
<th>x</th>
<th>y</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1234567</td>
<td>0</td>
<td>1</td>
<td>15122</td>
<td>0</td>
<td>2</td>
<td>12345</td>
<td>76</td>
</tr>
<tr>
<td>1</td>
<td>123456</td>
<td>7</td>
<td>1</td>
<td>1512</td>
<td>2</td>
<td>2</td>
<td>12345</td>
<td>2</td>
</tr>
<tr>
<td>2</td>
<td>12345</td>
<td>76</td>
<td>1</td>
<td>151</td>
<td>22</td>
<td>2</td>
<td>1234</td>
<td>76</td>
</tr>
<tr>
<td>3</td>
<td>1234</td>
<td>765</td>
<td>3</td>
<td>15</td>
<td>221</td>
<td>3</td>
<td>2400</td>
<td>0</td>
</tr>
<tr>
<td>4</td>
<td>123</td>
<td>7654</td>
<td>4</td>
<td>1</td>
<td>2215</td>
<td>4</td>
<td>240</td>
<td>0</td>
</tr>
<tr>
<td>5</td>
<td>12</td>
<td>76543</td>
<td>5</td>
<td>0</td>
<td>22151</td>
<td>5</td>
<td>24</td>
<td>0</td>
</tr>
<tr>
<td>6</td>
<td>1</td>
<td>765432</td>
<td>6</td>
<td>0</td>
<td>221510</td>
<td>6</td>
<td>2</td>
<td>4</td>
</tr>
<tr>
<td>7</td>
<td>0</td>
<td>7654321</td>
<td>7</td>
<td>0</td>
<td>2215100</td>
<td>7</td>
<td>0</td>
<td>42</td>
</tr>
</tbody>
</table>

Can you suggest a couple of loop invariants for the algorithm above? Hint: you may want to use the `POW` specification from lecture. What can you say about `POW(10, i)`?

```
//@loop_invariant
//@loop_invariant
//@loop_invariant
//@loop_invariant
```

Remember that if you use `POW`, you need your loop invariants to also ensure that the exponent will always be nonnegative.
Here’s two example traces of a different algorithm for reversing a seven-digit number; this algorithm has more complicated invariants. Can you state some of them? Think about division and modulo.

<table>
<thead>
<tr>
<th>i</th>
<th>j</th>
<th>x</th>
<th>y</th>
<th>i</th>
<th>j</th>
<th>x</th>
<th>y</th>
</tr>
</thead>
<tbody>
<tr>
<td>10000000</td>
<td>1</td>
<td>1234567</td>
<td>0</td>
<td>10000000</td>
<td>1</td>
<td>15122</td>
<td>0</td>
</tr>
<tr>
<td>1000000</td>
<td>10</td>
<td>1234560</td>
<td>7000000</td>
<td>1000000</td>
<td>10</td>
<td>15120</td>
<td>2000000</td>
</tr>
<tr>
<td>1000000</td>
<td>100</td>
<td>1234500</td>
<td>7600000</td>
<td>1000000</td>
<td>100</td>
<td>15100</td>
<td>2200000</td>
</tr>
<tr>
<td>100000</td>
<td>1000</td>
<td>1234000</td>
<td>7650000</td>
<td>1000000</td>
<td>1000</td>
<td>15000</td>
<td>2210000</td>
</tr>
<tr>
<td>10000</td>
<td>10000</td>
<td>1230000</td>
<td>7654000</td>
<td>1000000</td>
<td>10000</td>
<td>15000</td>
<td>2215000</td>
</tr>
<tr>
<td>100</td>
<td>100000</td>
<td>1200000</td>
<td>7654300</td>
<td>10000000</td>
<td>0</td>
<td>1000000</td>
<td>2215100</td>
</tr>
<tr>
<td>10</td>
<td>1000000</td>
<td>1000000</td>
<td>7654320</td>
<td>10000000</td>
<td>0</td>
<td>1000000</td>
<td>2215100</td>
</tr>
<tr>
<td>1</td>
<td>10000000</td>
<td>0</td>
<td>7654321</td>
<td>1</td>
<td>10000000</td>
<td>0</td>
<td>2215100</td>
</tr>
</tbody>
</table>

//@loop_invariant
//@loop_invariant
//@loop_invariant
//@loop_invariant

Now you have two good sets of loop invariants: you can use either one of them to implement a function that reverses the decimal digits in a nonnegative number! (There are other ways, too.)

In `reverse.c0`, write a function `reverse_dec` that reverses the decimal digits in a nonnegative number with at most 7 decimal digits. **Treat a number with fewer digits as if it has leading zeroes.**

Use only mathematical operations on integers: * / % + -. You shouldn’t have to use POW outside of contracts.

```c
1  % coin -d reverse.c0
2  --> reverse_dec(7654321);
3  1234567 (int)
4  --> reverse_dec(1512200);
5  22151 (int)
6  --> reverse_dec(42);
7  2400000 (int)
```

You can test your code against our test cases by running `cc0 -d -x reverse.c0 test-dec.c0`

In `reverse.c0`, write a function `reverse_hex` that reverses all the hex digits of any integer:

Use only bitwise operations on integers: & | ~ ^ << >> to manipulate the input (you may need to manipulate a counter using mathematical operations). Don’t use POW in your code.

```c
1  % coin -d -lutil reverse.c0
2  --> int2hex(reverse_hex(0x195D3B7F));
3  "F7B30591" (string)
4  --> int2hex(reverse_hex(0x4C0CAFE));
5  "EFAC0C00" (string)
6  --> int2hex(reverse_hex(16));
7  "01000000" (string)
8  --> reverse_hex(int_min());
9  8 (int)
10 --> reverse_hex(int_max());
11 9 (int)
```

You can test your code against our test cases by running `cc0 -d -x reverse.c0 test-hex.c0`