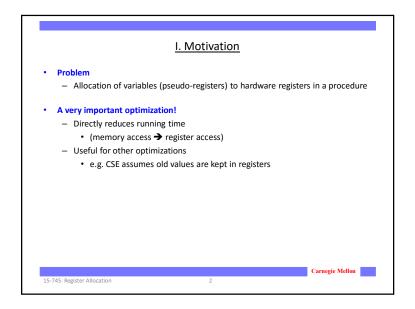
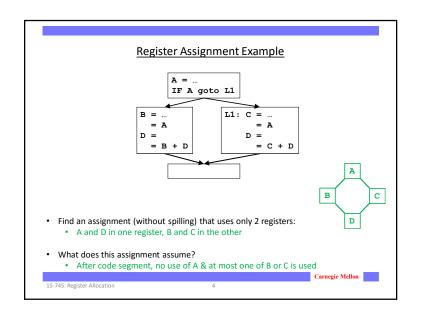
## Lecture 14 Register Allocation & Spilling I. Introduction II. Abstraction and the Problem III. Algorithm IV. Spilling [ALSU 8.8] Phillip B. Glibbons 15-745: Register Allocation 1

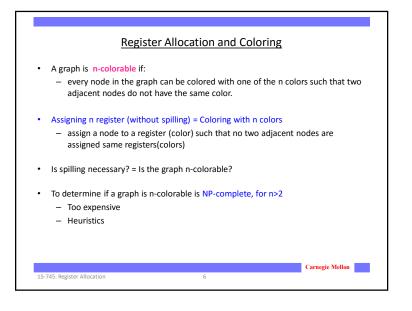
### Goals • Find an allocation for all pseudo-registers, if possible • If there are not enough registers in the machine, choose registers to spill to memory Carnegie Mellon

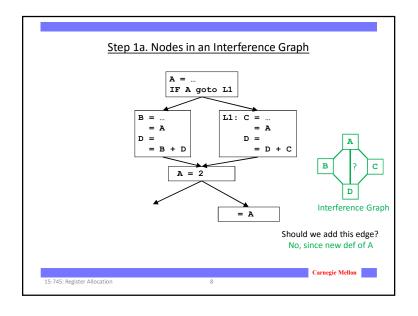


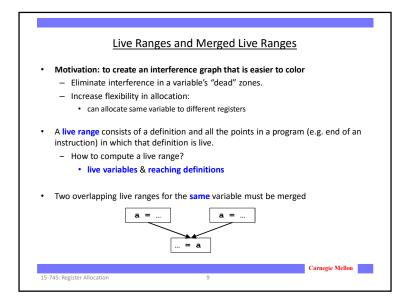


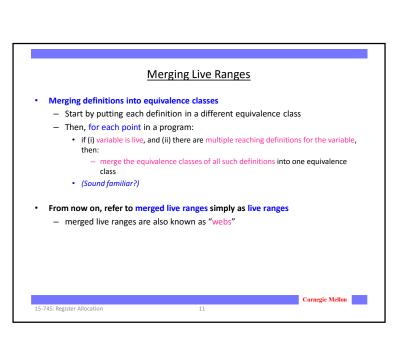
### II. An Abstraction for Allocation & Assignment Intuitively - Two pseudo-registers interfere if at some point in the program they cannot both occupy the same register. • Interference graph: an undirected graph, where – nodes = pseudo-registers - there is an edge between two nodes if their corresponding pseudo-registers interfere · What is not represented Interfere many - Extent of the interference between uses of different variables times vs. once - Where in the program is the interference E.g., cold path vs. hot path 15-745: Register Allocation

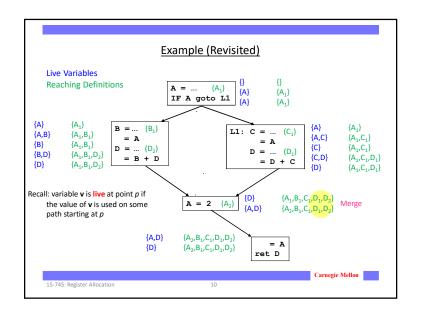
# III. Algorithm Step 1. Build an interference graph a. refining notion of a node b. finding the edges Step 2. Coloring - use heuristics to try to find an n-coloring • Success: - colorable and we have an assignment • Failure: - graph not colorable, or - graph is colorable, but it is too expensive to color

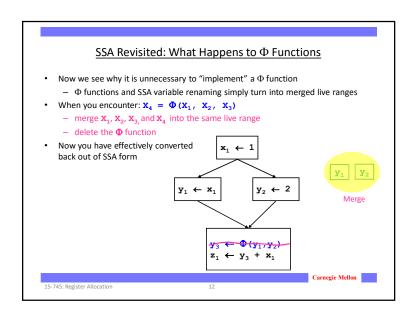




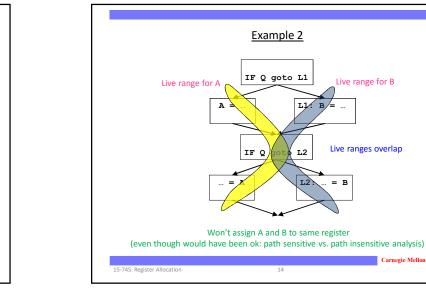


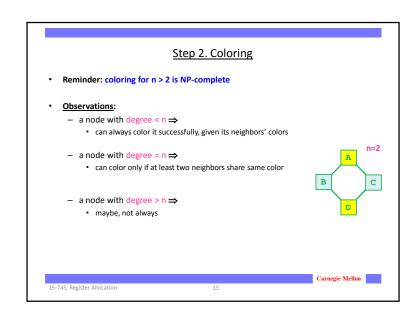


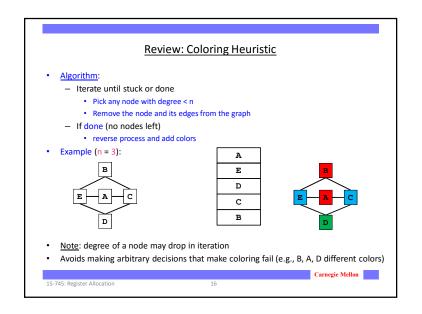




## Step 1b. Edges of Interference Graph • Intuitively: - Two live ranges (necessarily of different variables) may interfere if they overlap at some point in the program - Algorithm: - At each point in the program: - enter an edge for every pair of live ranges at that point • An optimized definition & algorithm for edges: - Algorithm: - check for interference only at the start of each live range - Faster - Better quality Carnegie Mellon

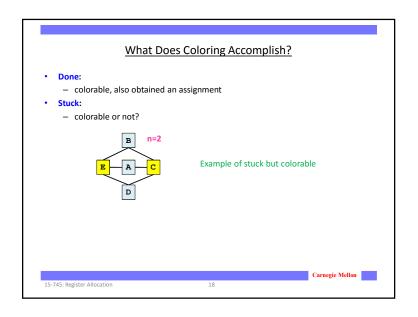


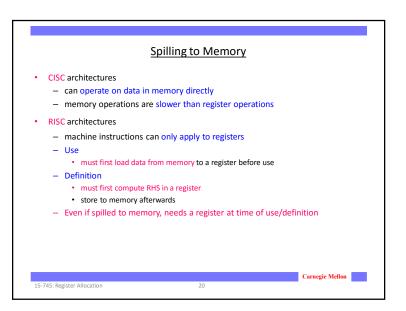




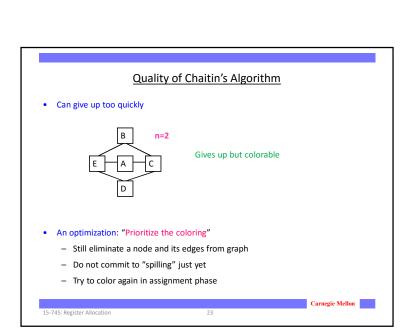
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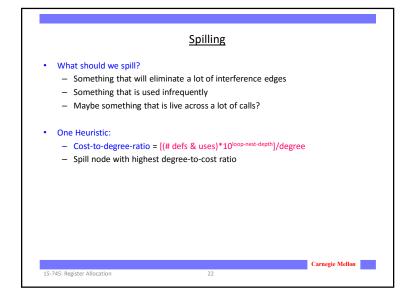
### IV. Extending Coloring: Design Principles A pseudo-register is - Colored successfully: allocated a hardware register Not colored: left in memory · Objective function Cost of an uncolored node: proportional to number of uses/definitions (dynamically) · estimate by its loop nesting - Objective: minimize sum of cost of uncolored nodes Heuristics - Benefit of spilling a pseudo-register: · increases colorability of pseudo-registers it interferes with · can approximate by its degree in interference graph Greedy heuristic • spill the pseudo-register with lowest cost-to-benefit ratio, whenever spilling is necessary Carnegie Mellon 15-745: Register Allocation

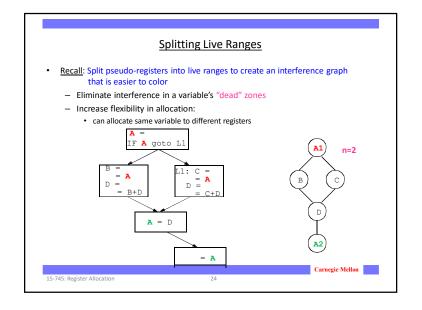




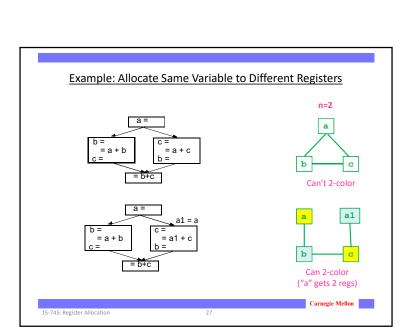
### Chaitin: Coloring and Spilling · Apply coloring heuristic Build interference graph Iterate until there are no nodes left If there exists a node v with less than n neighbor push v on register allocation stack v = node with highest degree-to-cost ratio mark v as spilled remove v and its edges from graph · Spilling may require use of registers; change interference graph While there is spilling rebuild interference graph and perform step above Assign registers While stack is not empty Pop v from stack Reinsert v and its edges into the graph Assign v a color that differs from all its neighbors 15-745: Register Allocation

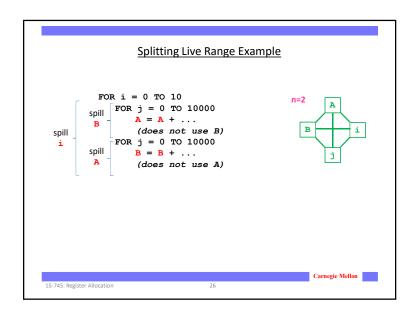


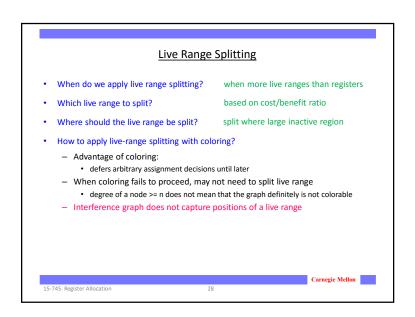


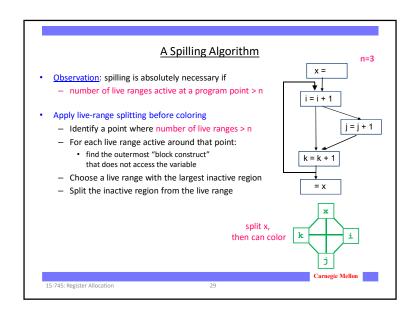


## Insight • Split a live range into smaller regions (by paying a small cost) to create an interference graph that is easier to color • Eliminate interference in a variable's "nearly dead" zones. • Cost: Memory loads and stores • Load and store at boundaries of regions with no activity • # active live ranges at a program point can be > # registers • Can allocate same variable to different registers • Cost: Register operations • a register copy between regions of different assignments • # active live ranges cannot be > # registers Carnegie Mellon









## Friday's Class • Instruction Scheduling [ALSU 10.1 – 10.2] 15-745: Register Allocation 31

### Summary • Problems: - Given n registers in a machine, is spilling avoided? - Find an assignment for all pseudo-registers, whenever possible. Solution: Abstraction: an interference graph nodes: live ranges · edges: presence of live range at time of definition Register Allocation and Assignment problems • equivalent to n-colorability of interference graph → NP-complete Heuristics to find an assignment for n colors successful: colorable, and finds assignment • not successful: colorability unknown & no assignment Carnegie Mellon 15-745: Register Allocation