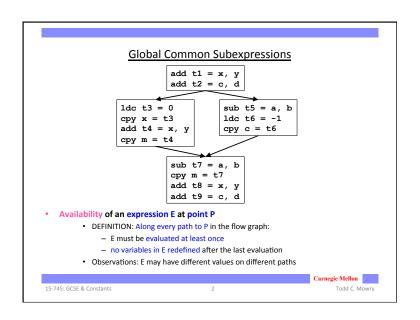
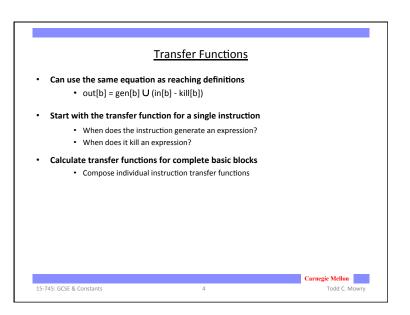
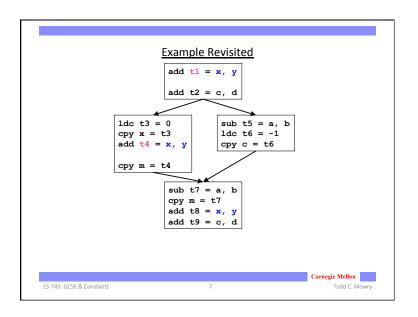
Lecture 7 More Examples of Data Flow Analysis: Global Common Subexpression Elimination; Constant Propagation/Folding I. Available Expressions Analysis II. Eliminating CSEs III. Constant Propagation/Folding Reading: 9.2.6, 9.4

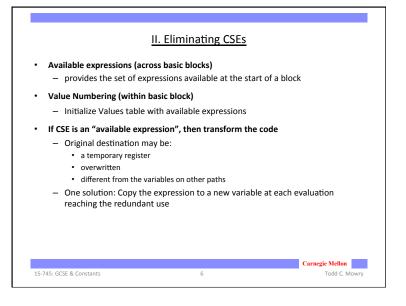
Formulating the Problem · Domain: · a bit vector, with a bit for each textually unique expression in the program · Forward or Backward? · Lattice Elements? Meet Operator? · check: commutative, idempotent, associative · Partial Ordering Top? · Bottom? Boundary condition: entry/exit node? · Initialization for iterative algorithm? Carnegie Mellon 15-745: GCSE & Constants Todd C. Mowry

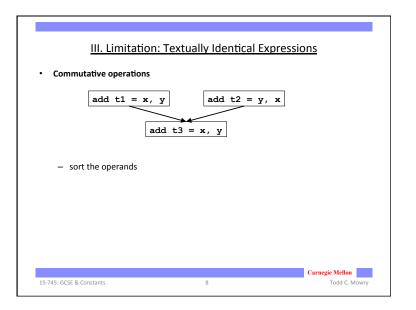


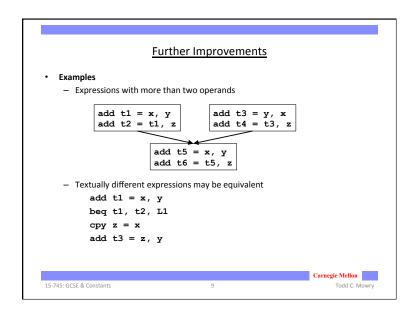


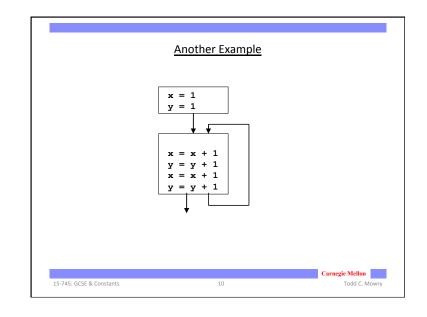
Composing Transfer Functions • Derive the transfer function for an entire block in1 out1 = gen1 U (in1 - kill1) = in2 out2 = gen2 U (in2 - kill2) • Since out1 = in2 we can simplify: • out2 = gen2 U (gen1 - kill1) - kill2) • out2 = gen2 U (gen1 - kill2) U (in1 - (kill1 U kill2)) • out2 = gen2 U (gen1 - kill2) U (in1 - (kill1 U kill2)) • out2 = gen2 U (gen1 - kill2) U (in1 - (kill2 U (kill1 - gen2))) • Result • gen = gen2 U (gen1 - kill2) • kill = kill2 U (kill1 - gen2)

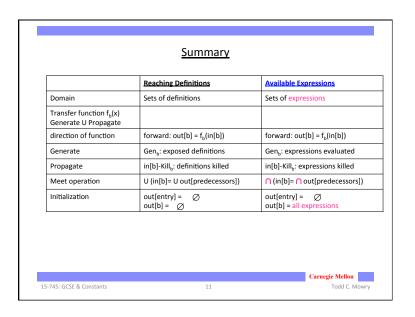


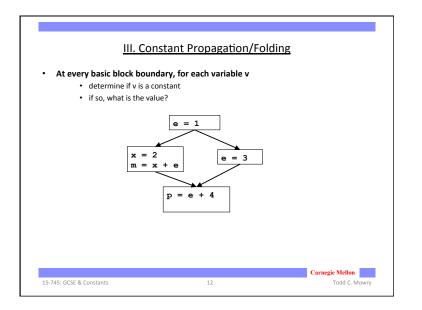


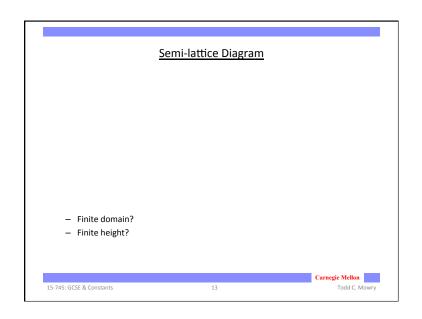


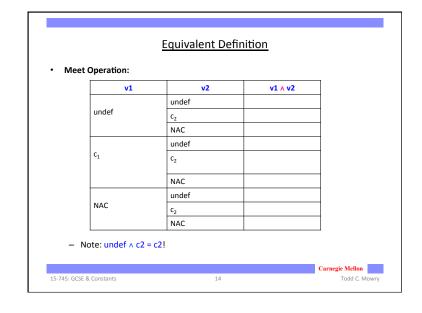


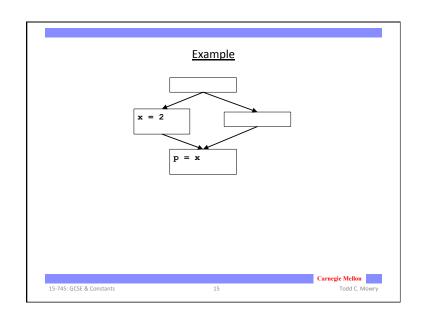


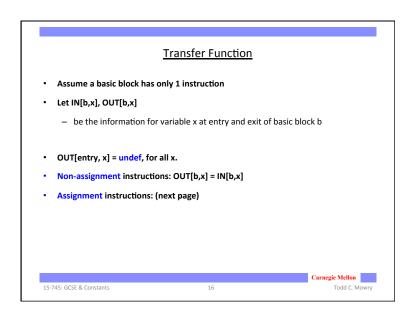












Constant Propagation (Cont.)

- Let an assignment be of the form x₃ = x₁ + x₂
 - "+" represents a generic operator
 - OUT[b,x] = IN [b,x], if x ≠ x₃

IN[b,x ₁]	IN[b,x ₂]	OUT[b,x ₃]
undef	undef	
	C ₂	
	NAC	
c ₁	undef	
	C ₂	
	NAC	
NAC	undef	
	C ₂	
	NAC	

- Use: $x \le y$ implies $f(x) \le f(y)$ to check if framework is monotone
 - $[v_1 v_2...] \le [v_1' v_2'...], f([v_1 v_2...]) \le f([v_1' v_2'...])$

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