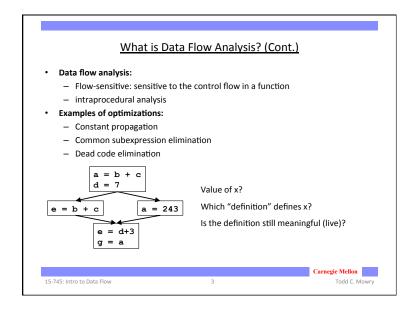
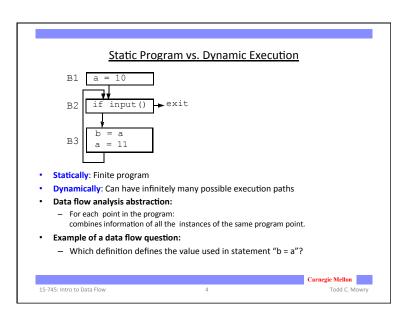
Lecture 4 Introduction to Data Flow Analysis I. Structure of data flow analysis II. Example 1: Reaching definition analysis III. Example 2: Liveness analysis IV. Generalization



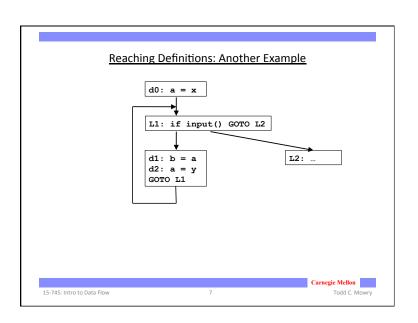
What is Data Flow Analysis? Local analysis (e.g. value numbering) analyze effect of each instruction compose effects of instructions to derive information from beginning of basic block to each instruction Data flow analysis analyze effect of each basic block compose effects of basic blocks to derive information at basic block boundaries from basic block boundaries, apply local technique to generate information on instructions Carnegie Mellon 15-745: Intro to Data Flow Todd C. Mowry

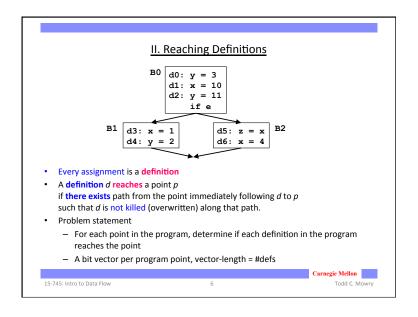


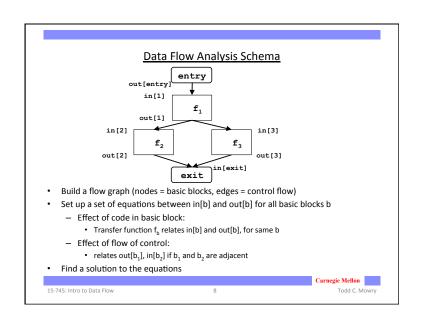
Effects of a Basic Block Effect of a statement: a = b+c Uses variables (b, c) • Kills an old definition (old definition of a) • new definition (a) • Compose effects of statements -> Effect of a basic block • A locally exposed use in a b.b. is a use of a data item which is not preceded in the b.b. by a definition of the data item · any definition of a data item in the basic block kills all definitions of the same data item reaching the basic block. • A locally available definition = last definition of data item in b.b. t1 = r1+r2r2 = t1t2 = r2 + r1r1 = t2t3 = r1*r1r2 = t3if r2>100 goto L1 Carnegie Mellon

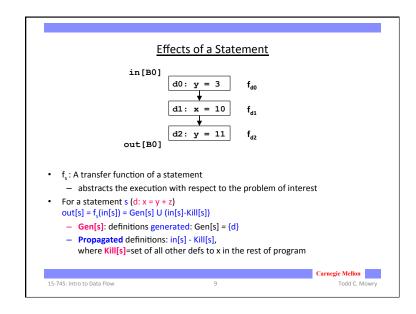
Todd C. Mowry

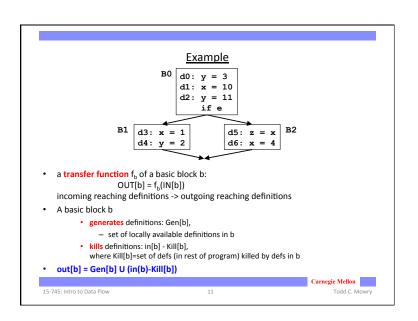
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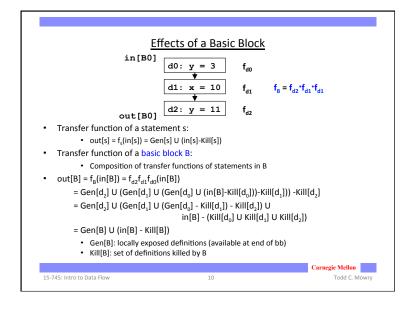


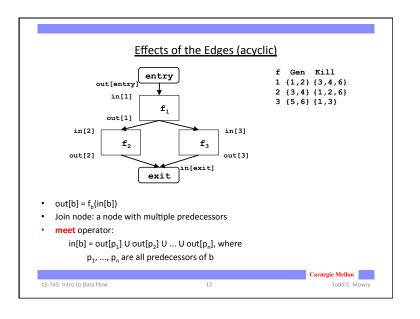


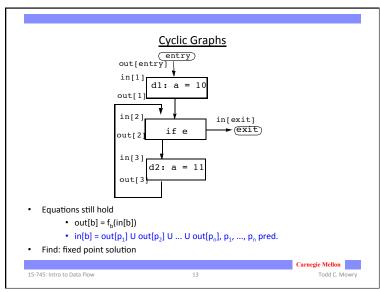






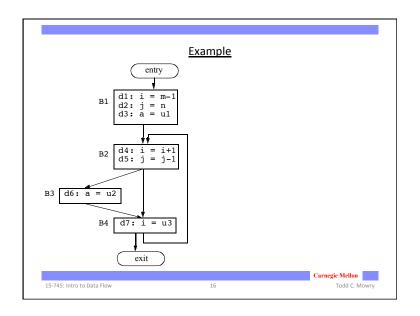






```
Reaching Definitions: Worklist Algorithm
input: control flow graph CFG = (N, E, Entry, Exit)
// Initialize
    out[Entry] = Ø
                            // can set out[Entry] to special def
                            // if reaching then undefined use
    For all nodes i
        out[i] = Ø
                            // can optimize by out[i]=gen[i]
    ChangedNodes = N
// iterate
    While ChangedNodes \neq \emptyset {
        Remove i from ChangedNodes
        in[i] = U (out[p]), for all predecessors p of i
        oldout = out[i]
        out[i] = f,(in[i])
                               // out[i]=gen[i]U(in[i]-kill[i])
        if (oldout # out[i]) {
            for all successors s of i
                add s to ChangedNodes
    }
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```

```
Reaching Definitions: Iterative Algorithm
input: control flow graph CFG = (N, E, Entry, Exit)
// Boundary condition
   out[Entry] = \emptyset
// Initialization for iterative algorithm
   For each basic block B other than Entry
      out[B] = \emptyset
// iterate
   While (Changes to any out[] occur) {
      For each basic block B other than Entry {
         in[B] = U (out[p]), for all predecessors p of B
         out[B] = f_B(in[B]) // out[B]=gen[B]U(in[B]-kill[B])
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```



III. Live Variable Analysis

- Definition
 - A variable \mathbf{v} is live at point p if
 - the value of \mathbf{v} is used along some path in the flow graph starting at p.
 - Otherwise, the variable is dead.
- Motivation
 - · e.g. register allocation for i = 0 to n ... i ... for i = 0 to n ... i ...
- · Problem statement
 - For each basic block
 - · determine if each variable is live in each basic block
 - Size of bit vector: one bit for each variable

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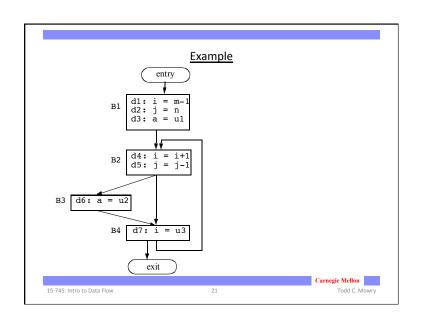
Flow Graph f Use entry 1 {e} {a,b} out[entry] 2 {} {a,b} in[1] 3 {a} {a,c} out[1] in[2] in[3] f_2 out[2] out[3] in[exit] exit in[b] = f_b(out[b]) Join node: a node with multiple successors meet operator: out[b] = $in[s_1] U in[s_2] U ... U in[s_n]$, where s₁, ..., s_n are all successors of b Carnegie Mellon 15-745: Intro to Data Flow 19 Todd C. Mowry

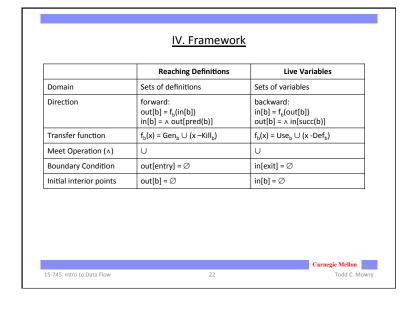
```
Effects of a Basic Block (Transfer Function)
• Insight: Trace uses backwards to the definitions
        an execution path
                                       control flow
                                                                 example
                                                                 d3: a = 1
                                                = f_b(OUT[b])
                                                                 d4: b = 1
                       def
                                                                 d5: c = a
                                     OUT[b]
                                                                 d6: a = 4
                       use
· A basic block b can
         • generate live variables: Use[b]
              - set of locally exposed uses in b
         • propagate incoming live variables: OUT[b] - Def[b],
              - where Def[b]= set of variables defined in b.b.

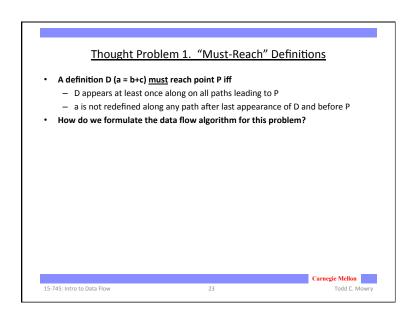
    transfer function for block b:

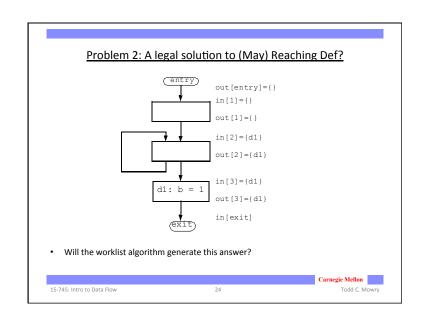
                  in[b] = Use[b] U (out(b)-Def[b])
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```

```
Liveness: Iterative Algorithm
input: control flow graph CFG = (N, E, Entry, Exit)
// Boundary condition
   in[Exit] = \emptyset
// Initialization for iterative algorithm
   For each basic block B other than Exit
      in[B] = \emptyset
// iterate
   While (Changes to any in[] occur) {
      For each basic block B other than Exit {
         out[B] = U (in[s]), for all successors s of B
         in[B] = f_B(out[B]) // in[B]=Use[B]U(out[B]-Def[B])
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```









Questions

- Correctness
 - equations are satisfied, if the program terminates.
- · Precision: how good is the answer?
 - is the answer ONLY a union of all possible executions?
- · Convergence: will the analysis terminate?
 - or, will there always be some nodes that change?
- Speed: how fast is the convergence?
 - how many times will we visit each node?

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2

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