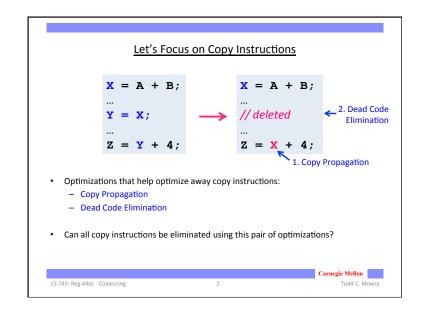
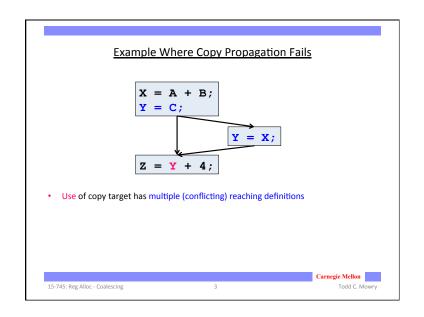
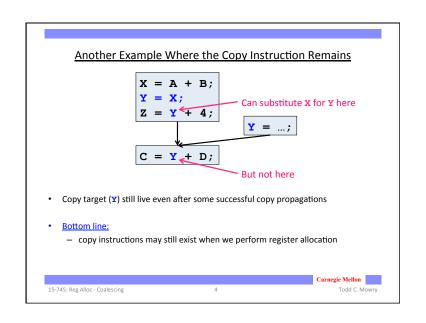
# Lecture 16 Register Allocation: Coalescing Carnegie Mellon Todd C. Mowry 15-745: Reg Alloc - Coalescing







### Copy Instructions and Register Allocation

• What clever thing might the register allocator do for copy instructions?



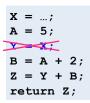
- If we can assign both the source and target of the copy to the same register:
  - then we don't need to perform the copy instruction at all!
  - the copy instruction can be removed from the code
    - even though the optimizer was unable to do this earlier
- One way to do this:
  - treat the copy source and target as the same node in the interference graph
    - then the coloring algorithm will naturally assign them to the same register
  - this is called "coalescing"

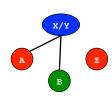
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### **Example Revisited: With Coalescing**





Valid coloring with 3 registers

- With coalescing, **X** and **Y** are now guaranteed to end up in the same register
  - the copy instruction can now be eliminated
- Great! So should we go ahead and do this for every copy instruction?

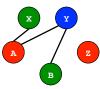
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# Simple Example: Without Coalescing





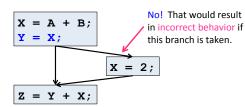
Valid coloring with 3 registers

- Without coalescing, **X** and **Y** can end up in different registers
  - cannot eliminate the copy instruction

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# Should We Coalesce **x** and **y** In This Case?



- It is legal to coalesce **X** and **Y** for a "**Y** = **X**" copy instruction iff:
  - initial definition of Y's live range is this copy instruction, AND
  - the live ranges of **x** and **y** do not interfere otherwise
- But just because it is legal doesn't mean that it is a good idea...

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### Why Coalescing May Be Undesirable, Even If Legal

- What is the likely impact of coalescing **X** and **Y** on:
  - live range size(s)?
    - · recall our discussion of live range splitting
  - colorability of the interference graph?
- Fundamentally, coalescing adds further constraints to the coloring problem
  - doesn't make coloring easier; may make it more difficult
- · If we coalesce in this case, we may:
  - save a copy instruction, BUT
  - cause significant spilling overhead if we can no longer color the graph

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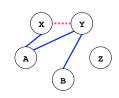
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### Representing Coalescing Candidates in the Interference Graph

- To decide whether to coalesce, we augment the interference graph
- Coalescing candidates are represented by a new type of interference graph edge:
  - dotted lines: coalescing candidates
    - try to assign vertices the same color
      - (unless that is problematic, in which case they can be given different colors)
  - solid lines: interference
    - vertices must be assigned different colors





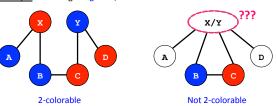
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### When to Coalesce

- · Goal when coalescing is legal:
  - coalesce unless it would make a colorable graph non-colorable
- · The bad news:
  - predicting colorability is tricky!
    - · it depends on the shape of the graph
    - · graph coloring is NP-hard
- Example: assuming 2 registers, should we coalesce X and Y?



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# How Do We Know When Coalescing Will Not Cause Spilling?

- Key insight:
  - Recall from the coloring algorithm:
    - we can always successfully N-color a node if its degree is < N
- To ensure that coalescing does not cause spilling:
  - check that the degree < N invariant is still locally preserved after coalescing</li>
    - if so, then coalescing won't cause the graph to become non-colorable
  - no need to inspect the entire interference graph, or do trial-and-error
- Note:
  - $\,-\,$  We do NOT need to determine whether the full graph is colorable or not
  - Just need to check that coalescing does not cause a colorable graph to become non-colorable

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# Simple and Safe Coalescing Algorithm

- We can safely coalesce nodes X and Y if (|X| + |Y|) < N</li>
  - Note: |x| = degree of node x counting interference (not coalescing) edges

Example:



 $(|\mathbf{x}| + |\mathbf{y}|) = (1+2) = 3$ 



Degree of coalesced node can be no larger than 3

- if N >= 4, it would always be safe to coalesce these two nodes
  - this cannot cause new spilling that would not have occurred with the original graph
- if N < 4, it is unclear

How can we (safely) be more aggressive than this?

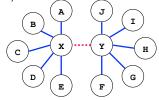
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### Another Helpful Insight

- Colors are not assigned until nodes are popped off the stack
  - nodes with degree < N are pushed on the stack first</li>
  - when a node is popped off the stack, we know that it can be colored
    - because the number of potentially conflicting neighbors must be < N
- Spilling only occurs if there is no node with degree < N to push on the stack

<u>Example</u>: (N=2)



 $|\mathbf{x}| = 5$  $|\mathbf{Y}| = 5$ 

2-colorable after coalescing x and y?

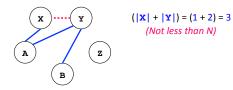
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# What About This Example?

- Assume N = 3
- Is it safe to coalesce x and y?



- Notice: X and Y share a common (interference) neighbor: node A
  - hence the degree of the coalesced X/Y node is actually 2 (not 3)
  - therefore coalescing **X** and **Y** is guaranteed to be safe when N = 3
- · How can we adjust the algorithm to capture this?

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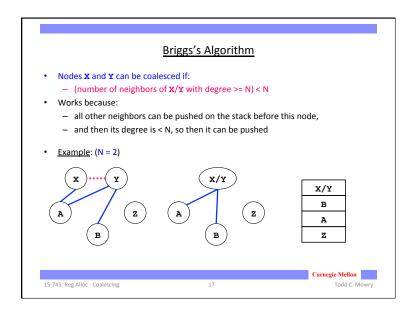
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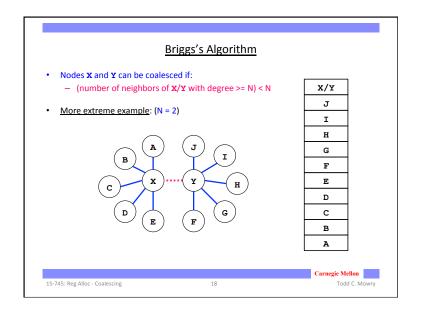
# **Building on This Insight**

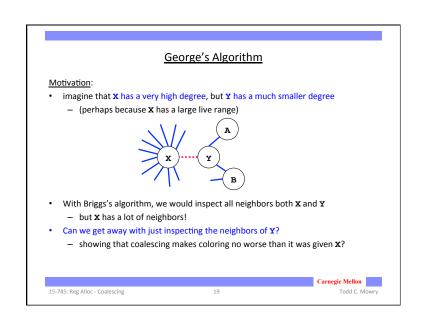
- When would coalescing cause the stack pushing (aka "simplification") to get stuck?
  - 1. coalesced node must have a degree >= N
    - otherwise, it can be pushed on the stack, and we are not stuck
  - 2. AND it must have at least N neighbors that each have a degree >= N
    - otherwise, all neighbors with degree < N can be pushed before this node
      - reducing this node's degree below N (and therefore we aren't stuck)
- · To coalesce more aggressively (and safely), let's exploit this second requirement
  - which involves looking at the degree of a coalescing candidate's neighbors
    - not just the degree of the coalescing candidates themselves

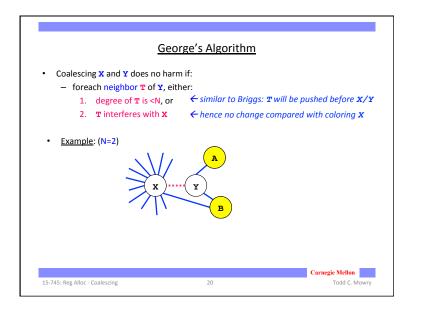
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# Summary

- Coalescing can enable register allocation to eliminate copy instructions
  - if both source and target of copy can be allocated to the same register
- However, coalescing must be applied with care to avoid causing register spilling
- · Augment the interference graph:
  - dotted lines for coalescing candidate edges
  - try to allocate to same register, unless this may cause spilling
- Coalescing Algorithms:
  - simply based upon degree of coalescing candidate nodes (X and Y)
  - Briggs's algorithm
    - look at degree of neighboring nodes of **x** and **y**
  - George's algorithm
    - asymmetrical: look at neighbors of Y (degree and interference with X)

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