

Lecture 14

SSA-Style Optimizations

(Slides courtesy of Seth Goldstein.)

Todd C. Mowry

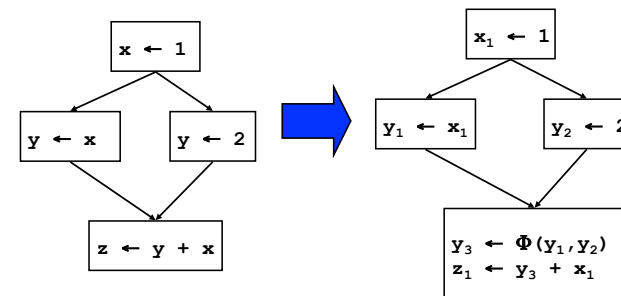
15-745: SSA-Style Optimizations

Carnegie Mellon

1

Review: Minimal SSA

- Each assignment generates a fresh variable.
- At each join point insert Φ functions for all **live variables** with **multiple outstanding defs**.



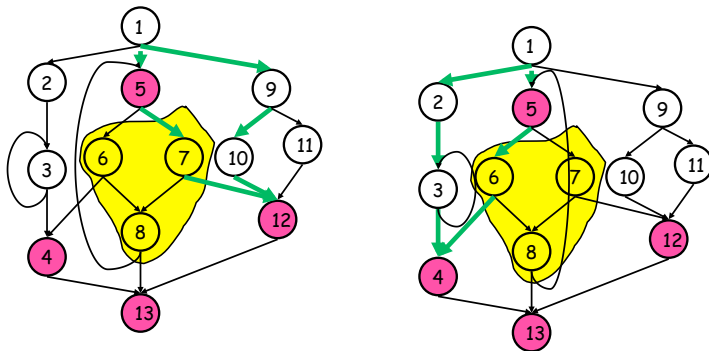
15-745: SSA-Style Optimizations

2

Carnegie Mellon

Todd C. Mowry

Review: Dominance Frontier and Path Convergence



15-745: SSA-Style Optimizations

3

Carnegie Mellon

Todd C. Mowry

Constant Propagation

- If " $v \leftarrow c$ ", replace all uses of v with c
- If " $v \leftarrow \Phi(c, c, c)$ ", replace all uses of v with c

```

W ← list of all defs
while !W.isEmpty {
  Stmt S ← W.removeOne
  if ((S has form " $v \leftarrow c$ ") ||
    (S has form " $v \leftarrow \Phi(c, \dots, c)$ ") ) then {
    delete S
    foreach stmt U that uses v {
      replace v with c in U
      W.add(U)
    }
  }
}

```

15-745: SSA-Style Optimizations

4

Carnegie Mellon

Todd C. Mowry

Other Optimizations with SSA

- **Copy propagation**
 - delete " $x \leftarrow \Phi(y,y)$ " and replace all x with y
 - delete " $x \leftarrow y$ " and replace all x with y
- **Constant Folding**
 - (Also, constant conditions too!)

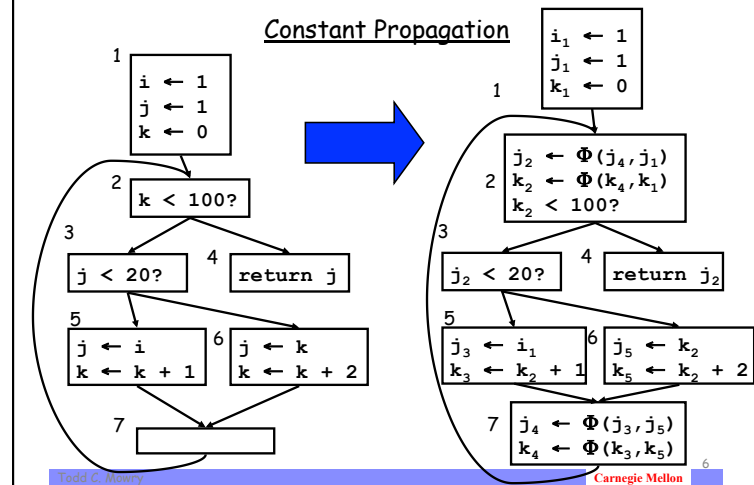
15-745: SSA-Style Optimizations

5

Carnegie Mellon

Todd C. Mowry

Constant Propagation

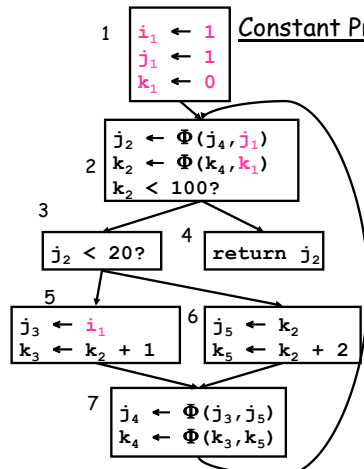


Todd C. Mowry

15-745: SSA-Style Optimizations

Carnegie Mellon

Constant Propagation



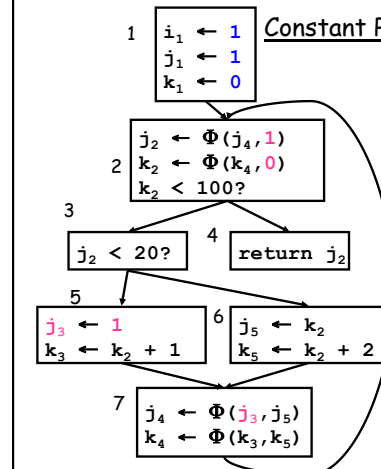
Todd C. Mowry

15-745: SSA-Style Optimizations

7

Carnegie Mellon

Constant Propagation

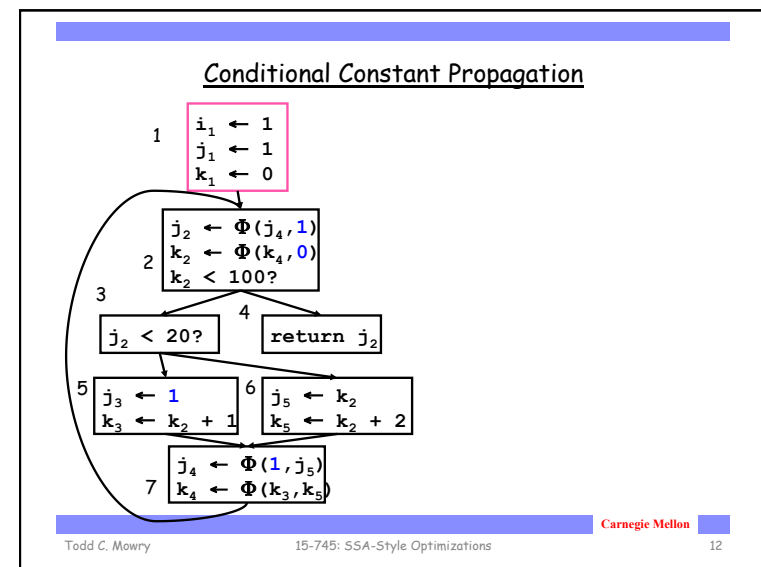
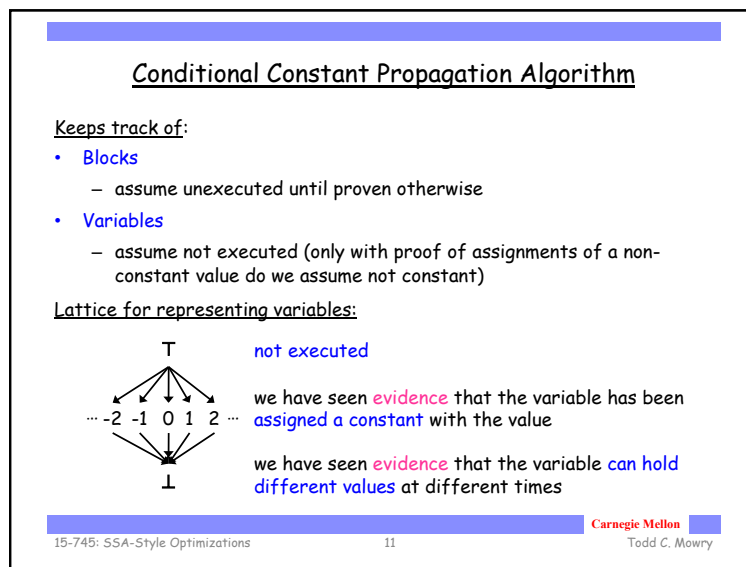
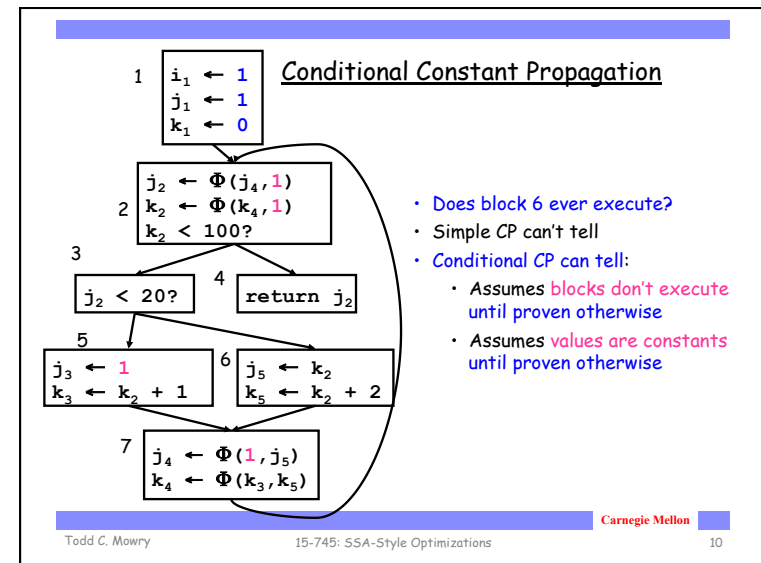
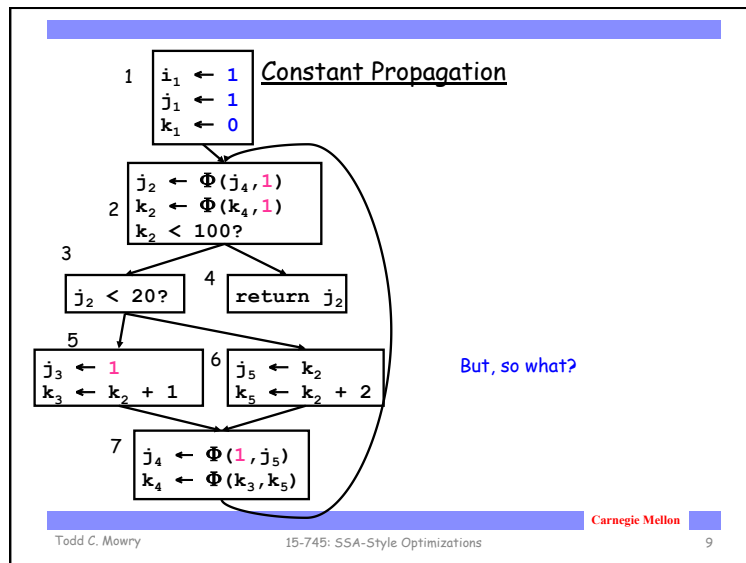


Todd C. Mowry

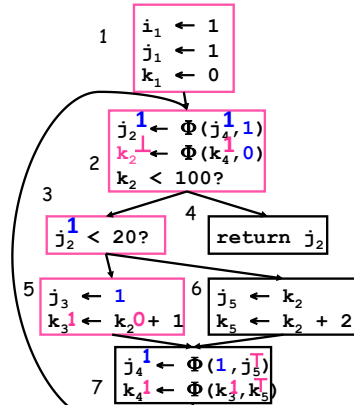
15-745: SSA-Style Optimizations

8

Carnegie Mellon



Conditional Constant Propagation



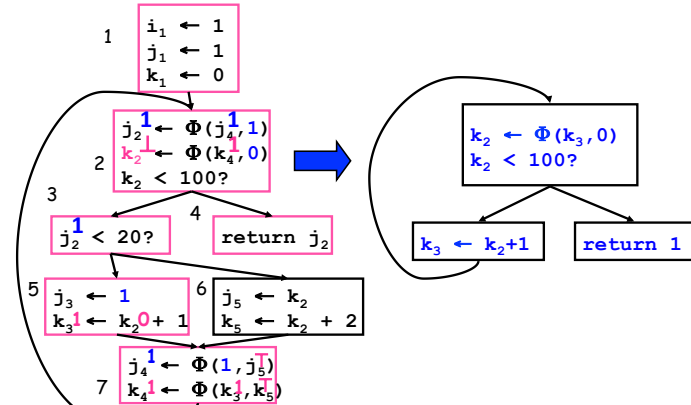
Todd C. Mowry

15-745: SSA-Style Optimizations

Carnegie Mellon

13

Conditional Constant Propagation



Todd C. Mowry

15-745: SSA-Style Optimizations

Carnegie Mellon

14

Dead Code Elimination

```
W <- list of all defs
while !W.isEmpty {
  Stmt S <- W.removeOne
  if |S.users| != 0 then continue
  if S.hasSideEffects() then continue
  foreach def in S.operands.definers {
    def.users <- def.users - {S}
    if |def.users| == 0 then
      W <- W UNION {def}
  }
  delete S
}
```

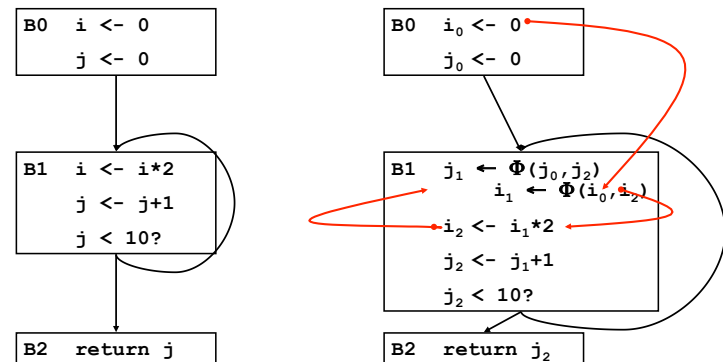
Todd C. Mowry

15-745: SSA-Style Optimizations

Carnegie Mellon

15

Example DCE



Standard DCE leaves Zombies!

Todd C. Mowry

15-745: SSA-Style Optimizations

Carnegie Mellon

16

Aggressive Dead Code Elimination

Assume a statement is dead until proven otherwise.

```

init:
  mark as live all stmts that have side-effects:
    - I/O
    - stores into memory
    - returns
    - calls a function that MIGHT have side-effects
  As we mark S live, insert S.operands.definers into W

while (|W| > 0) {
  S ← W.removeOne()
  if (S is live) continue;
  mark S live, insert S.operands.definers into W
}
  
```

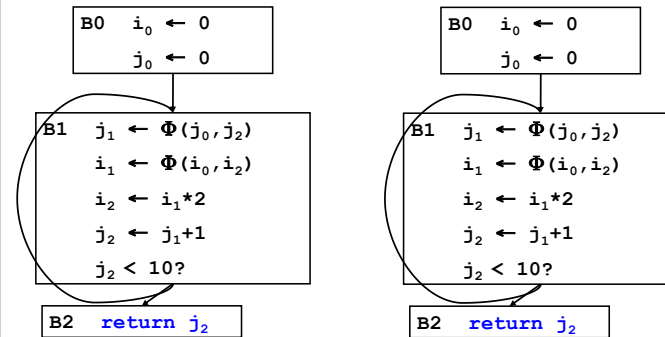
Todd C. Mowry

15-745: SSA-Style Optimizations

Carnegie Mellon

17

Example DCE



Problem!

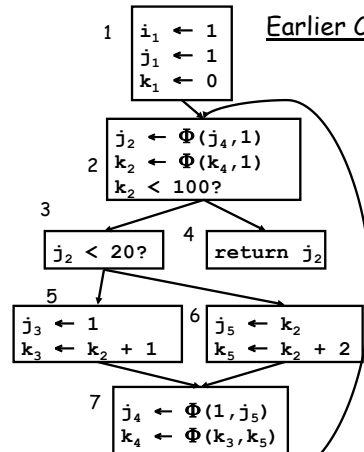
Todd C. Mowry

15-745: SSA-Style Optimizations

Carnegie Mellon

18

Earlier CCP Example Revisited



Todd C. Mowry

15-745: SSA-Style Optimizations

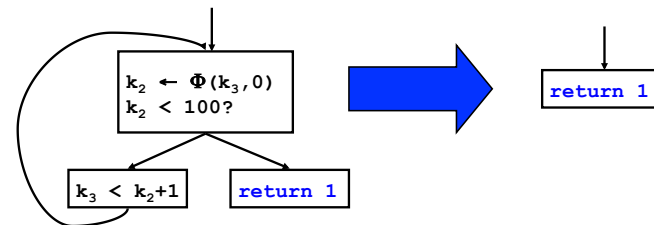
Carnegie Mellon

19

Applying Dead Code Elimination to the Result of CCP

After CCP

After DCE



Small problem.

Todd C. Mowry

15-745: SSA-Style Optimizations

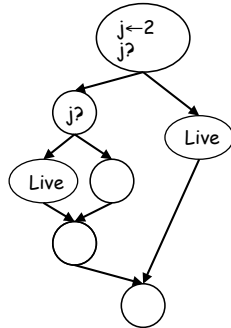
Carnegie Mellon

20

Fixing DCE

if **S** is live, then

if **T** determines if **S** can execute, **T** should be live



15-745: SSA-Style Optimizations

21

Carnegie Mellon

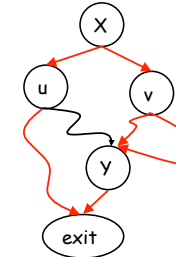
Todd C. Mowry

Control Dependence

Y is control-dependent on **X** if

- **X** branches to **u** and **v**
- $\exists$ a path $u \rightarrow \text{exit}$ which does not go through **Y**
- $\forall$ paths $v \rightarrow \text{exit}$ go through **Y**

i.e. **X** can determine whether or not **Y** is executed.



15-745: SSA-Style Optimizations

22

Carnegie Mellon

Todd C. Mowry

Aggressive Dead Code Elimination (Fixed Version)

Assume a statement is dead until proven otherwise.

init:

mark as live all stmts that have side-effects:

- I/O
- stores into memory
- returns
- calls a function that MIGHT have side-effects

As we mark **S** live, insert:

- **S.operands.definers** into **W**
- **S.CD⁻¹** into **W**

while (**|W|** > 0) {

S ← **W.removeOne()**

if (**S** is live) continue;

mark **S** live, insert:

- **S.operands.definers** into **W**
- **S.CD⁻¹** into **W**

}

Conditional tests for blocks upon which **S** are control-dependent are also inserted into work-list.

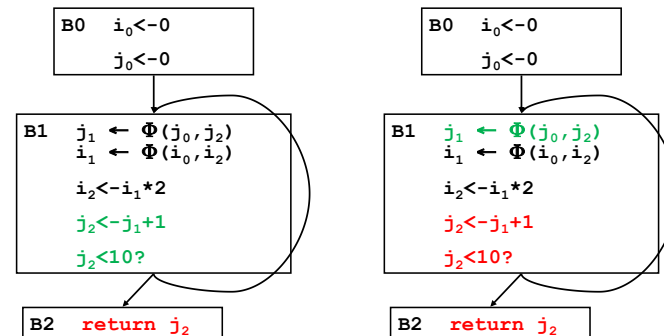
Todd C. Mowry

15-745: SSA-Style Optimizations

Carnegie Mellon

23

Example DCE



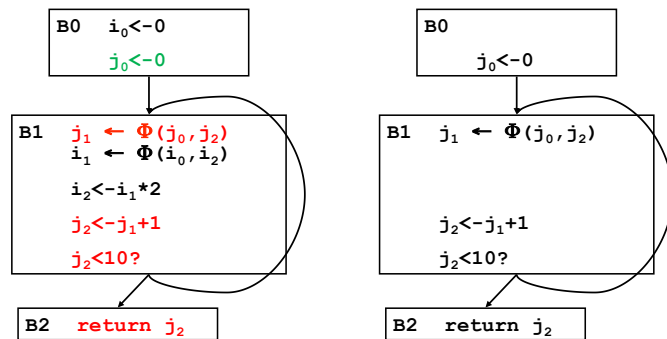
Todd C. Mowry

15-745: SSA-Style Optimizations

Carnegie Mellon

24

Example DCE



Todd C. Mowry

15-745: SSA-Style Optimizations

Carnegie Mellon

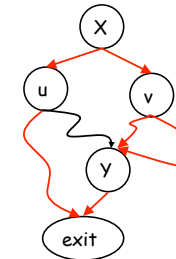
25

Finding the Control Dependence Graph

Y is **control-dependent** on X if

- X branches to u and v
- $\exists$ a path $u \rightarrow \text{exit}$ which does not go through Y
- $\forall$ paths $v \rightarrow \text{exit}$ go through Y

i.e. X can determine whether or not Y is executed.



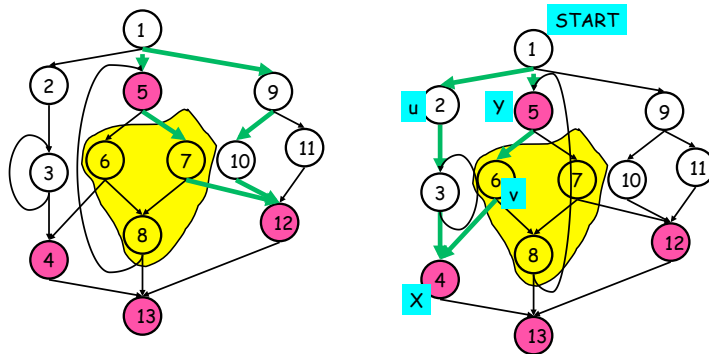
15-745: SSA-Style Optimizations

26

Carnegie Mellon

Todd C. Mowry

Dominance Frontier and Path Convergence



Any ideas?

15-745: Intro to SSA

27

Carnegie Mellon

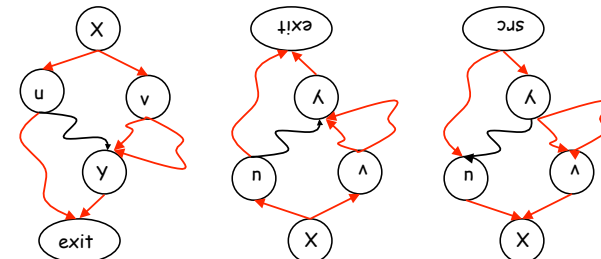
Todd C. Mowry

Finding the Control Dependence Graph

Y is **control-dependent** on X if

- X branches to u and v
- $\exists$ a path $u \rightarrow \text{exit}$ which does not go through Y
- $\forall$ paths $v \rightarrow \text{exit}$ go through Y

i.e. X can determine whether or not Y is executed.



15-745: SSA-Style Optimizations

28

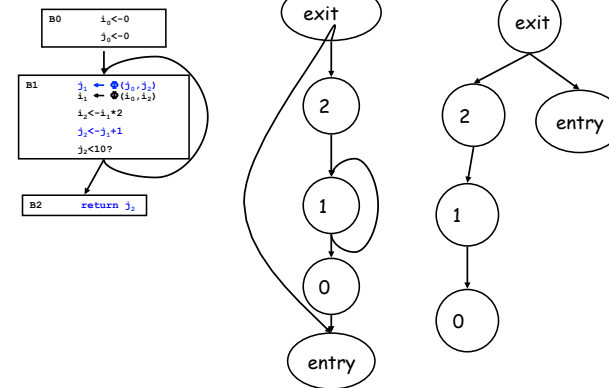
Carnegie Mellon

Todd C. Mowry

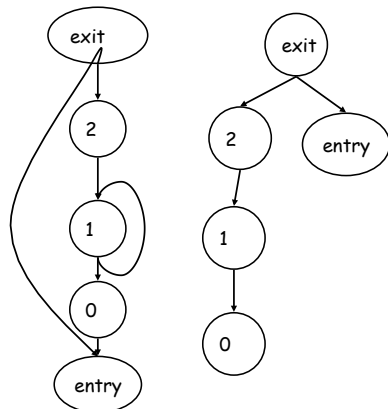
Finding the CDG

- Construct CFG
- Add entry node and exit node
- Add (entry,exit)
- Create G' , the reverse CFG
- Compute D-tree in G' (post-dominators of G)
- Compute $DF_G(y)$ for all $y \in G'$ (post-DF of G)
- Add $(x,y) \in G$ to CDG if $x \in DF_G(y)$

CDG of example



CDG of example



```
exit: {}
2: {entry}
1: {1,entry}
0: {entry}
entry: {}
```