15-251

Great Theoretical Ideas in Computer Science

15-251

**Great Theoretical Ideas** in Computer Science

www.cs.cmu.edu/~15251

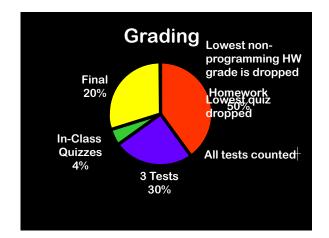
#### **Course Staff**

#### **Instructors**

Victor Adamchik Danny Sleator

#### **TAs**

Drew Besse Adam Blank Dmtriy Chernyak Sameer Chopra Dan Kilgallin Alan Pierce



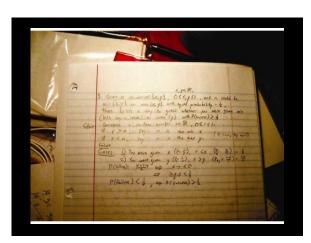
#### **Weekly Homework**

Homeworks handed out Tuesdays (except for a couple) and are due the following Tuesday, at midnight

Ten points per day late penalty

No homework will be accepted more than two days late

Homework MUST be typeset, and a single PDF file





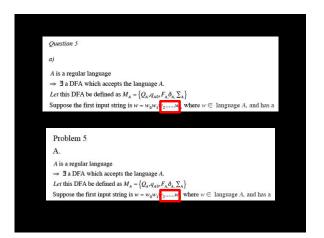
#### **Collaboration + Cheating**

You may NOT share written work

You may NOT use Google (or other search engines)

You may NOT use solutions to previous years' homework.

You MUST sign the class honor code



#### **Textbook**

There is NO textbook for this class

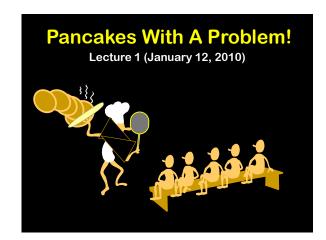
We have class notes in wiki format

You too can edit the wiki!!!

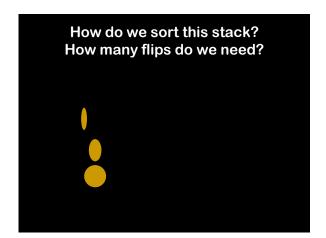


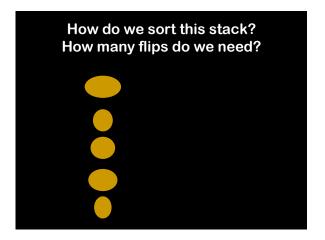
15-251

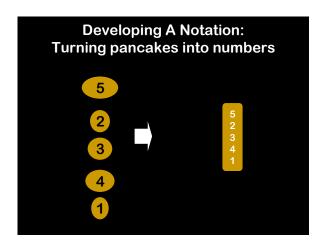
Cooking for Computer Scientists

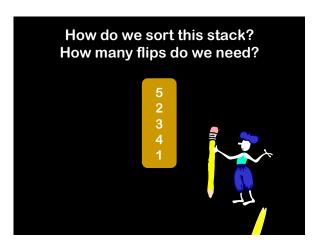




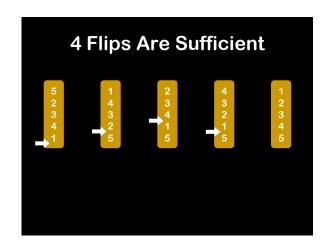


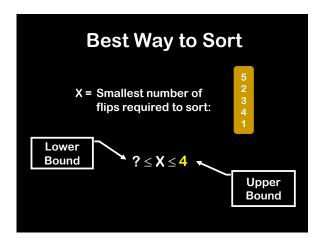


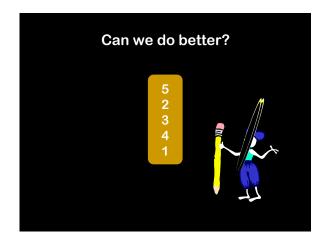


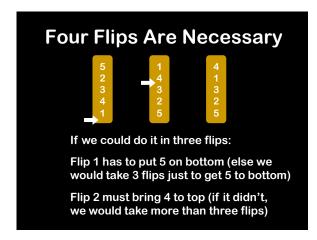


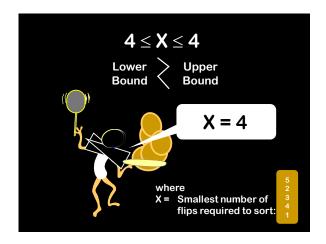


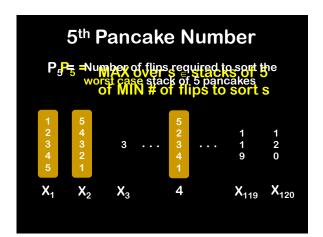


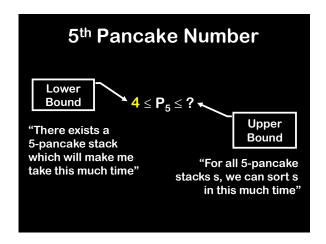


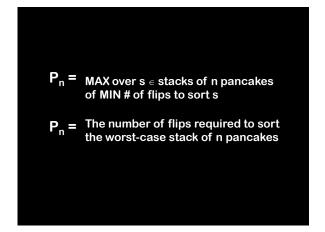


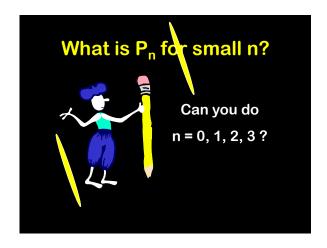


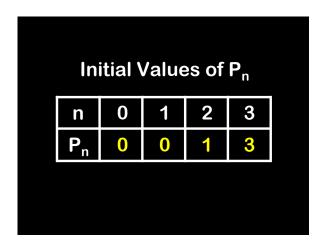


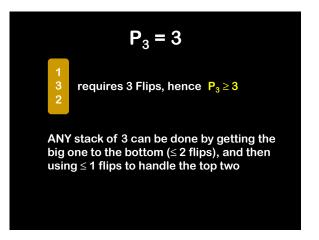


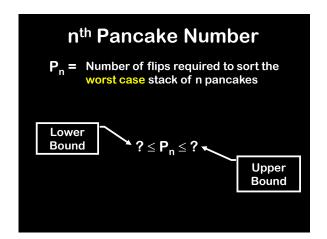


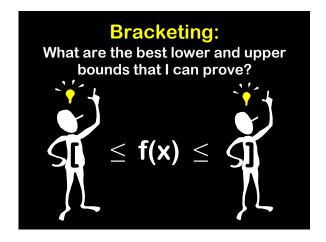


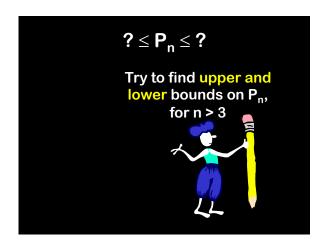




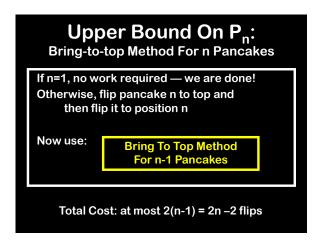


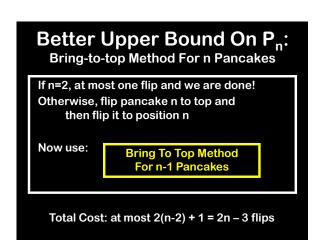


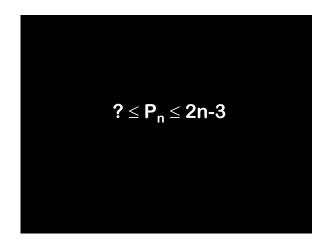


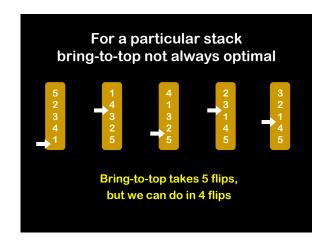


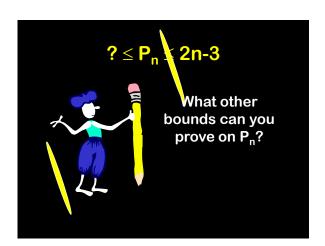


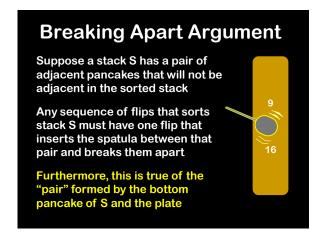


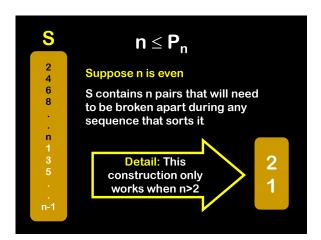


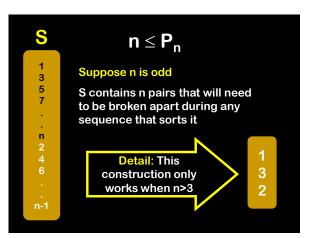


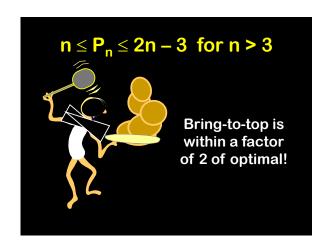


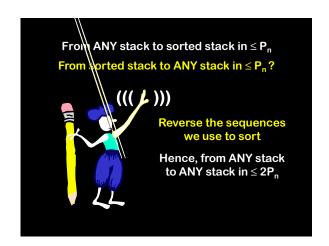




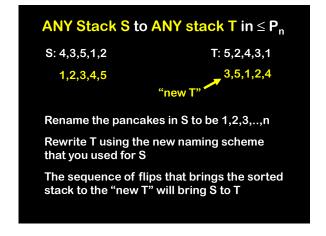


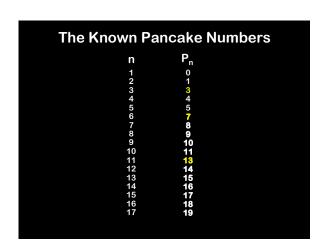




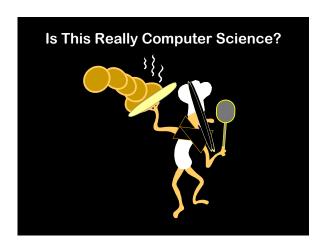


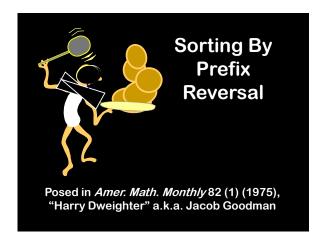


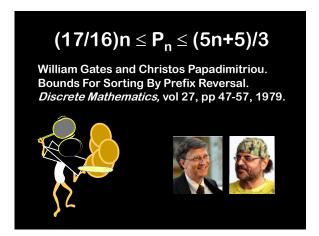


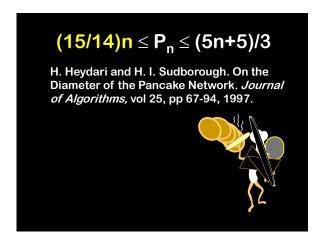


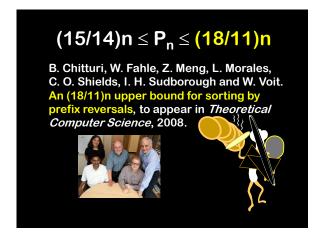
# P<sub>18</sub> is Unknown It is either 20 or 21, we don't know which. 1·2·3·4·...·17·18 = 18! orderings of 18 pancakes 18! = 6.402373 × 10<sup>15</sup> To give a lower bound of 21 (say), we would have to find one of these stacks for which no sequences of 20 swaps sort the stack.

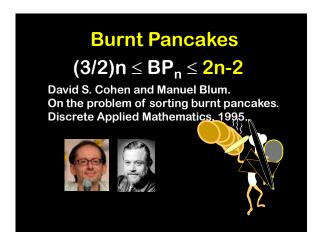












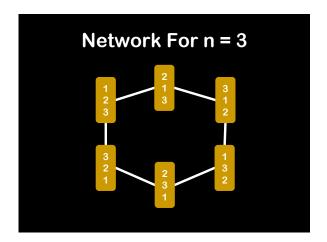
## How many different stacks of n pancakes are there?

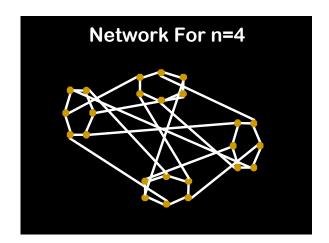
 $n! = 1 \times 2 \times 3 \times ... \times n$ 

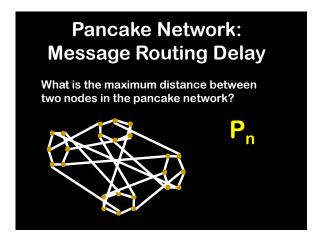
#### Pancake Network: Definition For n! Nodes

For each node, assign it the name of one of the n! stacks of n pancakes

Put a wire between two nodes if they are one flip apart



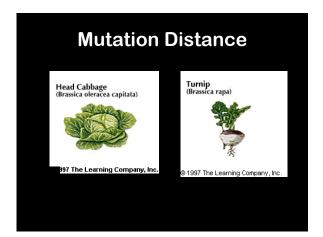


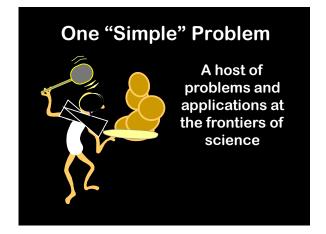


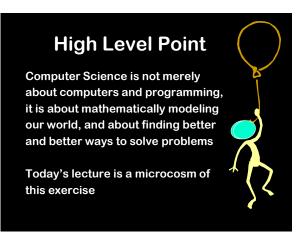
### Pancake Network: Reliability

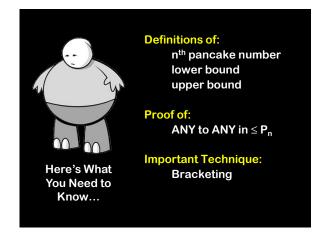
If up to n-2 nodes get hit by lightning, the network remains connected, even though each node is connected to only n-1 others

The Pancake Network is optimally reliable for its number of edges and nodes









Veit Elser's "Formidable 14"

Fit disks of the following diameters into a circular cavity of size 12.000:

2.150 2.250 2.308 2.348 2.586 2.684 2.684 2.964 2.986 3.194 3.320 3.414 3.670 3.736

The first 251 student who writes a program to solve this gets a special commendation from me!