

15-213

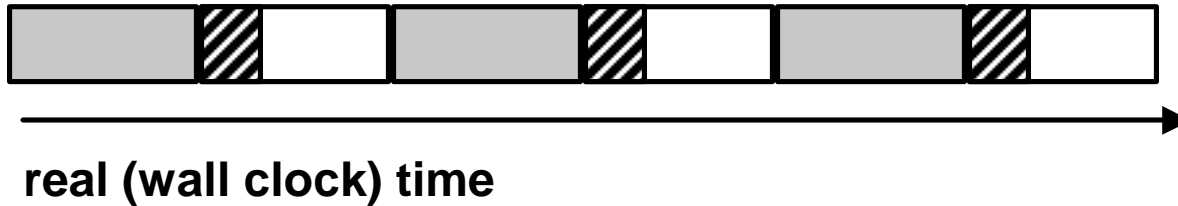
Performance Evaluation


May 2, 2000


Topics

- **Getting accurate measurements**
- **Amdahl's Law**

“Time” on a Computer System



 = **user time** (*time executing instructing instructions in the user process*)

 = **system time** (*time executing instructing instructions in kernel on behalf of user process*)

 = **some other user's time** (*time executing instructing instructions in different user's process*)

 +  +  = **real (wall clock) time**

We will use the word “time” to refer to user time.

Time of Day Clock

- return elapsed time since some reference time (e.g., Jan 1, 1970)
- example: Unix `gettimeofday()` command
- coarse grained (e.g., ~3msec resolution on Linux, 10 msec resolution on Windows NT)
 - Lots of overhead making call to OS
 - Different underlying implementations give different resolutions

```
#include <sys/time.h>
#include <unistd.h>

struct timeval tstart, tfinish;
double tsecs;
gettimeofday(&tstart, NULL);
P();
gettimeofday(&tfinish, NULL);
tsecs = (tfinish.tv_sec - tstart.tv_sec) +
        1e6 * (tfinish.tv_usec - tstart.tv_usec);
```

Interval (Count-Down) Timers

- set timer to some initial value
- timer counts down toward zero
- coarse grained (e.g., 10 msec resolution on Linux)

```
void init_etime() {  
    first.it_value.tv_sec  
        = 86400;  
    setitimer(ITIMER_VIRTUAL,  
              &first, NULL);  
}
```

```
double get_etime() {  
    struct itimerval curr;  
    getitimer(ITIMER_VIRTUAL, &curr);  
    return(double)(  
        (first.it_value.tv_sec -  
         curr.it_value.tv_sec) +  
        (first.it_value.tv_usec -  
         curr.it_value.tv_usec)*1e-6);  
}
```

Using the
interval timer

```
init_etime();  
secs = get_etime();  
P();  
secs = get_etime() - secs;  
printf("%lf secs\n", secs);
```

Cycle Counters

- **Most modern systems have built in registers that are incremented every clock cycle**
 - Very fine grained
 - Maintained as part of process state
 - » Save & restore with context switches
 - » Counter will reflect time spent by user process
- **Special assembly code instruction to access**
- **On (recent model) Intel machines:**
 - 64 bit counter.
 - RDTSC instruction sets `%edx` to high order 32-bits, `%eax` to low order 32-bits

Wrap Around Times for 550 MHz machine

- **Low order 32-bits wrap around every $2^{32} / (550 * 10^6) = 7.8$ seconds**
- **High order 64-bits wrap around every $2^{64} / (550 * 10^6) = 33539534679$ seconds**
 - 1065.3 years

Using the Cycle Counter

- **Example**

- Function that returns number of cycles elapsed since previous call to function
- Express as `double` to avoid overflow problems

```
/* Keep track of most recent reading of cycle counter */
static unsigned cyc_hi = 0;
static unsigned cyc_lo = 0;

static double delta_cycles()
{
    unsigned ncyc_hi, ncyc_lo;
    double result;
    /* Get cycle counter as ncyc_hi and ncyc_lo */
    . . .
    /* Do double precision subtraction */
    . . .
    cyc_hi = ncyc_hi; cyc_lo = ncyc_lo;
    return result;
}
```

Accessing the Cycle Counter (cont.)

- GCC allows inline assembly code with mechanism for matching registers with program variables
- Code only works on x86 machine compiling with GCC

```
unsigned ncyc_hi, ncyc_lo;  
/* Get cycle counter */  
asm("rdtsc\nmovl %%edx,%0\nmovl %%eax,%1"  
    : "=r" (ncyc_hi), "=r" (ncyc_lo)  
    : /* No input */  
    : "%edx", "%eax");
```

- Emit assembly with `rdtsc` and two `movl` instructions
- Code generates two outputs:
 - Symbolic register `%0` should be used for `ncyc_hi`
 - Symbolic register `%1` should be used for `ncyc_lo`
- Code has no inputs
- Registers `%eax` and `%edx` will be overwritten

Accessing the Cycle Counter (cont.)

Emitted Assembly Code

```
delta_cycles:
    pushl %ebp                # Stack stuff
    movl %esp,%ebp
    pushl %esi
    pushl %ebx
#APP
    rdtsc                    # Result of ASM Statement
    movl %edx,%esi           # Uses %esi for ncyc_hi
    movl %eax,%ecx           # Uses %ecx for ncyc_lo
#NO_APP
    movl %ecx,%ebx           # ncyc_lo
    subl cyc_lo,%ebx
    cmpl %ecx,%ebx
    seta %al
    xorl %edx,%edx
    movb %al,%dl
    movl %esi,%eax           # ncyc_hi
```

Using the Cycle Counter (cont.)

```
/* Keep track of most recent reading of cycle
counter */
static unsigned cyc_hi = 0;
static unsigned cyc_lo = 0;

static double delta_cycles()
{
    unsigned ncyc_hi, ncyc_lo;
    unsigned hi, lo, borrow;
    double result;
    . . .
    /* Do double precision subtraction */
    lo = ncyc_lo - cyc_lo;
    borrow = lo > ncyc_lo;
    hi = ncyc_hi - cyc_hi - borrow;
    result = (double) hi * (1 << 30) * 4 + lo;
    . . .
}
```

Timing with Cycle Counter

```
double tsecs;  
delta_cycles();  
P();  
tsecs = delta_cycles() / (MHZ * 1e6);
```

Measurement Pitfalls

Overhead

- Calling `delta_cycles()` incurs small amount of overhead
- Want to measure long enough code sequence to compensate

Unexpected Cache Effects

- artificial hits or misses
- e.g., these measurements were taken with the Alpha cycle counter:

```
foo1(array1, array2, array3);      /* 68,829 cycles */  
foo2(array1, array2, array3);      /* 23,337 cycles */
```

vs.

```
foo2(array1, array2, array3);      /* 70,513 cycles */  
foo1(array1, array2, array3);      /* 23,203 cycles */
```

Dealing with Overhead & Cache Effects

- Keep doubling number of times execute P() until reach some threshold
 - Used CMIN = 50000

```
int cnt = 1;
double cmeas = 0;
double cycles;
do {
    int c = cnt;
    P();                      /* Warm up cache */
    (void) delta_cycles();
    while (c-- > 0)
        P();
    cmeas = delta_cycles();
    cycles = cmeas / cnt;
    cnt += cnt;
} while (cmeas < CMIN); /* Make sure have enough */
return cycles / (1e6 * MHZ);
```

Context Switching

Context switches can also affect cache performance

- e.g., (foo1, foo2) cycles on an unloaded timing server:
 - » 71,002, 23,617
 - » 67,968, 23,384
 - » 68,840, 23,365
 - » 68,571, 23,492
 - » 69,911, 23,692

Why Do Context Switches Matter?

- Cycle counter only accumulates when running user process
- Some amount of overhead
- Caches polluted by OS and other user's code & data
 - Cold misses as restart process

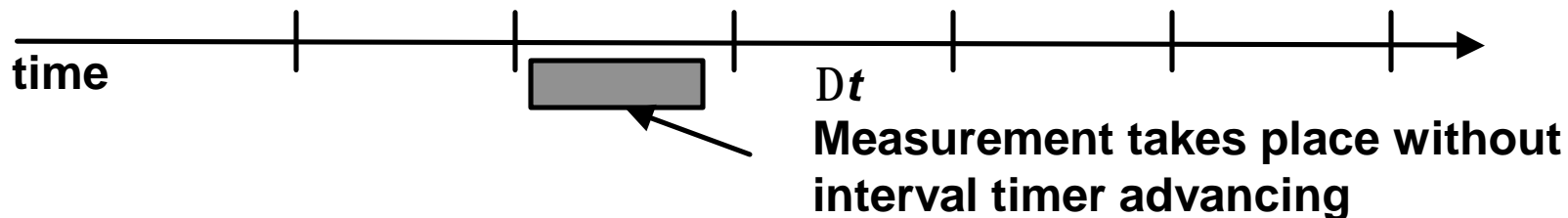
Measurement Strategy

- Try to measure uninterrupted code execution

Detecting Context Switches

Clock Interrupts

- Processor clock causes interrupt every Δt seconds
 - Typically $\Delta t = 10$ ms
 - Same as interval timer resolution



- Can detect by seeing if interval timer has advanced during measurement

```
start = get_etime();

/* Perform Measurement */
. . .
if (get_etime() - start > 0)
    /* Discard measurement */
```

Detecting Context Switches (Cont.)

External Interrupts

- E.g., due to completion of disk operation
- Occur at unpredictable times but generally take a long time to service

Detecting

- See if real time clock has advanced
 - Using coarse-grained interval timer

```
start = get_rtime();

/* Perform Measurement */
. . .
if (get_rtime() - start > 0)
    /* Discard measurement */
```

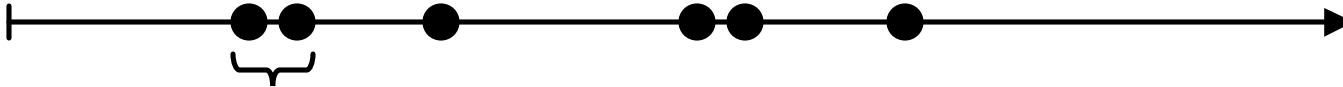
Reliability

- Good, but not 100%
- Can't get clean measurements on heavily loaded system

Improving Accuracy

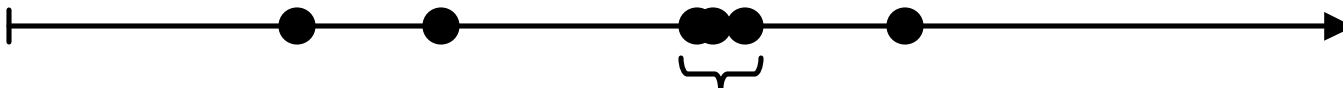
Current Timer Code

- Assume that bad measurements always overestimate time
 - True if main problem is due to context switches
- Take multiple samples (2–10) until lowest two are within some small tolerance of each other



Better Timing Code

- Erroneous measurements both under- and over-estimate time, but are not correlated to each other
- Look for clustering of times among samples



Measurement Summary

It's difficult to get accurate times

- compensating for overhead
- but can't always measure short procedures in loops
 - global state
 - mallocs
 - changes cache behavior

It's difficult to get repeatable times

- cache effects due to ordering and context switches

Moral of the story:

- Adopt a healthy skepticism about measurements!
- Always subject measurements to sanity checks.

Amdahl's Law

You plan to visit a friend in Normandy France and must decide whether it is worth it to take the Concorde SST (\$3,100) or a 747 (\$1,021) from NY to Paris, assuming it will take 4 hours Pgh to NY and 4 hours Paris to Normandy.

	time NY® Paris	total trip time	speedup over 747
747	8.5 hours	16.5 hours	1
SST	3.75 hours	11.75 hours	1.4

Taking the SST (which is 2.2 times faster) speeds up the overall trip by only a factor of 1.4!

Speedup

Old program (unenhanced)



Old time: $T = T_1 + T_2$

T_1 = time that can NOT be enhanced.

T_2 = time that can be enhanced.

New program (enhanced)



New time: $T \Leftarrow T_1 \Leftarrow T_2 \Leftarrow$

$T_2 \Leftarrow$ time after the enhancement.

Speedup: $S_{\text{overall}} = T / T \Leftarrow$

Computing Speedup

Two key parameters:

$$F_{\text{enhanced}} = T_2 / T \quad (\text{fraction of original time that can be improved})$$

$$S_{\text{enhanced}} = T_2 / T_2' \quad (\text{speedup of enhanced part})$$

$$\begin{aligned} T &= T_1 + T_2' = T_1 + T_2 / S_{\text{enhanced}} = T(1 - F_{\text{enhanced}}) + T_2 / S_{\text{enhanced}} && [\text{by def of } S_{\text{enhanced}}] \\ &= T(1 - F_{\text{enhanced}}) + T(F_{\text{enhanced}} / S_{\text{enhanced}}) && [\text{by def of } F_{\text{enhanced}}] \\ &= T((1 - F_{\text{enhanced}}) + F_{\text{enhanced}} / S_{\text{enhanced}}) \end{aligned}$$

Amdahl's Law:

$$S_{\text{overall}} = T / T' = 1 / ((1 - F_{\text{enhanced}}) + F_{\text{enhanced}} / S_{\text{enhanced}})$$

Key idea:

- Amdahl's Law quantifies the general notion of diminishing returns.
- It applies to any activity, not just computer programs.

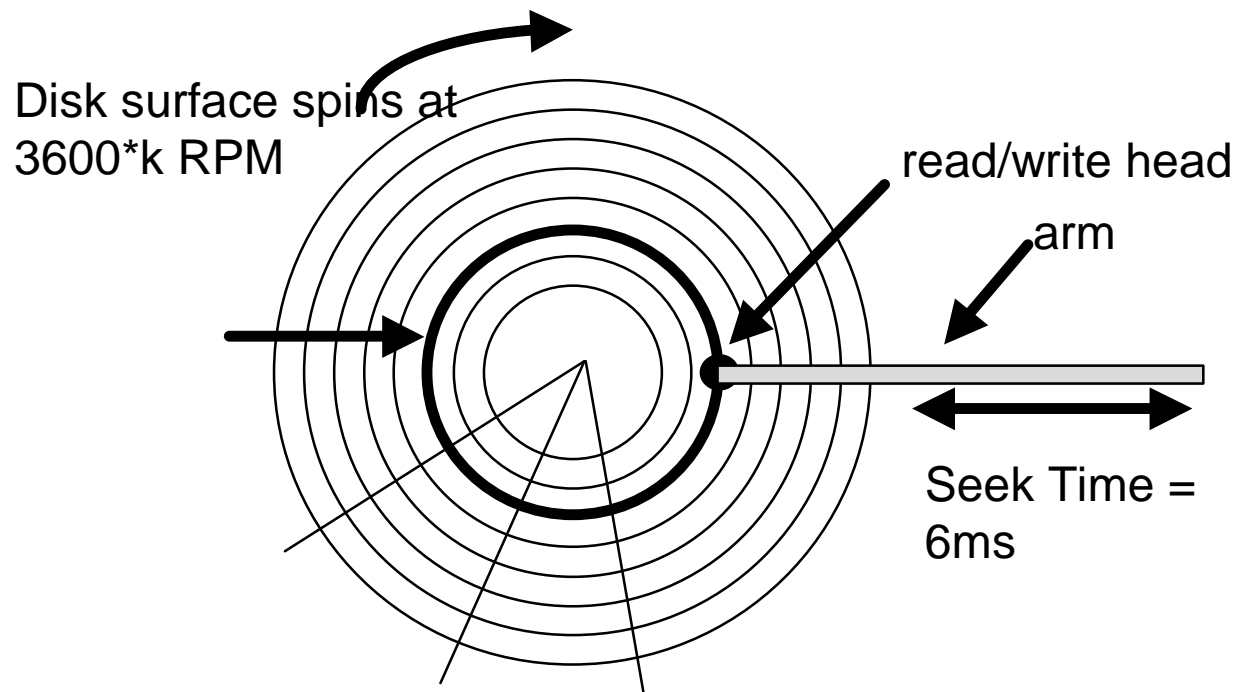
Amdahl's Law Example

Trip example:

- Suppose that for the New York to Paris leg, we now consider the possibility of taking a rocket ship (15 minutes) or a handy rip in the fabric of space-time (0 minutes):

	time NY->Paris	total trip time	speedup over 747
747	8.5 hours	16.5 hours	1
SST	3.75 hours	11.75 hours	1.4
rocket	0.25 hours	8.25 hours	2.0
rip	0.0 hours	8 hours	2.1

Magnetic Disk Example



Average Rotational Latency

- $1/2$ revolution takes $1 / (120 \cdot k)$ seconds = $8.5/k$ milliseconds

Total Latency:

- $k = 1$: 14.5 ms 1.0X
- $k = 4$: 8.1 ms 1.8X

Lesson from Amdahl's Law

Useful Corollary of Amdahl's law:

- $\frac{1}{S_{\text{overall}}} = \frac{1}{1 - F_{\text{enhanced}}}$

F_{enhanced}	Max S_{overall}	F_{enhanced}	Max S_{overall}
0.0	1	0.9375	16
0.5	2	0.96875	32
0.75	4	0.984375	64
0.875	8	0.9921875	128

Moral: It is hard to speed up a program.

Moral++ : It is easy to make premature optimizations.

Other Maxims

Second Corollary of Amdahl's law:

- When you identify and eliminate one bottleneck in a system, something else will become the bottleneck

Beware of Optimizing on Small Benchmarks

- Easy to cut corners that lead to asymptotic inefficiencies
 - E.g., Intel's string hash function