Andrew login ID:	
Recitation Section:	

# CS 15-213, Spring 2008 Exam 1

Tue. February 26, 2008

#### **Instructions:**

- Make sure that your exam is not missing any sheets, then write your full name, Andrew login ID, and recitation section (A–H) on the front.
- Write your answers in the space provided below the problem. If you make a mess, clearly indicate your final answer.
- The exam has a maximum score of 70 points.
- The problems are of varying difficulty. The point value of each problem is indicated. Pile up the easy points quickly and then come back to the harder problems.
- This exam is OPEN BOOK. You may use any books or notes you like. No calculators or other electronic devices are allowed.
- Good luck!

1 (8):
2 (8):
3 (10):
4 (9):
5 (8):
6 (8):
7 (11):
8 (8):
TOTAL (70):

## Problem 1. (8 points):

For this problem, assume the following:

- We are running code on a 6-bit machine using two's complement arithmetic for signed integers.
- short integers are encoded using 3 bits.
- Sign extension is performed whenever a short is casted to an int
- Right shifts of ints are arithmetic.

Fill in the empty boxes in the table below. The following definitions are used in the table:

```
int a = -29;
short b = (short)a;
unsigned ua = a;
int x = -21;
short y = (short)x;
unsigned ux = x;
```

Note: You need not fill in entries marked with "—".

Expression	Decimal Representation	Binary Representation
_	27	
_		100100
x		
У		
ux		
a >> 2		
ua >> 2		
b << 1		
-TMin		

# Problem 2. (8 points):

#### Part A

Fill in the blanks in the table below with the number described in the first column of each row. You can give your answers as unexpanded simple arithmetic expressions (such as  $15^{213} + 42$ ); you should not have trouble fitting your answers into the space provided.

Description	Number
<pre>int x=1; float *f = (float *)&amp;x What is the value of *f?</pre>	
int $x=-1$ ; float $*f = (float *)&x$ ; What is the value of $*f$ ?	
Smallest positive integer that cannot be represented as a 32-bit float	

#### Part B

Assume we are running code on an IA32 machine, which has a 32-bit word size and uses two's complement arithmetic for signed integers. Consider the following definition:

int 
$$x = foo();$$

Fill in the empty boxes in the table below. For each of the C expressions in the first column, either:

- State that it is true of all argument values, or
- Give an example where it is not true.

Puzzle	True / Counterexample
x < 0 ⇒ -x > 0	
x ^ ~x < 0	
$(x^{(x)} (x) > 31)) + 1 > 0$	
(((!!x) << 31) >> 31) & x == x	

# Problem 3. (10 points):

Consider an 8-bit IEEE floating-point representation with:

- 1 sign bit
- 3 exponent bits (therefore the bias  $B = 2^{3-1} 1 = 3$ )
- 4 mantissa bits
- A. Fill in the blanks in the following table. Express numerical values as fractions (e.g., 277/512).

Number	Bit representation
3/8	
$-\infty$	
9/2	
	0 010 0101
	1 000 1000
	0 111 0010

- B. Give the bit representation and numerical value of the largest number representable in this format as a *denormalized* floating-point number.
- C. Give the bit representation and numerical value of the largest number representable in this format as a *normalized* floating-point number.

## Problem 4. (9 points):

Consider the following x86-64 assembly code:

```
# on entry: %rdi = n, %rsi = A
000000000040056e <bar>:
  40056e:
                 41 b8 00 00 00 00
                                                  $0x0,%r8d
                                           mov
                 41 b9 00 00 00 00
  400574:
                                           mov
                                                  $0x0,%r9d
                 41 39 f9
  40057a:
                                           cmp
                                                  %edi,%r9d
  40057d:
                 7d 30
                                                  4005af < bar + 0x41 >
                                           jge
  40057f:
                 ba 00 00 00 00
                                                  $0x0, %edx
                                           mov
                 39 fa
  400584:
                                           cmp
                                                  %edi,%edx
  400586:
                 7d 1f
                                                  4005a7 <bar+0x39>
                                           jge
                 49 63 c1
  400588:
                                           movslq %r9d, %rax
  40058b:
                 48 8b 0c c6
                                           mov
                                                  (%rsi,%rax,8),%rcx
                 48 63 c2
                                           movslq %edx, %rax
  40058f:
                 8b 04 81
  400592:
                                           mov
                                                  (%rcx,%rax,4),%eax
                 41 Of af c1
  400595:
                                           imul
                                                  %r9d,%eax
  400599:
                 Of af c2
                                           imul
                                                  %edx, %eax
  # Instruction "cltq" is equivalent to "movslq %eax, %rax"
  40059c:
                 48 98
                                           cltq
  40059e:
                 49 01 c0
                                           add
                                                  %rax,%r8
  4005a1:
                 ff c2
                                           inc
                                                  %edx
                 39 fa
  4005a3:
                                           cmp
                                                  %edi,%edx
  4005a5:
                 7c e8
                                           jl
                                                  40058f <bar+0x21>
  4005a7:
                 41 ff c1
                                           inc
                                                  %r9d
                 41 39 f9
  4005aa:
                                                  %edi,%r9d
                                           cmp
  4005ad:
                 7c d0
                                           jl
                                                  40057f < bar + 0x11 >
                 4c 89 c0
  4005af:
                                                  %r8,%rax
                                           mov
  4005b2:
                 c3
                                           retq
```

Fill in BOTH of the blanks below for the corresponding C code.

## Problem 5. (8 points):

Consider the C code below, where H and J are constants declared with #define.

```
int array1[H][J];
int array2[J][H];
int copy_array(int x, int y) {
    array2[y][x] = array1[x][y];
    return 1;
}
```

Suppose the above C code generates the following x86-64 assembly code:

```
# On entry:
    edi = x
#
    esi = y
copy_array:
   movslq %edi,%rdi
   movslq %esi,%rsi
          %rdi, %rax
   movq
          (%rsi,%rsi,8), %rdx
   leaq
           $5, %rax
   salq
   subq
          %rdi, %rax
          %rdi, %rdx
   addq
   leaq
          (%rsi,%rax,2), %rax
           array1(,%rax,4), %eax
   movl
           %eax, array2(,%rdx,4)
   movl
   movl
           $1, %eax
   ret
```

What are the values of H and J?

H =

## Problem 6. (8 points):

Consider the following data structure declaration:

```
struct node{
 char x;
  int array[2];
  int idx;
 struct node *next;
};
Below are given four C functions and four x86-64 code blocks.
  char *mon(struct node *ptr){
    return &ptr->x;
                                          movl
                                                 8(%rdi), %eax
                                          movl
                                                 %eax, 12(%rdi)
  int tue(struct node *ptr){
    return ptr->array[ptr->idx];
  }
                                                 %rdi, %rax
                                          movq
  void wed(struct node *ptr){
                                          movq 16(%rdi), %rax
    ptr->idx = ptr->array[1];
                                          movsbl (%rax),%eax
    return;
  }
                                          movslq 12(%rdi),%rax
  char thu(struct node *ptr){
                                          movl 4(%rdi,%rax,4), %eax
    ptr = ptr->next;
    return ptr->x;
```

In the following table, next to the name of each x86-64 code block, write the name of the C function that it implements.

Code Block	<b>Function Name</b>
А	
В	
С	
D	

# Problem 7. (11 points):

The next problem concerns code generated by GCC for a function involving a switch statement. The code uses a jump to index into the jump table:

```
400518: ff 24 d5 40 06 40 00 jmpg *0x400640(,%rdx,8)
```

Using GDB, we extract the 8-entry jump table as:

```
0x400640:
              0 \times 0000000000400527
0x400648:
              0x000000000400525
0x400650:
              0x000000000400531
0x400658:
              0x00000000040051f
0x400660:
              0 \times 0000000000400525
0x400668:
              0 \times 0000000000400525
0x400670:
              0 \times 000000000040052a
0x400678:
              0x000000000400531
```

The following block of disassembled code implements the branches of the switch statement:

```
# on entry: %rdi = a, %rsi = b, %rdx = c
  400510: 31 c0
                                 xor
                                        %eax,%eax
  400512: 48 83 fa 07
                                        $0x7,%rdx
                                 cmp
  400516: 77 0d
                                        400525 <_Z4testlll+0x15>
                                 ja
  400518: ff 24 d5 40 06 40 00
                                        *0x400640(,%rdx,8)
                                 jmpq
  40051f: 48 89 f0
                                 mov
                                        %rsi,%rax
                                        %rdi,%rax
  400522: 48 29 f8
                                 sub
  400525: f3 c3
                                 repz retq # repz is a no-op here
  400527: 48 01 f7
                                        %rsi,%rdi
                                 add
  40052a: 48 89 f8
                                        %rdi,%rax
                                 mov
  40052d: 48 31 f0
                                        %rsi,%rax
                                 xor
  400530: c3
                                 retq
  400531: 48 8d 46 2a
                                 lea
                                        0x2a(%rsi),%rax
  400535: c3
                                 retq
```

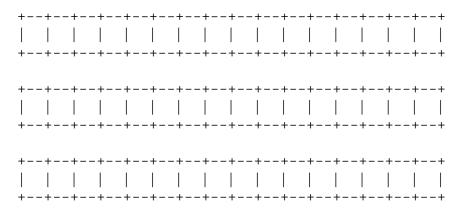
Fill in the blank portions of C code below to reproduce the function corresponding to this object code. You can assume that the first entry in the jump table is for the case when c equals 0.

```
long test(long a, long b, long c)
 long answer = ____;
 switch(c)
   case ___:
     answer = ____;
     break;
    case ___:
   case ___:
     answer = ____;
     break;
    case ___:
     /* Fall through */
    case ___:
     answer = ____;
     break;
   default:
     answer = ____;
  }
 return answer;
```

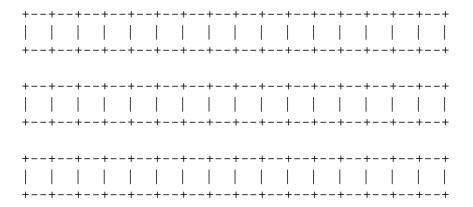
# Problem 8. (8 points):

```
struct BOOKLIST {
    char a;
    short US;
    char b;
    short CA;
    char c;
    double EU;
    char d;
    int UK;
} booklist;
```

A. Show how the struct above would appear on a 32 bit Windows machine (primitives of size k are k byte aligned). Label the bytes that belong to the various fields with their names and clearly mark the end of the struct. Use hatch marks to indicate bytes that are allocated in the struct but are not used.



B. Rearrange the above fields in booklist to conserve the most space in the memory below. Label the bytes that belong to the various fields with their names and clearly mark the end of the struct. Use hatch marks to indicate bytes that are allocated in the struct but are not used.



- C. How many bytes of the struct are wasted in part A?
- D. How many bytes of the struct are wasted in part B? Page 10 of 10