

15-213

“The course that gives CMU its Zip!”

Structured Data:

Sept. 20, 2001

Topics

- Arrays
- Structs
- Unions

Basic Data Types

Integral

- Stored & operated on in general registers
- Signed vs. unsigned depends on instructions used

Intel	GAS	Bytes	C
byte	b	1	[unsigned] char
word	w	2	[unsigned] short
double word	l	4	[unsigned] int

Floating Point

- Stored & operated on in floating point registers

Intel	GAS	Bytes	C
Single	s	4	float
Double	l	8	double
Extended	t	10/12	long double

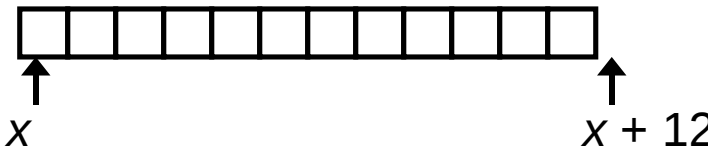
Array Allocation

Basic Principle

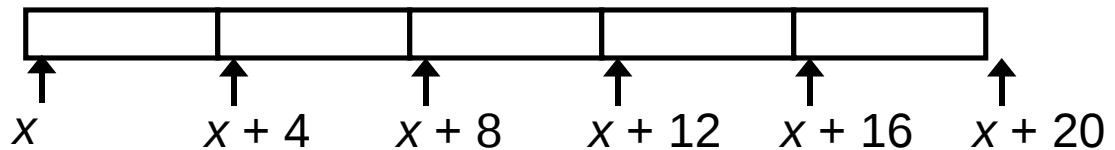
T $A[L];$

- Array of data type T and length L
- Contiguously allocated region of $L * \text{sizeof}(T)$ bytes

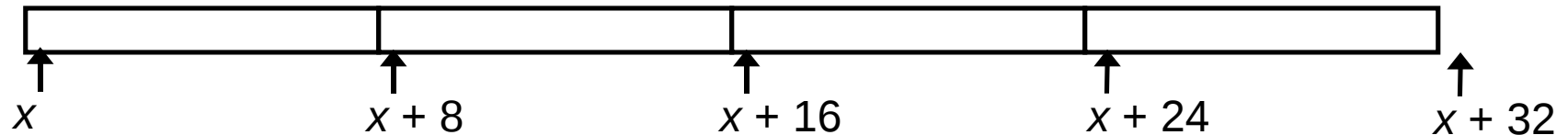
`char string[12];`



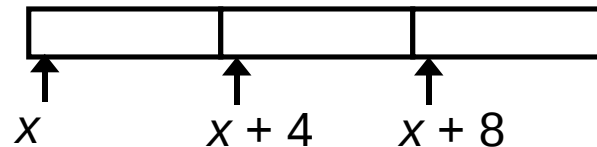
`int val[5];`



`double a[4];`



`char *p[3];`

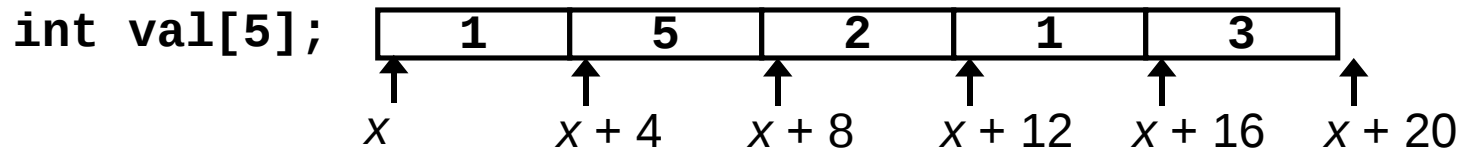


Array Access

Basic Principle

T $A[L]$;

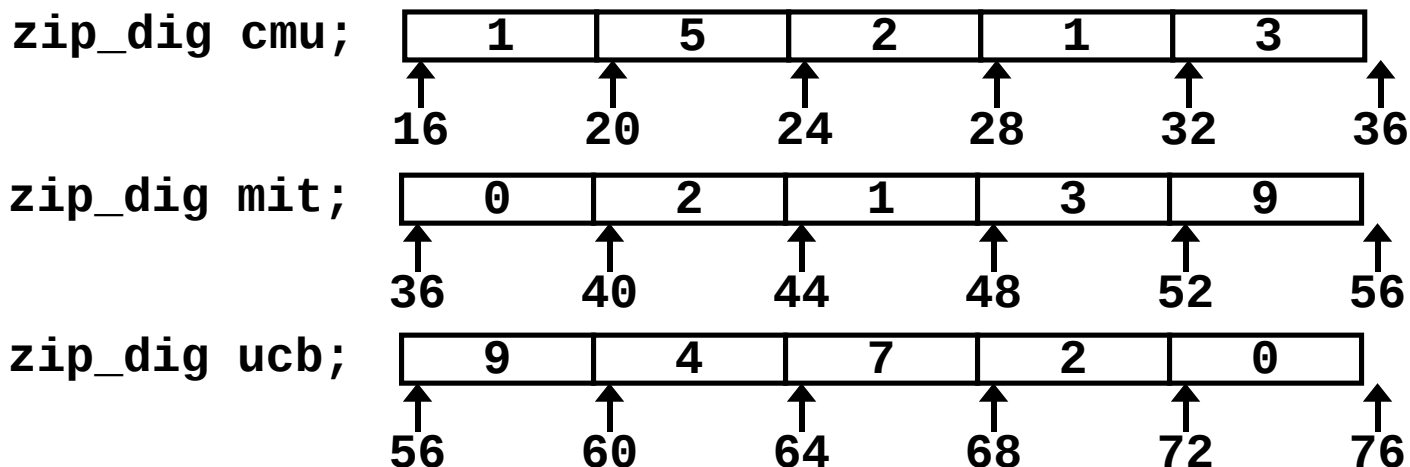
- Array of data type T and length L
- Identifier A can be used as a pointer to starting element of the array



Reference	Type	Value
<code>val[4]</code>	<code>int</code>	3
<code>val</code>	<code>int *</code>	x
<code>val+1</code>	<code>int *</code>	$x + 4$
<code>&val[2]</code>	<code>int *</code>	$x + 8$
<code>val[5]</code>	<code>int</code>	??
<code>*(val+1)</code>	<code>int</code>	5
<code>val + i</code>	<code>int *</code>	$x + 4i$

Array Example

```
typedef int zip_dig[5];  
  
zip_dig cmu = { 1, 5, 2, 1, 3 };  
zip_dig mit = { 0, 2, 1, 3, 9 };  
zip_dig ucb = { 9, 4, 7, 2, 0 };
```



Notes

- Declaration “`zip_dig cmu`” equivalent to “`int cmu[5]`”
- Example arrays were allocated in successive 20 byte blocks
 - Not guaranteed to happen in general

Array Accessing Example

Computation

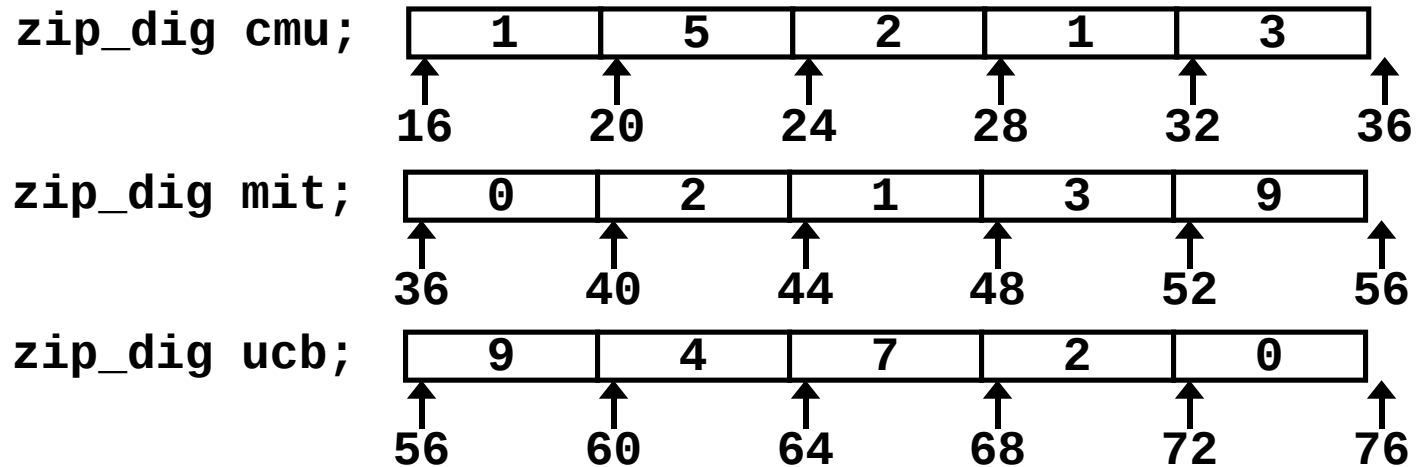
- Register `%edx` contains starting address of array
- Register `%eax` contains array index
- Desired digit at $4 * \%eax + \%edx$
- Use memory reference `(%edx,%eax,4)`

```
int get_digit
(zip_dig z, int dig)
{
    return z[dig];
}
```

Memory Reference Code

```
# %edx = z
# %eax = dig
movl (%edx,%eax,4),%eax # z[dig]
```

Referencing Examples



Code Does Not Do Any Bounds Checking!

Reference	Address	Value	Guaranteed?
<code>mit[3]</code>	$36 + 4 * 3 = 48$	3	Yes
<code>mit[5]</code>	$36 + 4 * 5 = 56$	9	No
<code>mit[-1]</code>	$36 + 4 * -1 = 32$	3	No
<code>cmu[15]</code>	$16 + 4 * 15 = 76$	??	No

- Out of range behavior implementation-dependent
 - No guaranteed relative allocation of different arrays

Array Loop Example

Original Source

```
int zd2int(zip_dig z)
{
    int i;
    int zi = 0;
    for (i = 0; i < 5; i++) {
        zi = 10 * zi + z[i];
    }
    return zi;
}
```

Transformed Version

- As generated by GCC
- Eliminate loop variable *i*
- Convert array code to pointer code
- Express in do-while form
 - No need to test at entrance

```
int zd2int(zip_dig z)
{
    int zi = 0;
    int *zend = z + 4;
    do {
        zi = 10 * zi + *z;
        z++;
    } while(z <= zend);
    return zi;
}
```

Array Loop Implementation

Registers

`%ecx` `z`
`%eax` `zi`
`%ebx` `zend`

Computations

- $10 * zi + *z$
implemented as
 $*z + 2 * (zi + 4 * zi)$
- `z++` increments by 4

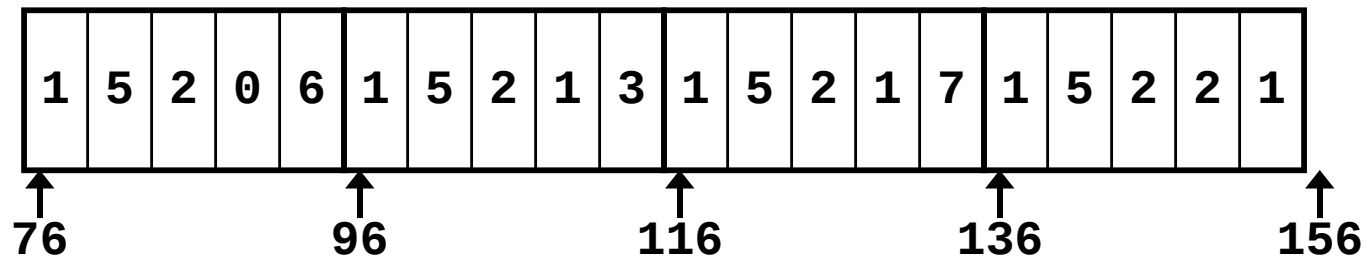
```
int zd2int(zip_dig z)
{
    int zi = 0;
    int *zend = z + 4;
    do {
        zi = 10 * zi + *z;
        z++;
    } while(z <= zend);
    return zi;
}
```

```
# %ecx = z
xorl %eax,%eax           # zi = 0
leal 16(%ecx),%ebx       # zend = z+4
.L59:
    leal (%eax,%eax,4),%edx # 5*zi
    movl (%ecx),%eax       # *z
    addl $4,%ecx           # z++
    leal (%eax,%edx,2),%eax # zi = *z + 2*(5*zi)
    cmpl %ebx,%ecx         # z : zend
    jle .L59               # if <= goto loop
```

Nested Array Example

```
#define PCOUNT 4
zip_dig pgh[PCOUNT] =
    {{1, 5, 2, 0, 6},
     {1, 5, 2, 1, 3},
     {1, 5, 2, 1, 7},
     {1, 5, 2, 2, 1}};
```

zip_dig
pgh[4];



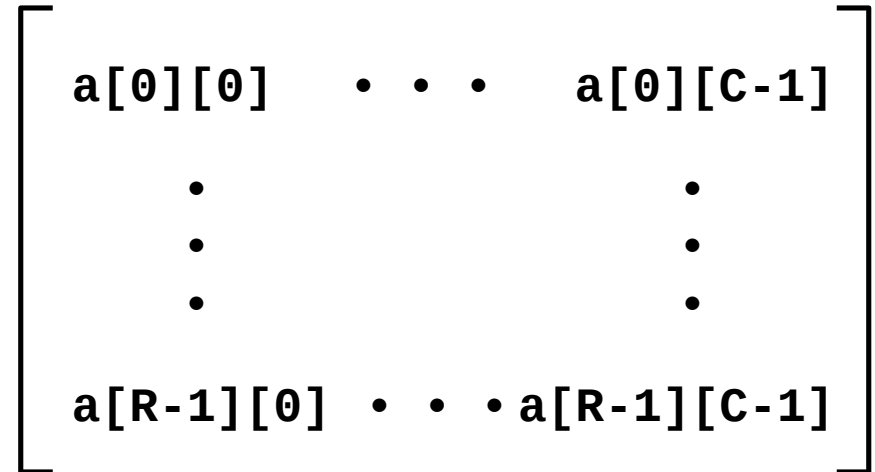
- Declaration “zip_dig pgh[4]” equivalent to “int pgh[4][5]”
 - Variable **pgh** denotes array of 4 elements
 - » Allocated contiguously
 - Each element is an array of 5 **int**’s
 - » Allocated contiguously
- “Row-Major” ordering of all elements guaranteed

Nested Array Allocation

Declaration

T $A[R][C];$

- Array of data type T
- R rows
- C columns
- Type T element requires K bytes



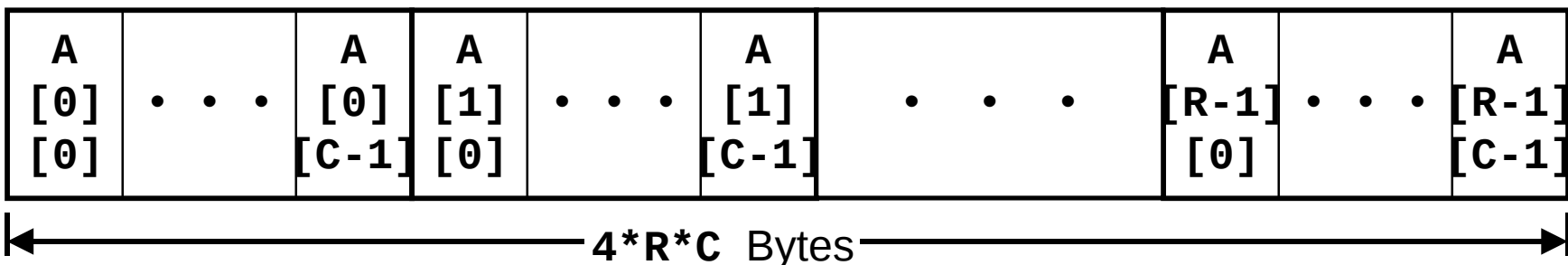
Array Size

- $R * C * K$ bytes

Arrangement

- Row-Major Ordering

`int A[R][C];`

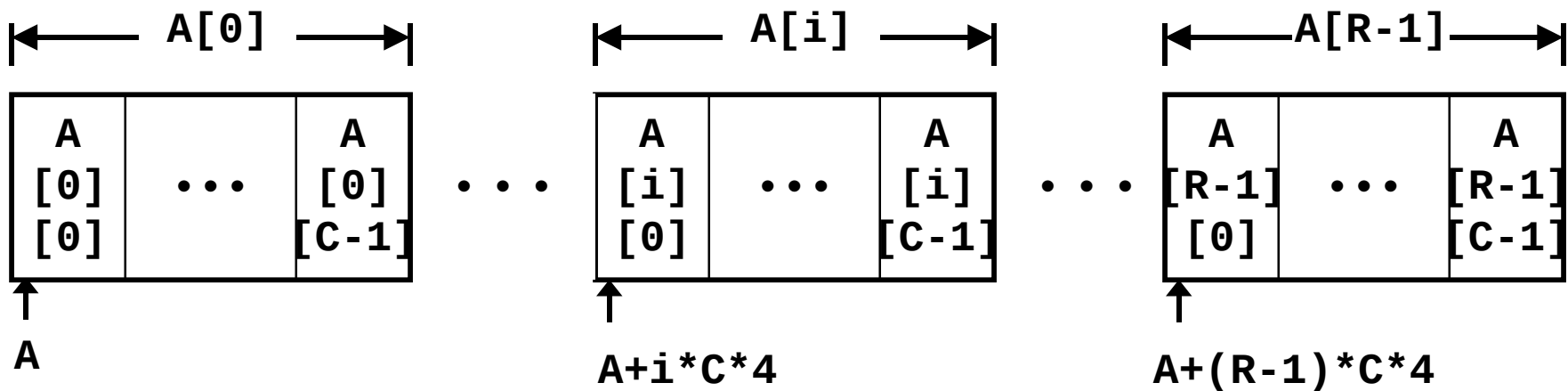


Nested Array Row Access

Row Vectors

- $A[i]$ is array of C elements
- Each element of type T
- Starting address $A + i * C * K$

```
int A[R][C];
```



Nested Array Row Access Code

```
int *get_pgh_zip(int index)
{
    return pgh[index];
}
```

Row Vector

- `pgh[index]` is array of 5 int's
- Starting address `pgh+20*index`

Code

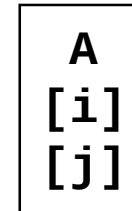
- Computes and returns address
- Compute as `pgh + 4*(index+4*index)`

```
# %eax = index
leal (%eax,%eax,4),%eax # 5 * index
leal pgh(,%eax,4),%eax  # pgh + (20 * index)
```

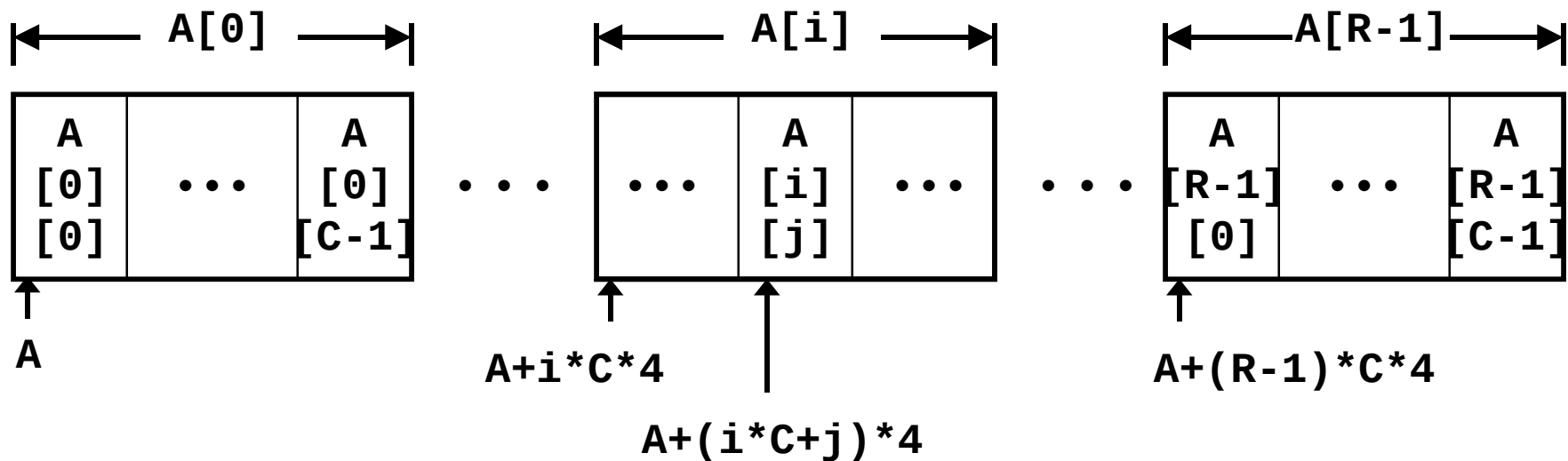
Nested Array Element Access

Array Elements

- $A[i][j]$ is element of type T
- Address $A + (i * C + j) * K$



```
int A[R][C];
```



Nested Array Element Access Code

Array Elements

- `pgh[index][dig]` is `int`
- Address:
 $\text{pgh} + 20 * \text{index} + 4 * \text{dig}$

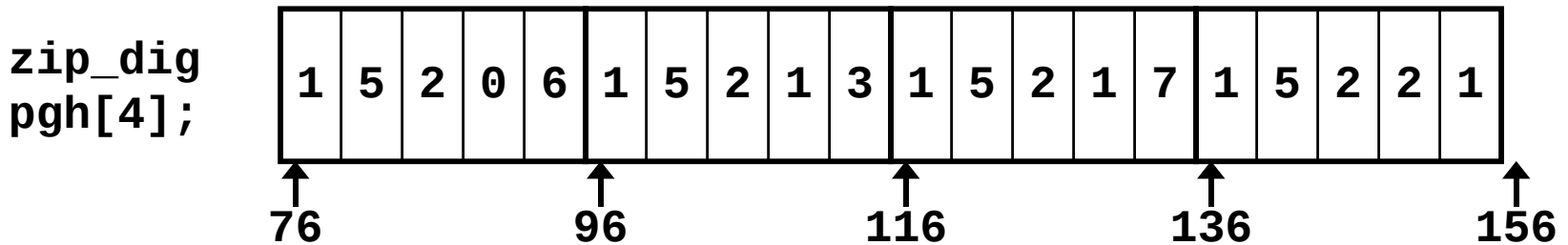
Code

- Computes address
 $\text{pgh} + 4 * \text{dig} + 4 * (\text{index} + 4 * \text{index})$
- `movl` performs memory reference

```
int get_pgh_digit
(int index, int dig)
{
    return pgh[index][dig];
}
```

```
# %ecx = dig
# %eax = index
leal 0(,%ecx,4),%edx      # 4*dig
leal (%eax,%eax,4),%eax    # 5*index
movl pgh(%edx,%eax,4),%eax # *(pgh + 4*dig + 20*index)
```

Strange Referencing Examples



Reference	Address	Value	Guaranteed?
pgh[3][3]	$76+20*3+4*3 = 148$	2	Yes
pgh[2][5]	$76+20*2+4*5 = 136$	1	Yes
pgh[2][-1]	$76+20*2+4*-1 = 112$	3	Yes
pgh[4][-1]	$76+20*4+4*-1 = 152$	1	Yes
pgh[0][19]	$76+20*0+4*19 = 152$	1	Yes
pgh[0][-1]	$76+20*0+4*-1 = 72$	??	No

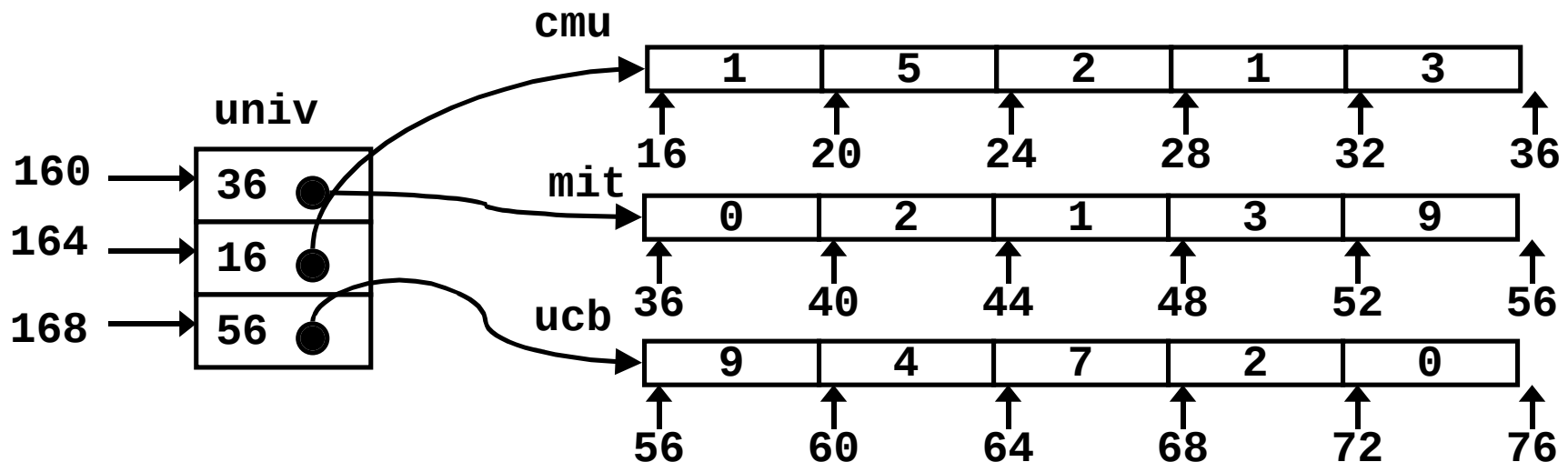
- Code does not do any bounds checking
- Ordering of elements within array guaranteed

Multi-Level Array Example

- Variable `univ` denotes array of 3 elements
– 4 bytes
- Each element is a pointer
– 4 bytes
- Each pointer points to array of `int`'s

```
zip_dig cmu = { 1, 5, 2, 1, 3 };  
zip_dig mit = { 0, 2, 1, 3, 9 };  
zip_dig ucb = { 9, 4, 7, 2, 0 };
```

```
#define UCOUNT 3  
int *univ[UCOUNT] = {mit, cmu, ucb};
```



Accessing Element in Multi-Level Array

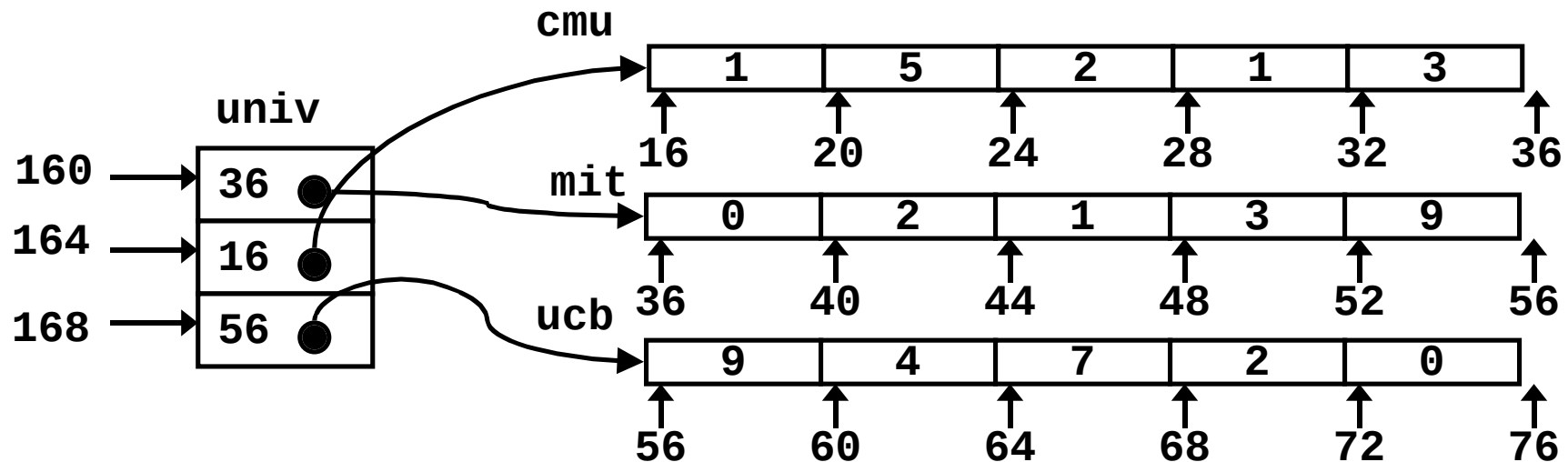
Computation

- Element access
Mem[Mem[univ+4*index]+4*dig]
- Must do two memory reads
 - First get pointer to row array
 - Then access element within array

```
int get_univ_digit
(int index, int dig)
{
    return univ[index][dig];
}
```

```
# %ecx = index
# %eax = dig
leal 0(,%ecx,4),%edx    # 4*index
movl univ(%edx),%edx    # Mem[univ+4*index]
movl (%edx,%eax,4),%eax # Mem[...+4*dig]
```

Strange Referencing Examples



Reference	Address	Value	Guaranteed?
<code>univ[2][3]</code>	$56 + 4 * 3 = 68$	2	Yes
<code>univ[1][5]</code>	$16 + 4 * 5 = 36$	0	No
<code>univ[2][-1]</code>	$56 + 4 * -1 = 52$	9	No
<code>univ[3][-1]</code>	??	??	No
<code>univ[1][12]</code>	$16 + 4 * 12 = 64$	7	No

- Code does not do any bounds checking
- Ordering of elements in different arrays not guaranteed

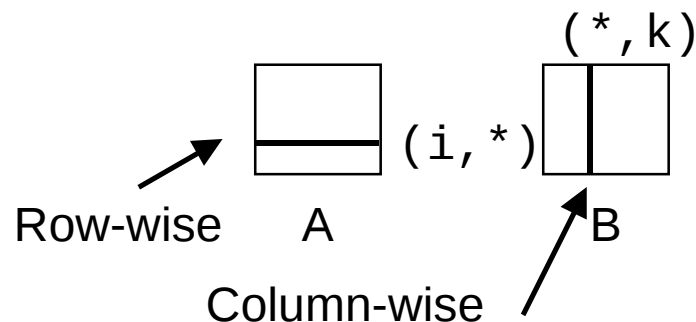
Using Nested Arrays

Strengths

- C compiler handles doubly subscripted arrays
- Generates very efficient code
 - Avoids multiply in index computation

Limitation

- Only works if have fixed array size



```
#define N 16
typedef int fix_matrix[N][N];
```

```
/* Compute element i,k of
   fixed matrix product */
int fix_prod_ele
(fix_matrix a, fix_matrix b,
 int i, int k)
{
    int j;
    int result = 0;
    for (j = 0; j < N; j++)
        result += a[i][j]*b[j][k];
    return result;
}
```

Dynamic Nested Arrays

Strength

- Can create matrix of arbitrary size

Programming

- Must do index computation explicitly

Performance

- Accessing single element costly
- Must do multiplication

```
int * new_var_matrix(int n)
{
    return (int *)
        calloc(sizeof(int), n*n);
}
```

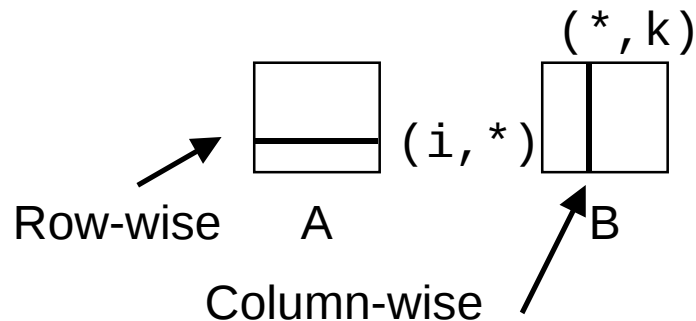
```
int var_ele
(int *a, int i,
 int j, int n)
{
    return a[i*n+j];
}
```

```
movl 12(%ebp),%eax    # i
movl 8(%ebp),%edx     # a
imull 20(%ebp),%eax   # n*i
addl 16(%ebp),%eax    # n*i+j
movl (%edx,%eax,4),%eax # Mem[a+4*(i*n+j)]
```

Dynamic Array Multiplication

Without Optimizations

- **Multiplies**
 - 2 for subscripts
 - 1 for data
- **Adds**
 - 4 for array indexing
 - 1 for loop index
 - 1 for data



```
/* Compute element i,k of
   variable matrix product */
int var_prod_ele
(int *a, int *b,
 int i, int k, int n)
{
    int j;
    int result = 0;
    for (j = 0; j < n; j++)
        result +=
            a[i*n+j] * b[j*n+k];
    return result;
}
```

Optimizing Dynamic Array Multiplication

Optimizations

- Performed when set optimization level to -O2

Code Motion

- Expression $i*n$ can be computed outside loop

Strength Reduction

- Incrementing j has effect of incrementing $j*n+k$ by n

Performance

- Compiler can optimize regular access patterns

```
{
    int j;
    int result = 0;
    for (j = 0; j < n; j++)
        result +=
            a[i*n+j] * b[j*n+k];
    return result;
}
```

```
{
    int j;
    int result = 0;
    int iTn = i*n;
    int jTnPk = k;
    for (j = 0; j < n; j++) {
        result +=
            a[iTn+j] * b[jTnPk];
        jTnPk += n;
    }
    return result;
}
```

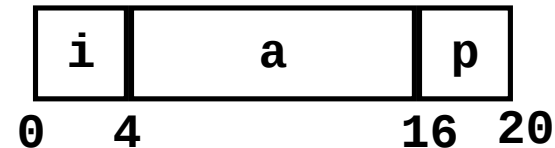
Structures

Concept

- Contiguously-allocated region of memory
- Refer to members within structure by names
- Members may be of different types

```
struct rec {  
    int i;  
    int a[3];  
    int *p;  
};
```

Memory Layout



Accessing Structure Member

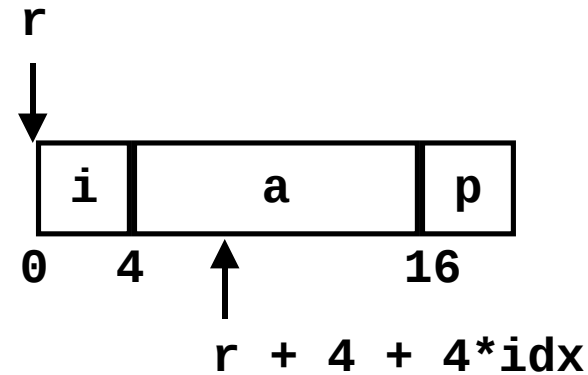
```
void  
set_i(struct rec *r,  
      int val)  
{  
    r->i = val;  
}
```

Assembly

```
# %eax = val  
# %edx = r  
movl %eax, (%edx)    # Mem[r] = val
```

Generating Pointer to Structure Member

```
struct rec {  
    int i;  
    int a[3];  
    int *p;  
};
```



Generating Pointer to Array Element

- Offset of each structure member determined at compile time

```
int *  
find_a  
(struct rec *r, int idx)  
{  
    return &r->a[idx];  
}
```

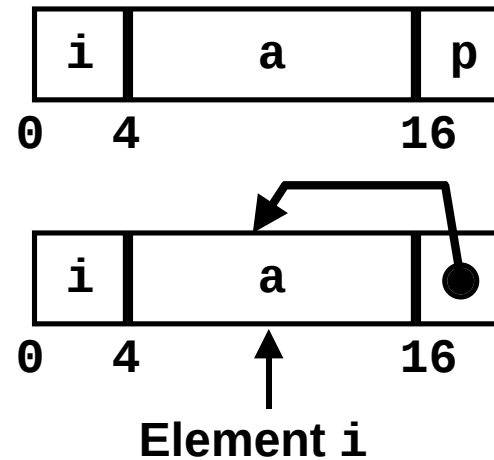
```
# %ecx = idx  
# %edx = r  
leal 0(,%ecx,4),%eax    # 4*idx  
leal 4(%eax,%edx),%eax  # r+4*idx+4
```

Structure Referencing (Cont.)

C Code

```
struct rec {  
    int i;  
    int a[3];  
    int *p;  
};
```

```
void  
set_p(struct rec *r)  
{  
    r->p =  
        &r->a[r->i];  
}
```



```
# %edx = r  
movl (%edx),%ecx      # r->i  
leal 0(,%ecx,4),%eax   # 4*(r->i)  
leal 4(%edx,%eax),%eax # r+4+4*(r->i)  
movl %eax,16(%edx)     # Update r->p
```

Alignment

Aligned Data

- Primitive data type requires K bytes
- Address must be multiple of K
- Required on some machines; advised on IA32
 - treated differently by Linux and Windows!

Motivation for Aligning Data

- Memory accessed by (aligned) double or quad-words
 - Inefficient to load or store datum that spans quad word boundaries
 - Virtual memory very tricky when datum spans 2 pages

Compiler

- Inserts gaps in structure to ensure correct alignment of fields

Specific Cases of Alignment

Size of Primitive Data Type:

- **1 byte** (e.g., char)
 - no restrictions on address
- **2 bytes** (e.g., short)
 - lowest 1 bit of address must be 0_2
- **4 bytes** (e.g., int, float, char *, etc.)
 - lowest 2 bits of address must be 00_2
- **8 bytes** (e.g., double)
 - Windows (and most other OS's & instruction sets):
 - » lowest 3 bits of address must be 000_2
 - Linux:
 - » lowest 2 bits of address must be 00_2
 - » i.e., treated the same as a 4-byte primitive data type
- **12 bytes** (long double)
 - Linux:
 - » lowest 2 bits of address must be 00_2
 - » i.e., treated the same as a 4-byte primitive data type

Satisfying Alignment with Structures

Offsets Within Structure

- Must satisfy element's alignment requirement

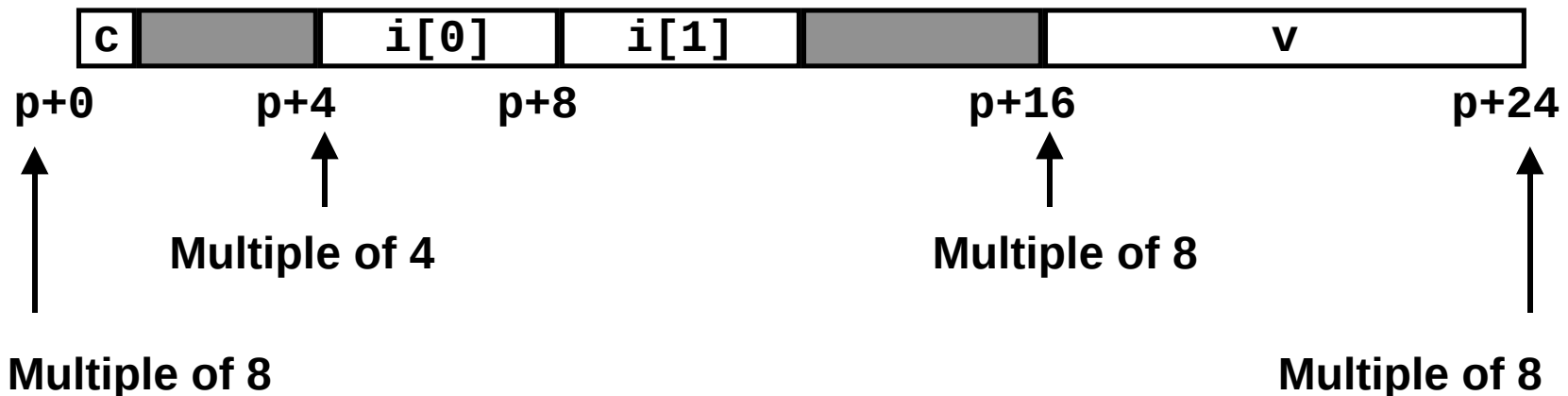
Overall Structure Placement

- Each structure has alignment requirement K
 - Largest alignment of any element
- Initial address & structure length must be multiples of K

```
struct S1 {  
    char c;  
    int i[2];  
    double v;  
} *p;
```

Example (under Windows):

- K = 8, due to double element

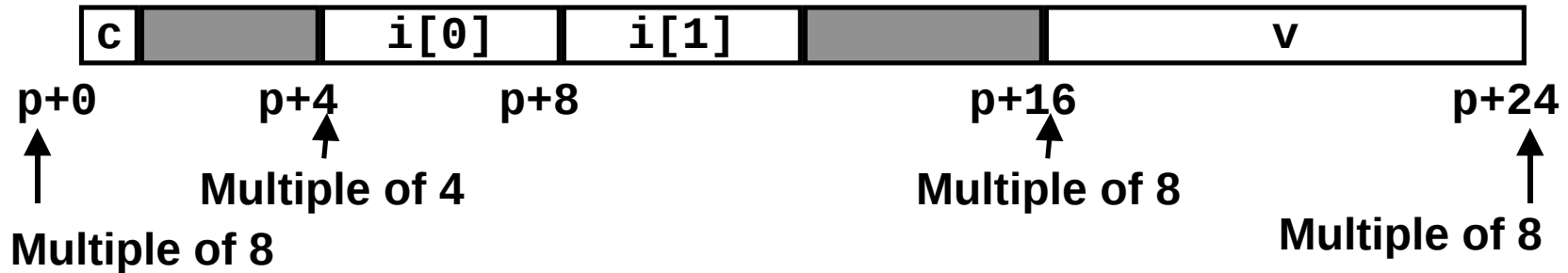


Linux vs. Windows

Windows (including Cygwin):

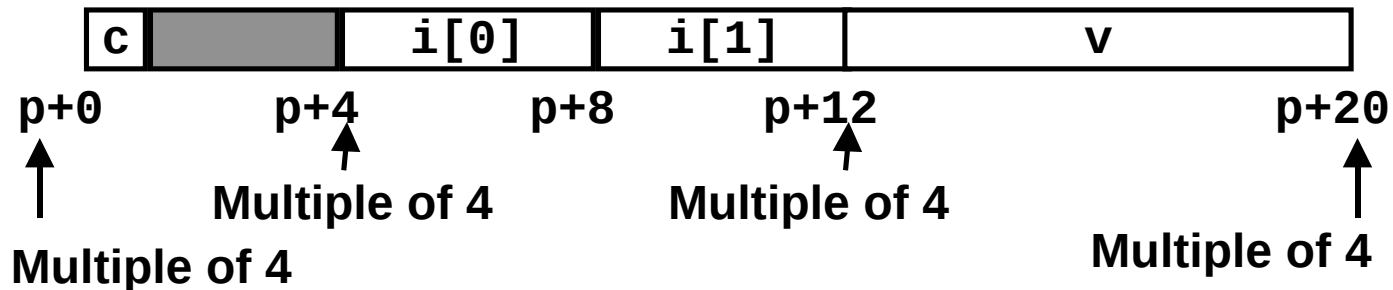
- $K = 8$, due to double element

```
struct S1 {  
    char c;  
    int i[2];  
    double v;  
} *p;
```



Linux:

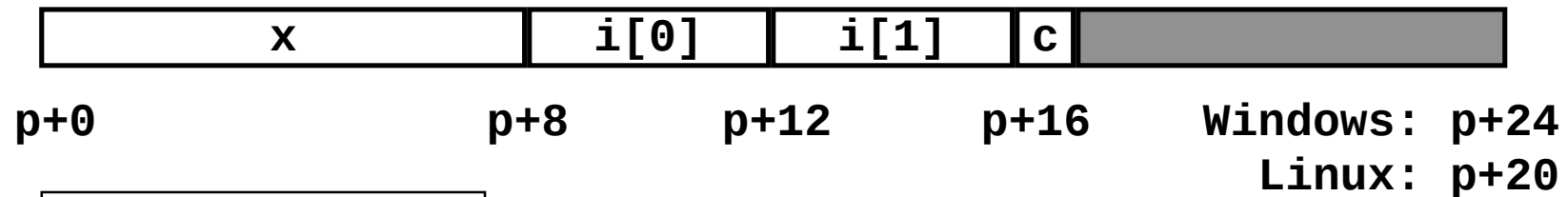
- $K = 4$; double treated like a 4-byte data type



Effect of Overall Alignment Requirement

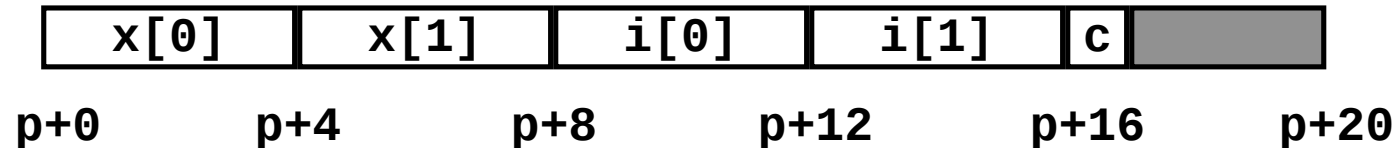
```
struct S2 {  
    double x;  
    int i[2];  
    char c;  
} *p;
```

p must be multiple of:
8 for Windows
4 for Linux



```
struct S3 {  
    float x[2];  
    int i[2];  
    char c;  
} *p;
```

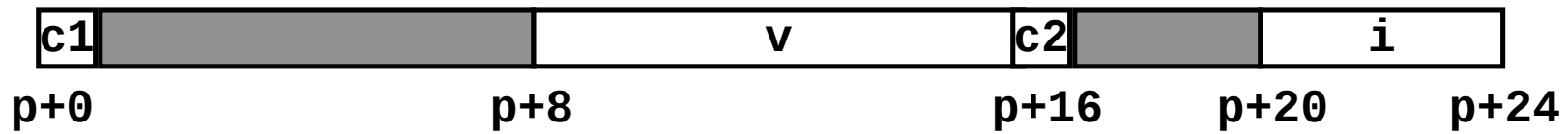
p must be multiple of 4 (in either OS)



Ordering Elements Within Structure

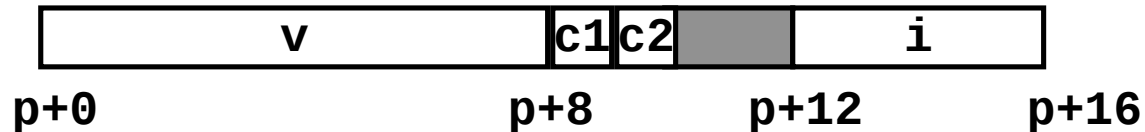
```
struct S4 {  
    char c1;  
    double v;  
    char c2;  
    int i;  
} *p;
```

10 bytes wasted space in Windows



```
struct S5 {  
    double v;  
    char c1;  
    char c2;  
    int i;  
} *p;
```

2 bytes wasted space

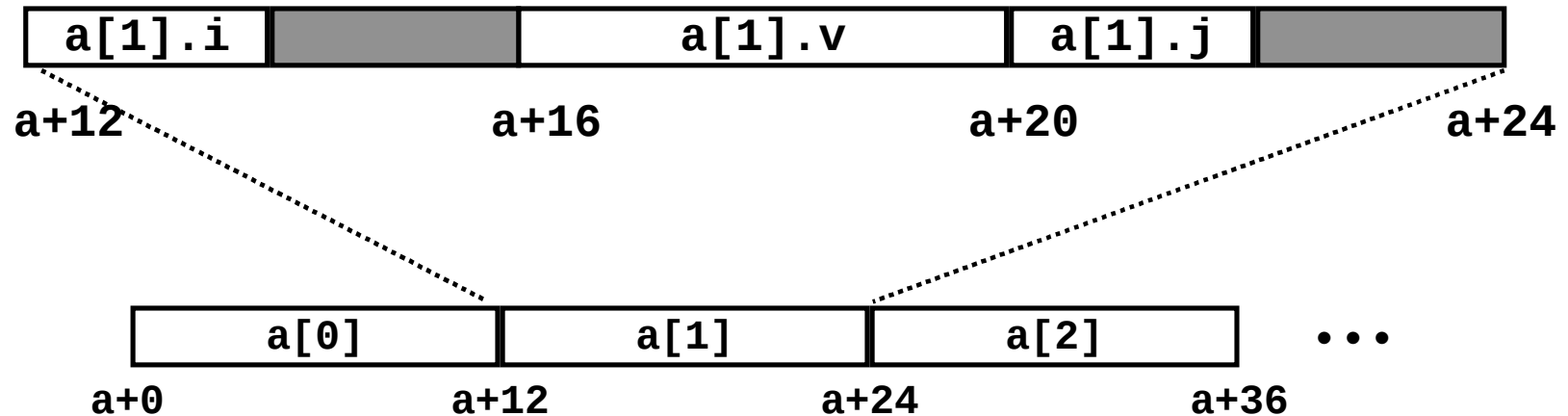


Arrays of Structures

Principle

- Allocated by repeating allocation for array type
- In general, may nest arrays & structures to arbitrary depth

```
struct S6 {  
    short i;  
    float v;  
    short j;  
} a[10];
```



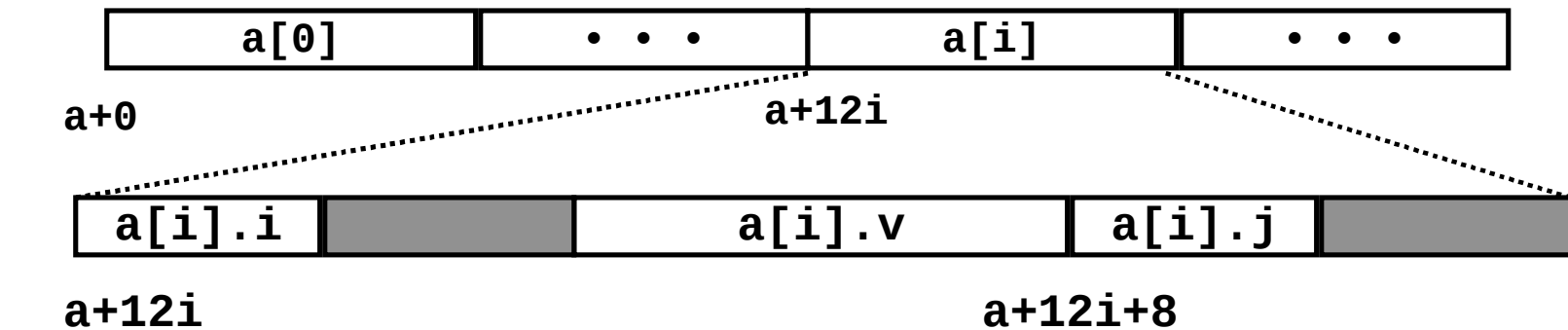
Accessing Element within Array

- Compute offset to start of structure
 - Compute $12*i$ as $4*(i+2i)$
- Access element according to its offset within structure
 - Offset by 8
 - Assembler gives displacement as $a + 8$
 - » Linker must set actual value

```
struct S6 {  
    short i;  
    float v;  
    short j;  
} a[10];
```

```
short get_j(int idx)  
{  
    return a[idx].j;  
}
```

```
# %eax = idx  
leal (%eax,%eax,2),%eax # 3*idx  
movswl a+8(,%eax,4),%eax
```

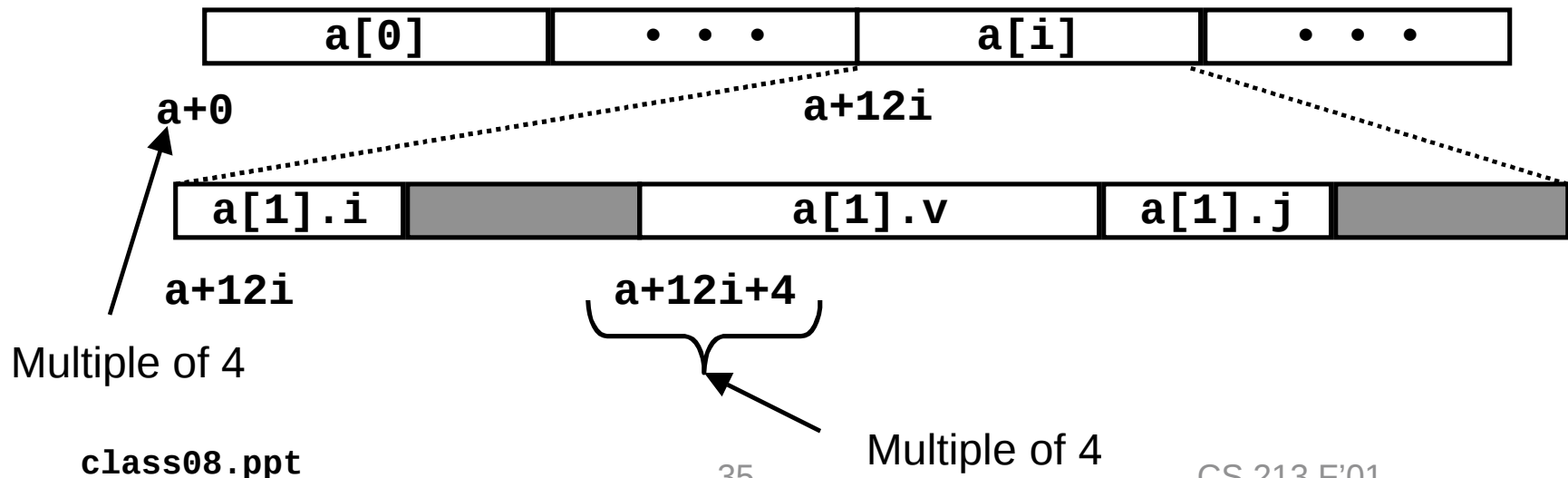


Satisfying Alignment within Structure

Achieving Alignment

- Starting address of structure array must be multiple of worst-case alignment for any element
 - a must be multiple of 4
- Offset of element within structure must be multiple of element's alignment requirement
 - v 's offset of 4 is a multiple of 4
- Overall size of structure must be multiple of worst-case alignment for any element
 - Structure padded with unused space to be 12 bytes

```
struct S6 {  
    short i;  
    float v;  
    short j;  
} a[10];
```

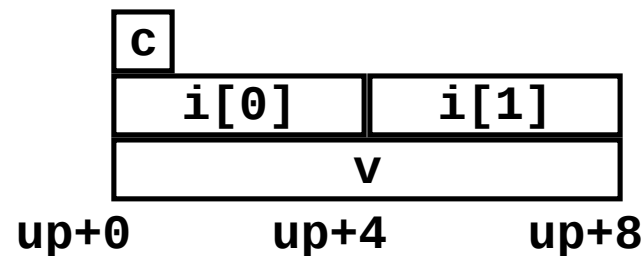


Union Allocation

Principles

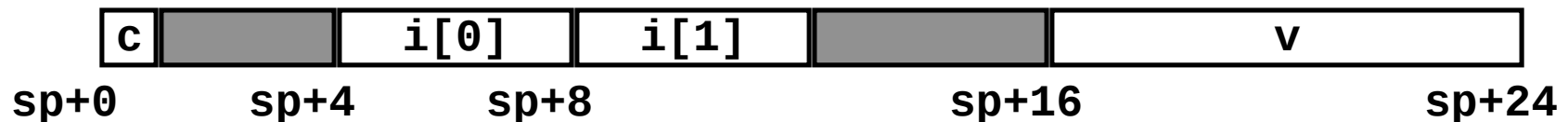
- Overlay union elements
- Allocate according to largest element
- Can only use one field at a time

```
union U1 {  
    char c;  
    int i[2];  
    double v;  
} *up;
```



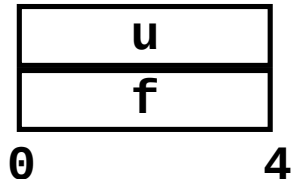
```
struct S1 {  
    char c;  
    int i[2];  
    double v;  
} *sp;
```

(Windows alignment)



Using Union to Access Bit Patterns

```
typedef union {  
    float f;  
    unsigned u;  
} bit_float_t;
```



- Get direct access to bit representation of float
- `bit2float` generates float with given bit pattern
 - NOT the same as `(float) u`
- `float2bit` generates bit pattern from float
 - NOT the same as `(unsigned) f`

```
float bit2float(unsigned u)  
{  
    bit_float_t arg;  
    arg.u = u;  
    return arg.f;  
}
```

```
unsigned float2bit(float f)  
{  
    bit_float_t arg;  
    arg.f = f;  
    return arg.u;  
}
```

Byte Ordering

Idea

- Long/quad words stored in memory as 4/8 consecutive bytes
- Which is most (least) significant?
- Can cause problems when exchanging binary data between machines

Big Endian

- Most significant byte has lowest address
- IBM 360/370, Motorola 68K, Sparc

Little Endian

- Least significant byte has lowest address
- Intel x86, Digital VAX

Byte Ordering Example

```
union {  
    unsigned char c[8];  
    unsigned short s[4];  
    unsigned int i[2];  
    unsigned long l[1];  
} dw;
```

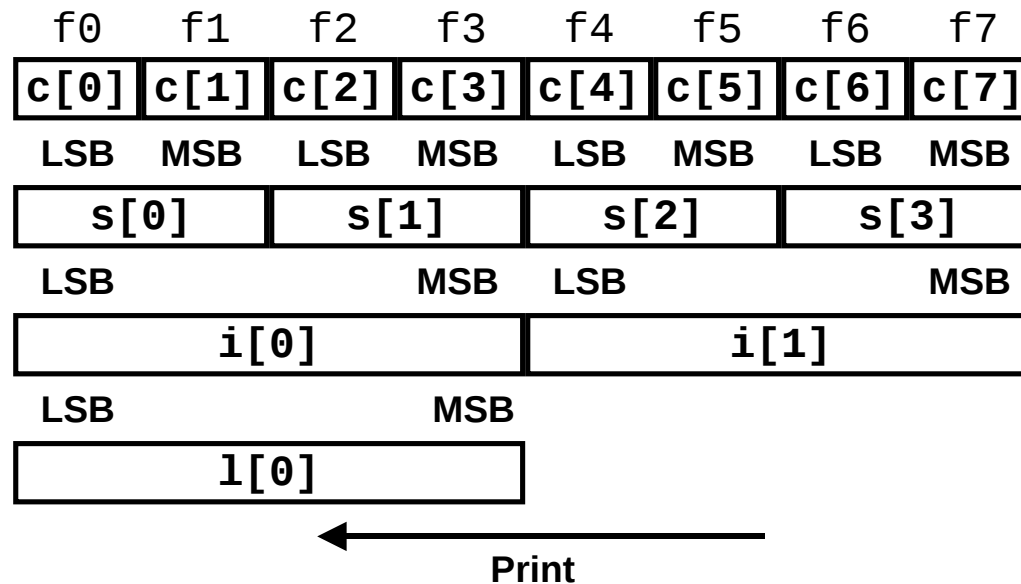
c[0]	c[1]	c[2]	c[3]	c[4]	c[5]	c[6]	c[7]
s[0]		s[1]		s[2]		s[3]	
i[0]				i[1]			
l[0]							

Byte Ordering Example (Cont).

```
int j;  
for (j = 0; j < 8; j++)  
    dw.c[j] = 0xf0 + j;  
  
printf("Characters 0-7 ==  
[0x%x, 0x%x, 0x%x, 0x%x, 0x%x, 0x%x, 0x%x, 0x%x]\n",  
       dw.c[0], dw.c[1], dw.c[2], dw.c[3],  
       dw.c[4], dw.c[5], dw.c[6], dw.c[7]);  
  
printf("Shorts 0-3 ==  
[0x%x, 0x%x, 0x%x, 0x%x]\n",  
       dw.s[0], dw.s[1], dw.s[2], dw.s[3]);  
  
printf("Ints 0-1 == [0x%x, 0x%x]\n",  
       dw.i[0], dw.i[1]);  
  
printf("Long 0 == [0x%lx]\n",  
       dw.l[0]);
```

Byte Ordering on x86

Little Endian

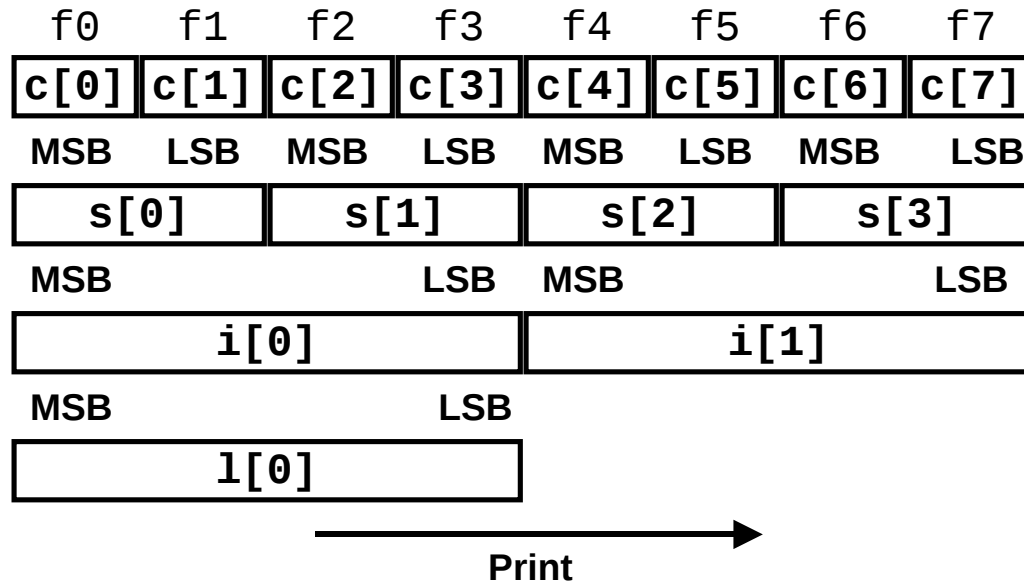


Output on Pentium:

Characters 0-7 == [0xf0,0xf1,0xf2,0xf3,0xf4,0xf5,0xf6,0xf7]
Shorts 0-3 == [0xf1f0,0xf3f2,0xf5f4,0xf7f6]
Ints 0-1 == [0xf3f2f1f0,0xf7f6f5f4]
Long 0 == [f3f2f1f0]

Byte Ordering on Sun

Big Endian

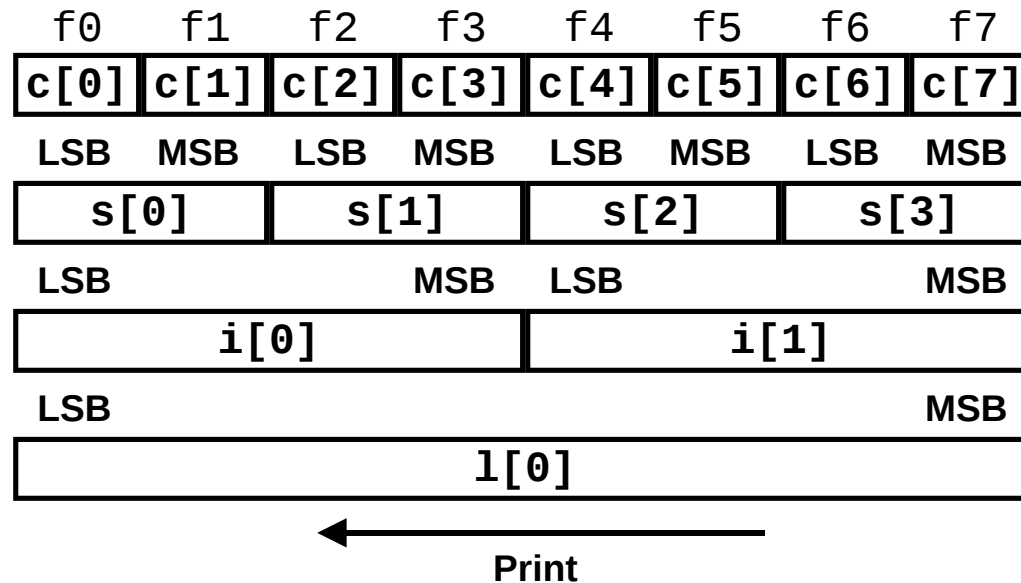


Output on Sun:

Characters 0-7 == [0xf0, 0xf1, 0xf2, 0xf3, 0xf4, 0xf5, 0xf6, 0xf7]
Shorts 0-3 == [0xf0f1, 0xf2f3, 0xf4f5, 0xf6f7]
Ints 0-1 == [0xf0f1f2f3, 0xf4f5f6f7]
Long 0 == [0xf0f1f2f3]

Byte Ordering on Alpha

Little Endian



Output on Alpha:

Characters 0-7 == [0xf0, 0xf1, 0xf2, 0xf3, 0xf4, 0xf5, 0xf6, 0xf7]
Shorts 0-3 == [0xf1f0, 0xf3f2, 0xf5f4, 0xf7f6]
Ints 0-1 == [0xf3f2f1f0, 0xf7f6f5f4]
Long 0 == [0xf7f6f5f4f3f2f1f0]

Summary

Arrays in C

- Contiguous allocation of memory
- Pointer to first element
- No bounds checking

Compiler Optimizations

- Compiler often turns array code into pointer code
`zd2int`
- Uses addressing modes to scale array indices
- Lots of tricks to improve array indexing in loops

Structures

- Allocate bytes in order declared
- Pad in middle and at end to satisfy alignment

Unions

- Overlay declarations
- Way to circumvent type system