#### 15-869

# Lecture 9 Body Representations

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Human Motion Modeling and Analysis
Fall 2012

#### Course Updates

#### Capture Project

- Now due next Monday (one week from today)

#### Final Project

- 3 minute pitches are due next class
- You should try to post your idea to the blog and get some feedback before then

#### Reading Signup

- Everyone has signed up by this point?

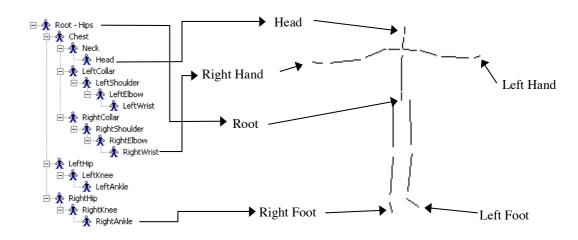
### Plan for Today's Class

- Review representation of skeleton motion
- Modeling shape and geometry of the body
  - Skinning (rigid, linear, dual quaternion)
  - Data-driven body models (SCAPE)
- Applications and discussion
  - Shape estimation from images
  - Image reshaping

Skeleton (tree hierarchy)

#### Hierarchical Structure

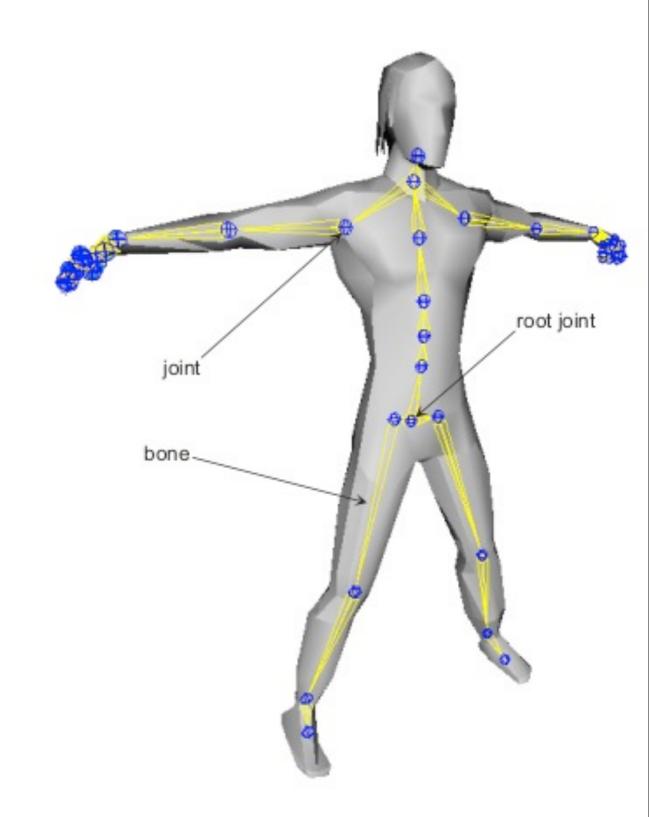
Common Data structure for Body Pose



Source: Meredith and Maddock, Motion Capture File Formats Explained

#### Skeleton (tree hierarchy)

- Nodes represent joints
- Joints are local coordinate systems (frames)
- Edges represent bones

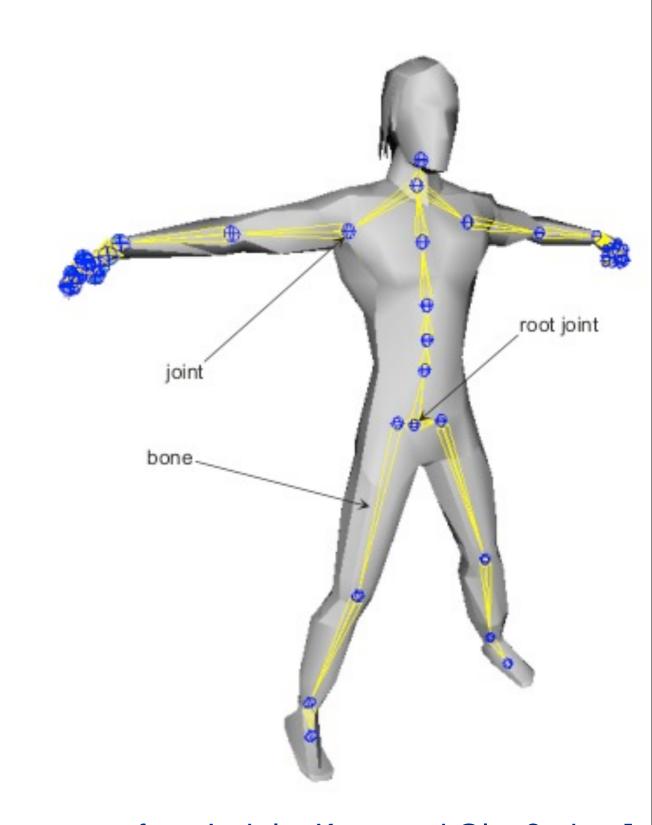


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#### Skin

- 3D model driven by the skeleton

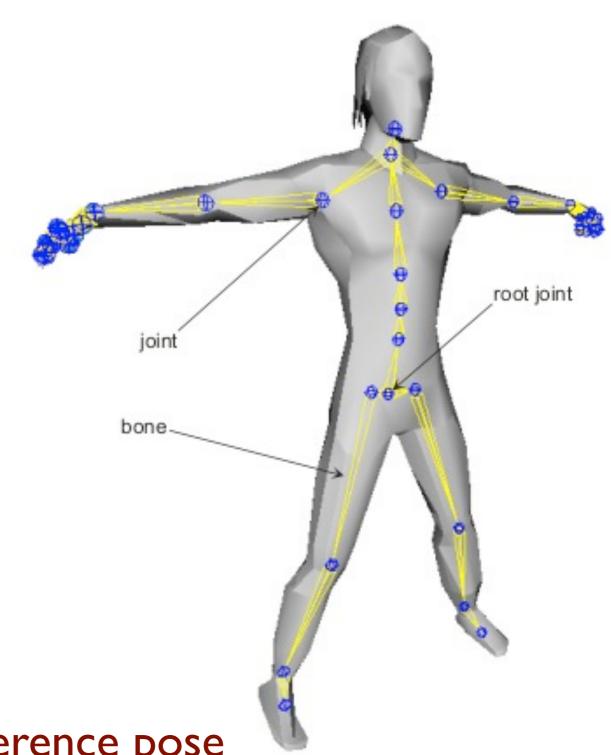


#### Skeleton (tree hierarchy)

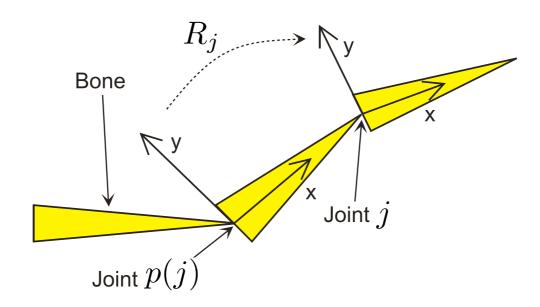
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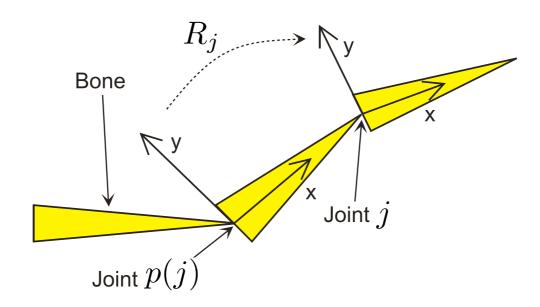


Both are typically designed in a reference pose



#### N-joint skeleton in reference frame is given by

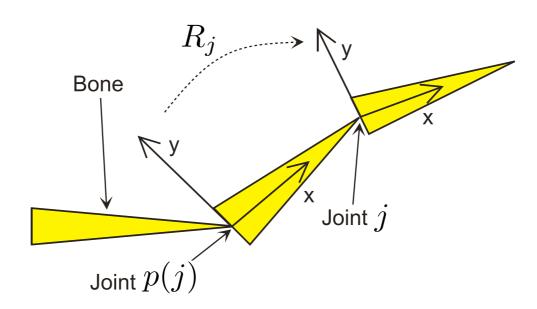
- Root frame expressed with respect to the world  $R_{
  m 0}$
- Relative joint coordinate frames  $R_1, R_2, R_3, \ldots, R_N$



#### N-joint skeleton in reference frame is given by

- Root frame expressed with respect to the world  $R_{
  m 0}$
- Relative joint coordinate frames  $R_1, R_2, R_3, \ldots, R_N$

$$R_{j} = \begin{pmatrix} r_{11} & r_{12} & r_{13} & t_{1} \\ r_{21} & r_{22} & r_{23} & t_{2} \\ r_{31} & r_{32} & r_{33} & t_{3} \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

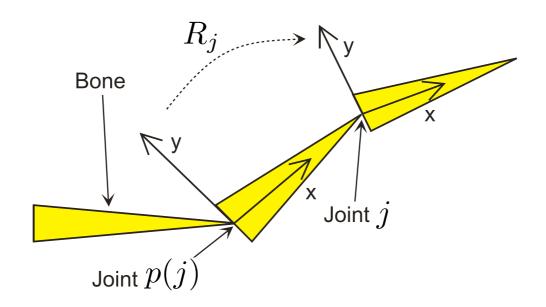


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- Root frame expressed with respect to the world  $R_{
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Mapping from world to a coordinate frame of joint j

$$A_j = R_0 \cdots R_{p(j)} R_j$$



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Mapping from world to a coordinate frame of joint j

$$A_j = R_0 \cdots R_{p(j)} R_j$$



### Animating Skeleton

#### Achieved by rotating each joint from it's reference posture

- Note: joint rotation effects the entire sub-tree (e.g., rotation at the shoulder will induce motion of the whole arm)

Rotation at joint j is described by:

$$T_j = \left( egin{array}{cccc} r_{11} & r_{12} & r_{13} & 0 \ r_{21} & r_{22} & r_{23} & 0 \ r_{31} & r_{32} & r_{33} & 0 \ 0 & 0 & 0 & 1 \end{array} 
ight)$$

### Animating Skeleton

Mapping from world to a coordinate frame of joint j in reference pose:

$$A_j = R_0 \cdots R_{p(j)} R_j$$

Mapping from world to a coordinate frame of joint j in animated pose:

$$F_j = R_0 T_0 \dots R_{p(j)} T_{p(j)} R_j T_j$$

### Animating Skeleton

Mapping from world to a coordinate frame of joint j in reference pose:

$$A_j = R_0 \cdots R_{p(j)} R_j$$

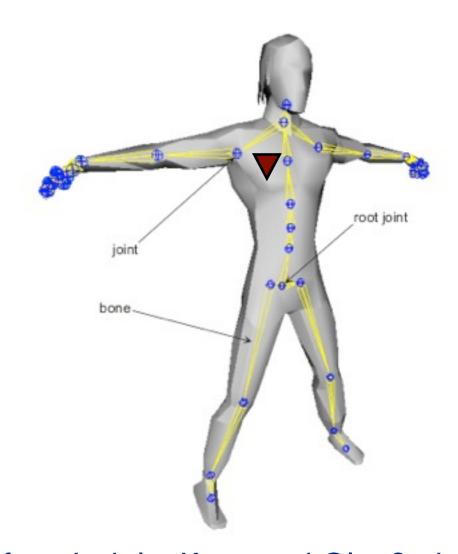
Mapping from world to a coordinate frame of joint j in animated pose:

$$F_j = R_0 T_0 \dots R_{p(j)} T_{p(j)} R_j T_j$$

Note: if 
$$T_j = I_{4\times 4}$$
 then  $F_j = A_j$ 

### Character Rigging

- I. Embed the skeleton into a 3D mesh (skin)
- 2. Assign vertices of the mesh to one or more bones to allow skin to move with the skeleton



# Rigid Skinning

I. Embed the skeleton into a 3D mesh (skin)

2. Assign vertices of the mesh to one or more bones to allow skin to move with the skeleton

Assign each vertex to one bone/joint - j

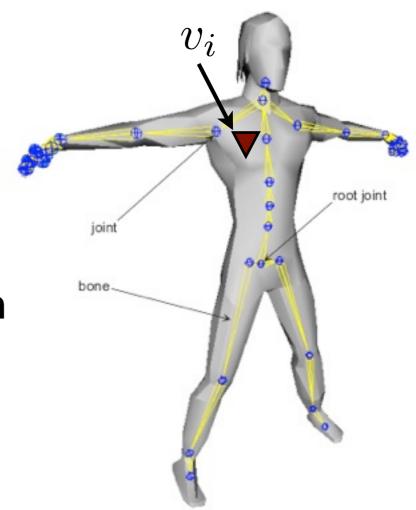
$$\hat{v}_i = F_j(A_j)^{-1} v_i$$

 $v_i$  - position of vertex in reference mesh

 $A_i$  - joint j in reference mesh

 $F_i$  - joint j in animated mesh

 $\hat{v_i}$  - position of vertex in animated mesh



### Rigid Skinning

Requires assignment of vertices on 3D mesh to joints on skeleton

- Often done manually
- Assigning to joint influencing the closest bone is usually a good automatic guess

Assign each vertex to one bone/joint - j

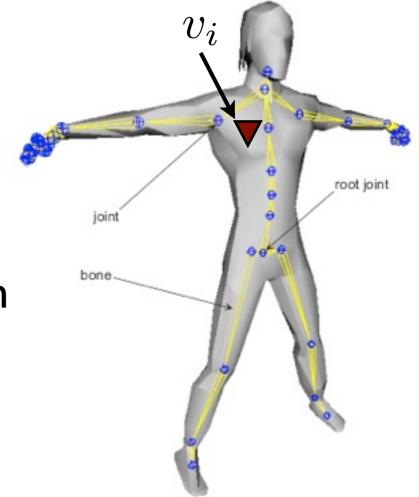
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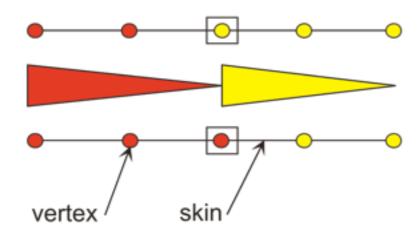
 $F_i$  - joint j in animated mesh

 $\hat{v_i}$  - position of vertex in animated mesh

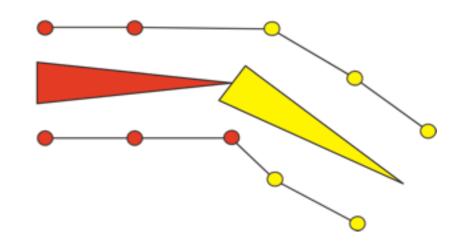


### Rigid Skinning Limitations

#### In reference pose:



#### In animated pose:



- Works well away from the ends of the bone (joints)
- Leads to unrealistic non-smooth deformations near joints

### Linear Blend Skinning

root joint

Each vertex is assigned to multiple bone/joints

$$\hat{v}_i = \sum_{j=1}^{N} w_{ji} F_j(A_j)^{-1} v_i$$

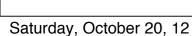


 $A_i$  - joint j in reference mesh

 $F_i$  - joint j in animated mesh

 $\hat{v_i}$  - position of vertex i in animated mesh

 $w_{ji}$  - influence of joint j on the vertex



### Linear Blend Skinning

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Weights need to be convex:  $\sum w_{ji} = 1, w_{ji} \geq 0$ 

$$\sum_{j=1}^{N} w_{ji} = 1, w_{ji} \ge 0$$

root joint

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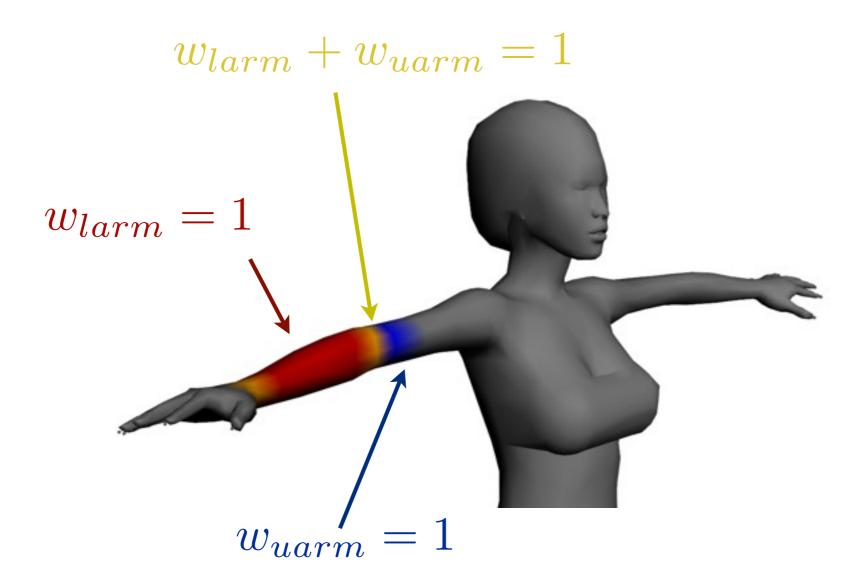
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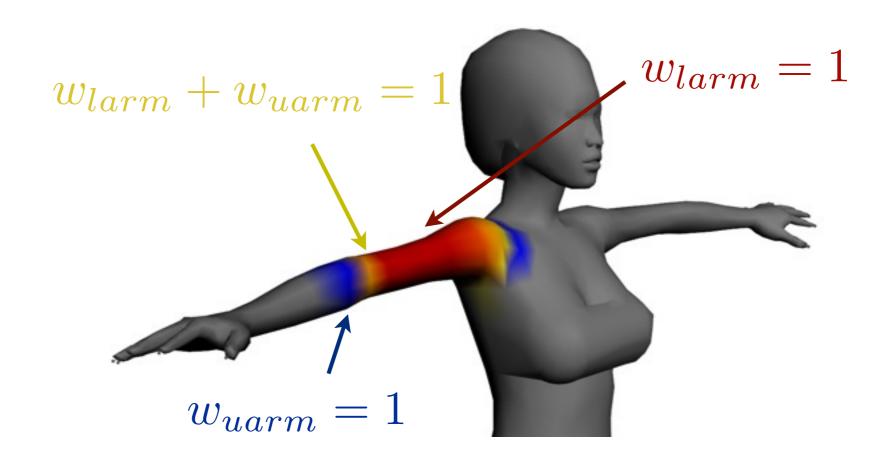
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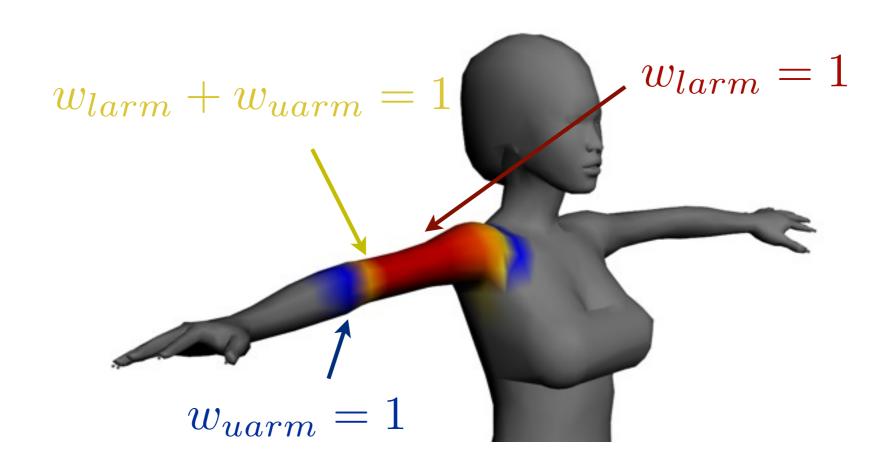
painted on or based on distance to joints

root joint

Weights need to be convex: 
$$\sum_{i=1}^{N} w_{ji} = 1, w_{ji} \geq 0$$

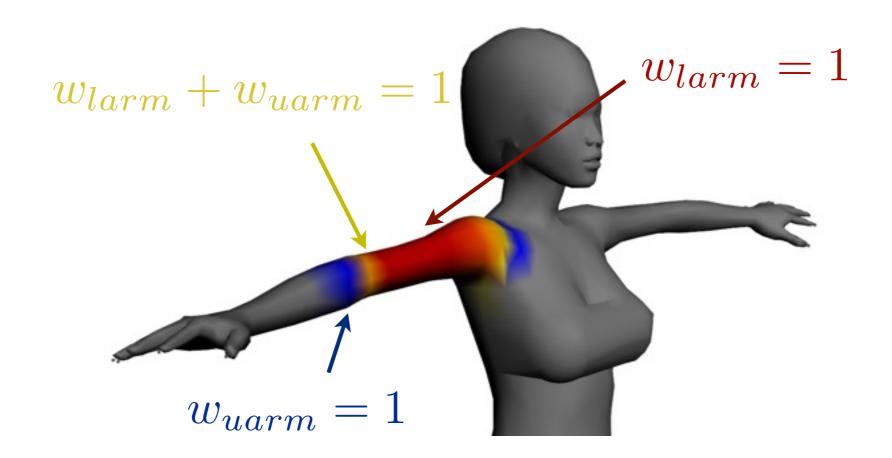






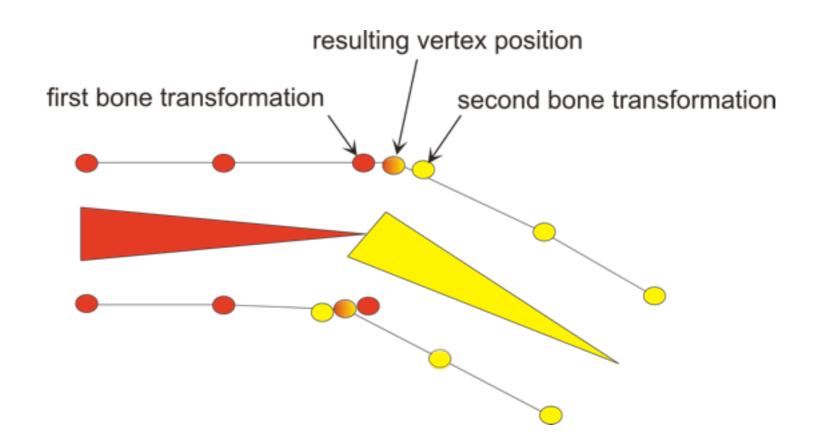
Why weights must convex?

$$\hat{v}_i = \sum_{j=1}^{N} w_{ji} F_j(A_j)^{-1} v_i$$



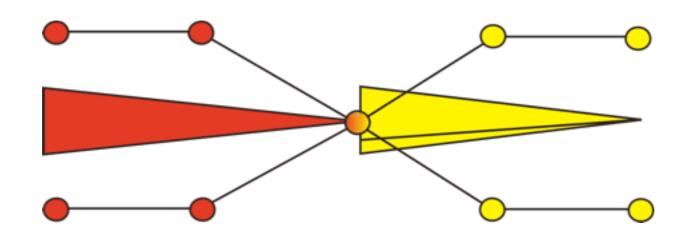
Why weights must convex?

### Linear Blend Skinning Example



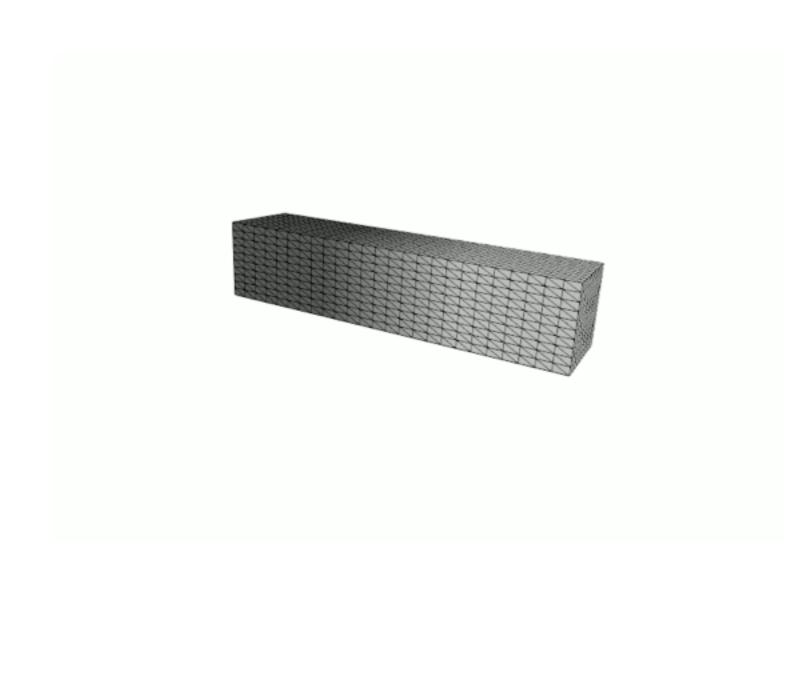
### Linear Blend Skinning Limitations

Joint twisting 180 degrees



produces a collapsing effect where skin collapses to a single point ("candy-wrapper" artifact)

### Linear Blend Skinning Limitations



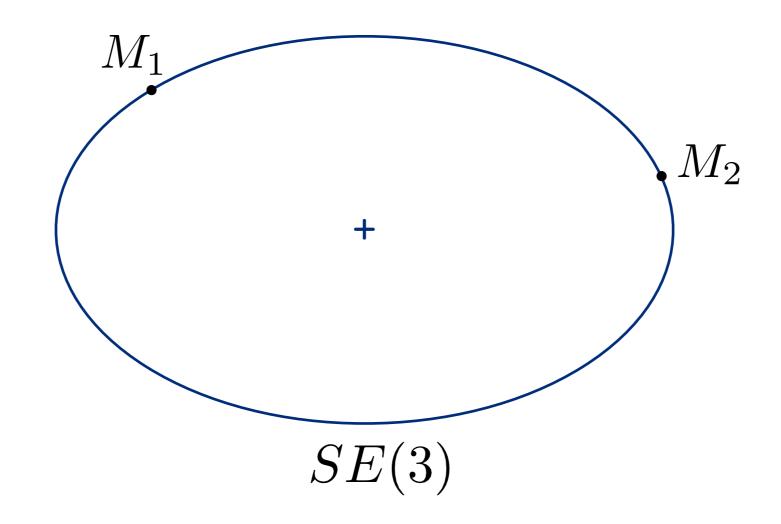


### Linear Blend Skinning Limitations

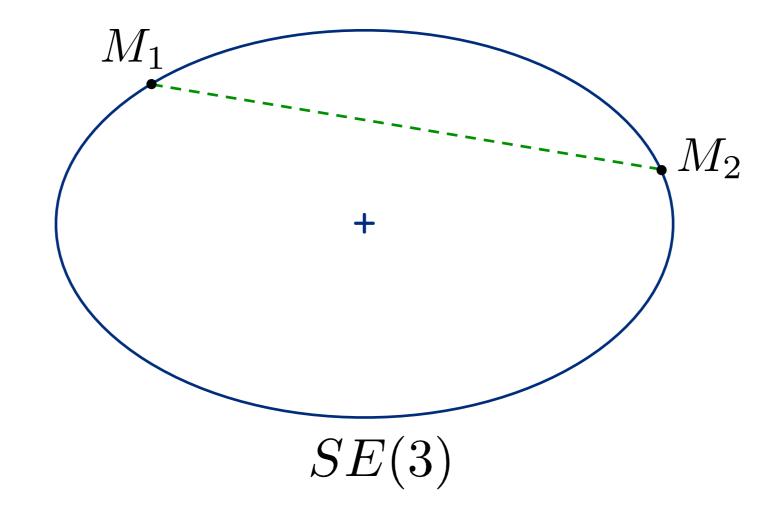


$$\hat{v}_i = \sum_{j=1}^N w_{ji} F_j(A_j)^{-1} v_i \iff \hat{v}_i = \left(\sum_{j=1}^N w_{ji} M_j\right) v_i$$

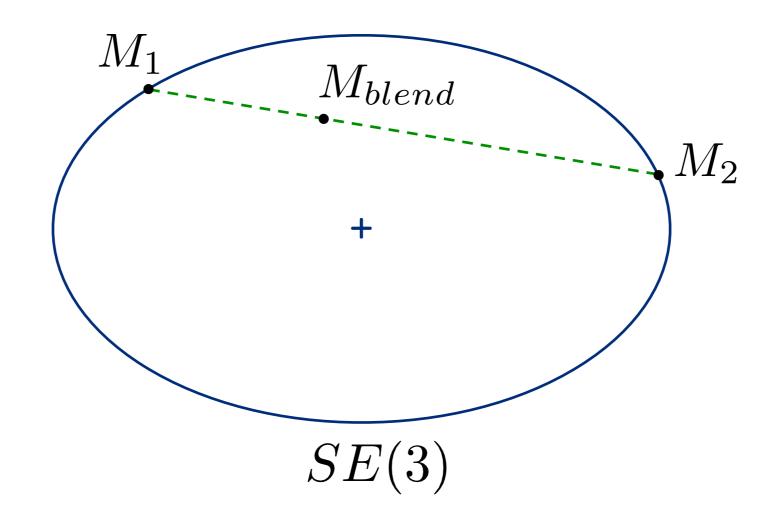
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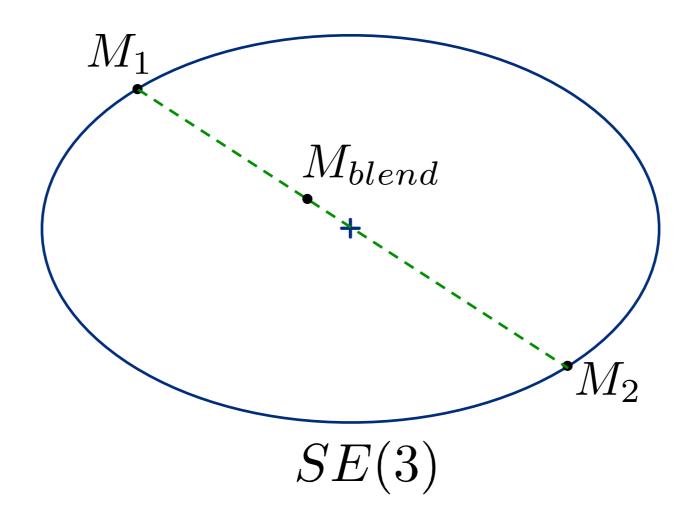


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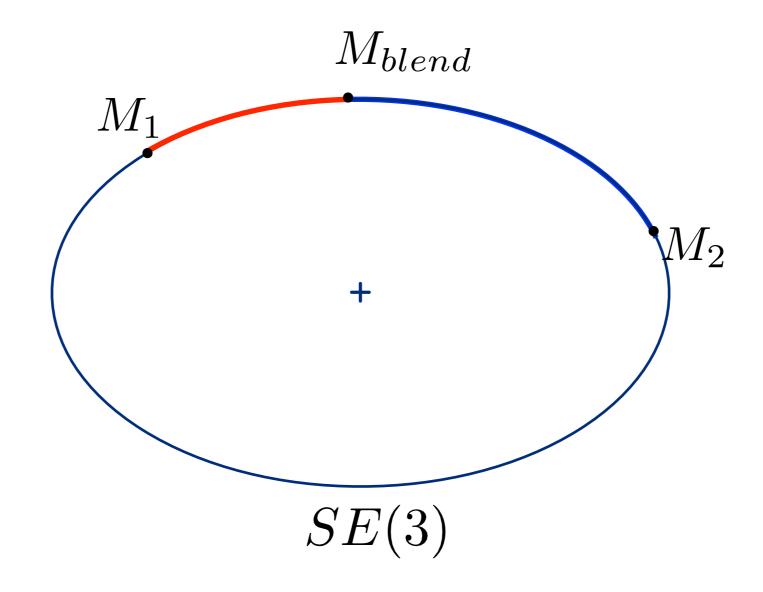


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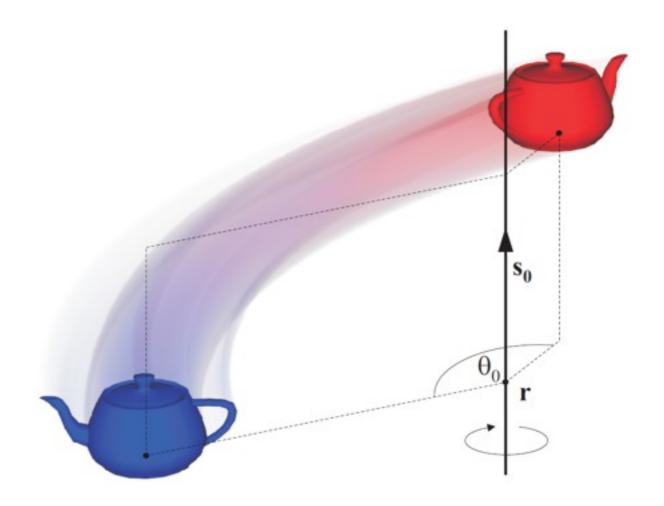
# SE(3) Intrinsic Blending



### Dual Quaternion Skinning

[Kavan et al., ACM TOG 2008]

#### Closed form approximation of SE(3) blending



# Regular Quaternions

Remember: Euler angles

## Rotation in 3D

$$Z = \begin{bmatrix} X' \\ Y' \\ Z' \end{bmatrix} = \begin{bmatrix} \cos(\phi) & \sin(\phi) & 0 \\ -\sin(\phi) & \cos(\phi) & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

$$\mathbf{R}_{z}$$

$$\begin{bmatrix} X' \\ Y' \\ Z' \end{bmatrix} = \begin{bmatrix} \cos(\theta) & 0 & \sin(\theta) \\ 0 & 1 & 0 \\ -\sin(\theta) & 0 & \cos(\theta) \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

$$\mathbf{R}_{y}$$

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$$\mathbf{R}_{x}$$

Note: I've overloaded the use of \phi in these slides. Earlier I used \phi to denote the original orientation. Here I am using it to denote the rotation about the Z-axis.

Interpolating Euler angles has similar issues as LBS skinning

# Regular Quaternions

- Quaternions are alternative representation for orientations (defined using complex algebra)
- Represents orientation using 4 tuples (roughly speaking one for amount of rotation and 3 for the axis)

$$q = w + xi + yi + zi$$

- However, there are only 3 degrees of freedom for a rotation
- Hence, to be a valid rotation, quaternion must be unit norm

$$||q|| = 1$$

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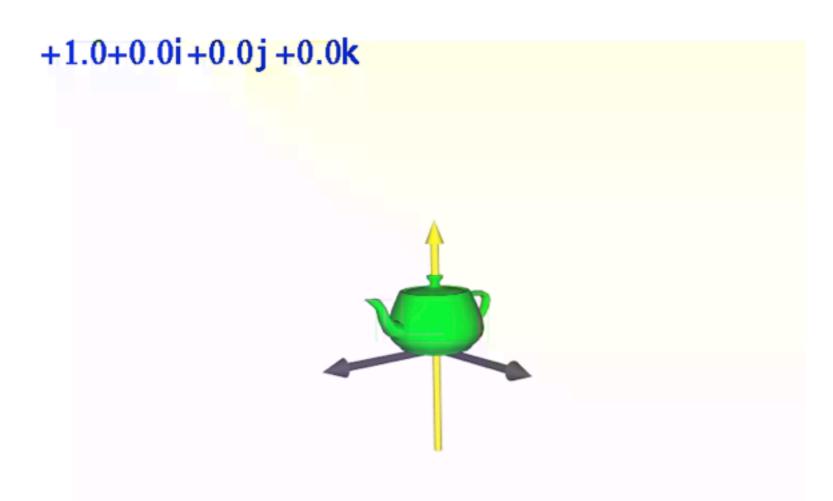
- However, there are only 3 degrees of freedom for a rotation
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$$||q|| = 1$$

Interpretation: Quaternions live on a sphere in a 4D space

## Dual Quaternions [Clifford 1873]

- Dual quaternions are able to model rigid transformations (rotation + translation)
- Map a 6 dimensional manifold in an 8 dimensional space
- Need to be unit length to represent a valid rigid transform



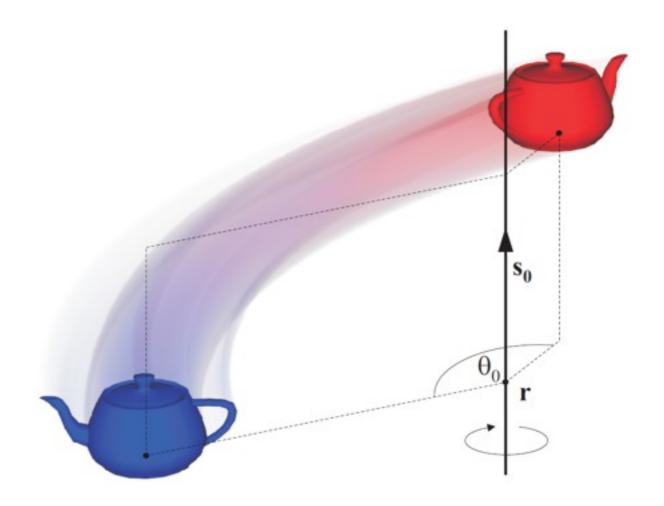
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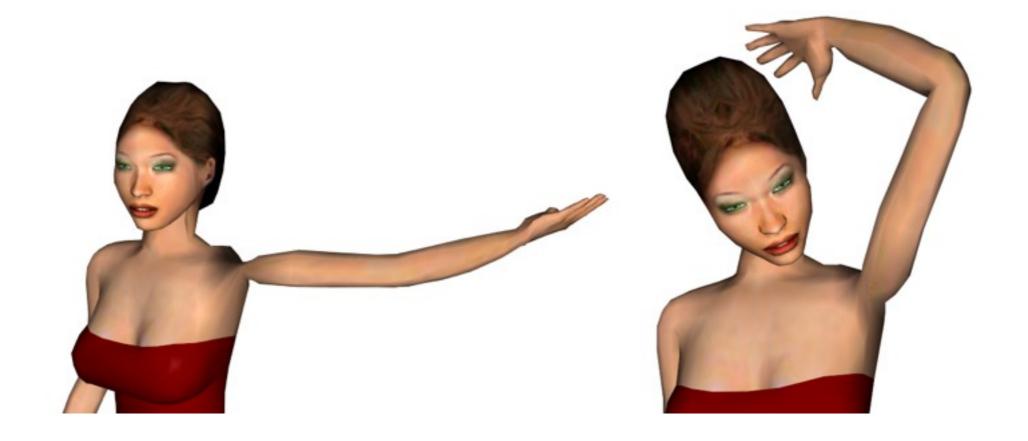
# Dual Quaternion Skinning

[Kavan et al., ACM TOG 2008]

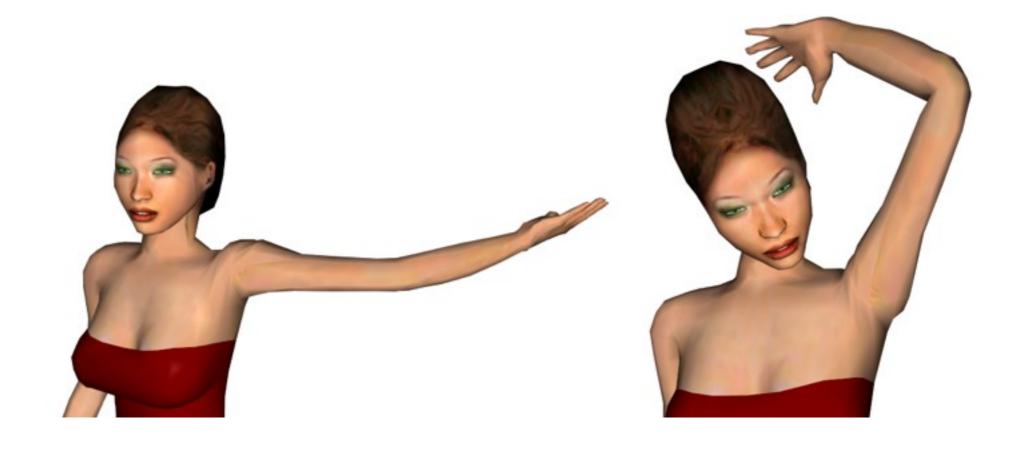
## Closed form approximation of SE(3) blending



# Comparison: Linear Blend Skinning



## Comparison: Dual Quaternion



# Dual Quaternion Skinning



# Skinning Limitations

- All skinning methods assume a fixed relationship between skeleton motion and the mesh
- Humans are more complex (e.g., muscles lead to local deformations)
- Skinning only allows animation of predefined body geometry (created by an animator), do not help us create this geometry

## Data-driven Body Shape Models



[Cyberware]

Idea: Let's scan real people and figure out how their body deforms and what body types are possible

## Data-driven Body Shape Models



## **Pipeline**

[Cyberware]

- Register all the scans
- Create (typically parametric) model of shape
- Use that model for an interesting application

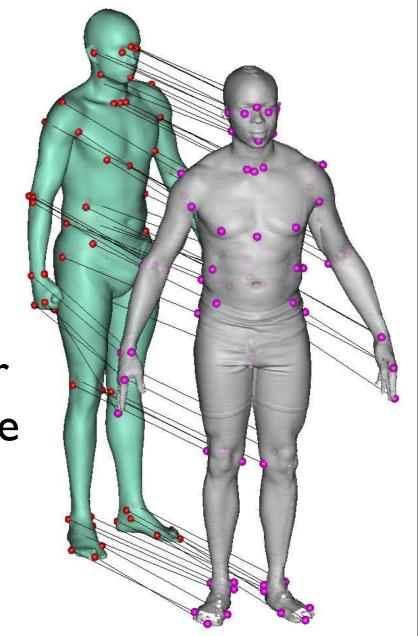
[Allen et al., 2003]

Marker-based Non-rigid Iterative Closest Point Registration

Goal: Fit a template mesh to triangulated 3D point cloud

$$E = \alpha E_d + \beta E_s + \gamma E_m$$

Amounts to estimating a 4x4 transform for every vertex through optimization of above



[Allen et al., 2003]

Marker-based Non-rigid Iterative Closest Point Registration

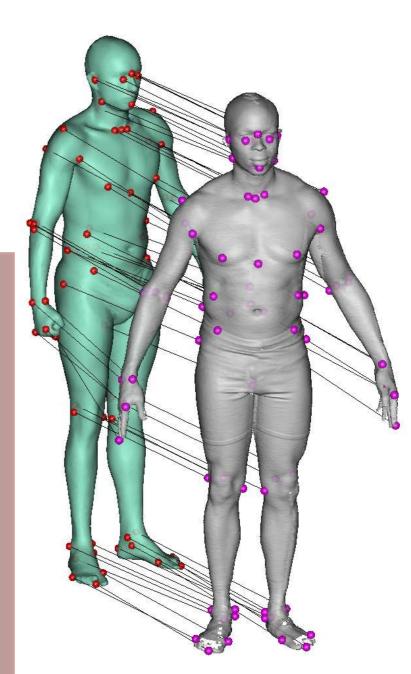
Goal: Fit a template mesh to triangulated 3D point cloud

$$E = \alpha E_d + \beta E_s + \gamma E_m$$
 data term

$$E_d = \sum_{i=1}^{V} w_i \operatorname{gap}^2(\mathbf{T}_i \vec{v}_i, \mathcal{D})$$

Distance from the reference mesh point to closest compatible vertex on observed surface

- Angle between surface normals
- Robust measure for dealing with holes



[Allen et al., 2003]

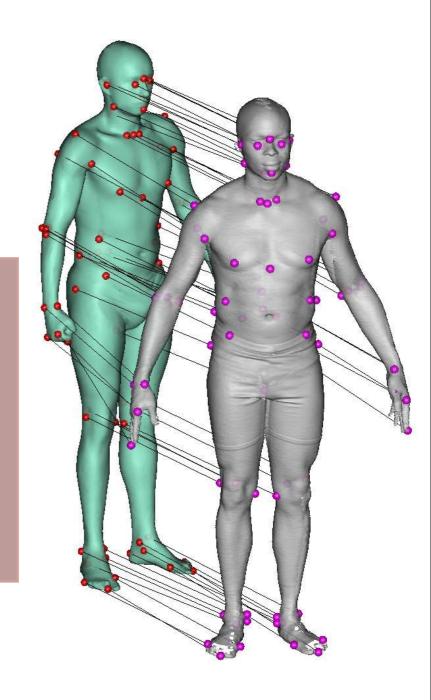
Marker-based Non-rigid Iterative Closest Point Registration

Goal: Fit a template mesh to triangulated 3D point cloud

$$E = \alpha E_d + \beta E_s + \gamma E_m$$
 data term smoothness term

$$E_s = \sum_{\{i,j | (\vec{v}_i, \vec{v}_j) \in \text{edges}(\mathcal{T})\}} ||\mathbf{T}_i - \mathbf{T}_j||_F^2$$

Ensures that transforms on near by vertices are similar (induces local smoothness)



[Allen et al., 2003]

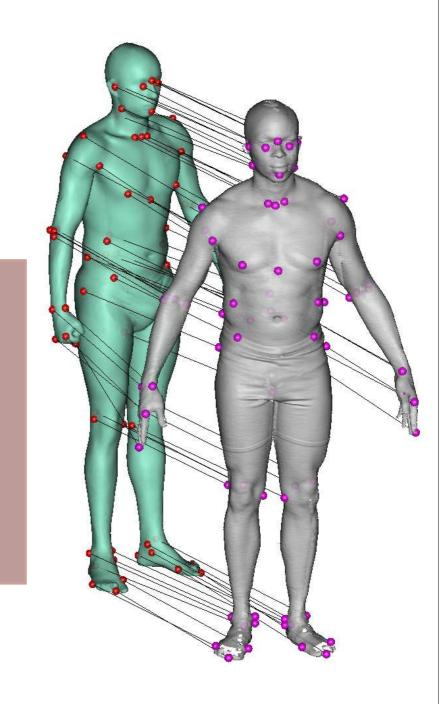
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$$E = \alpha E_d + \beta E_s + \gamma E_m$$
 data term smoothness marker anchor term term

$$E_m = \sum_{i=1}^{M} ||\mathbf{T}_{\kappa_i} \vec{v}_{\kappa_i} - \vec{m}_i||^2$$

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[Allen et al., 2003]

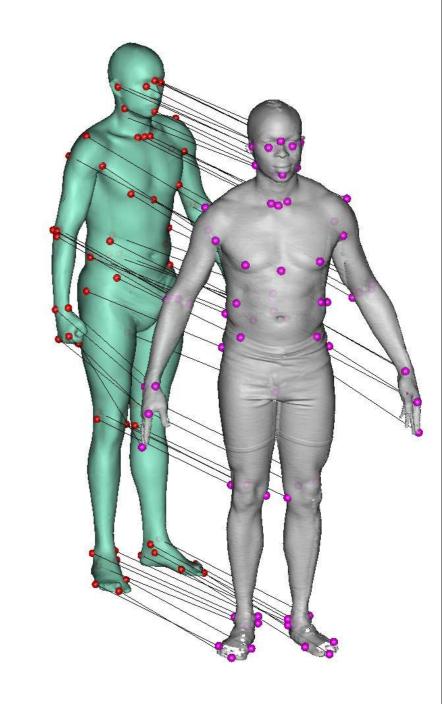
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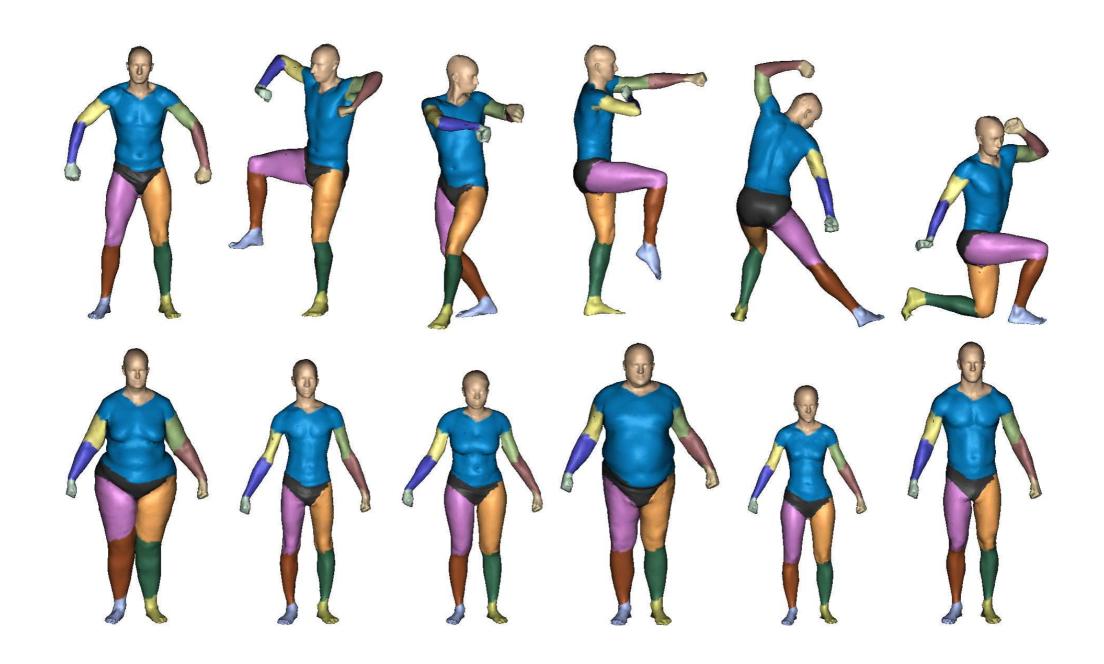
$$E = \alpha E_d + \beta E_s + \gamma E_m$$
 data term smoothness marker anchor term term

Solved using gradient descent

Initialized by aligning centers of mass



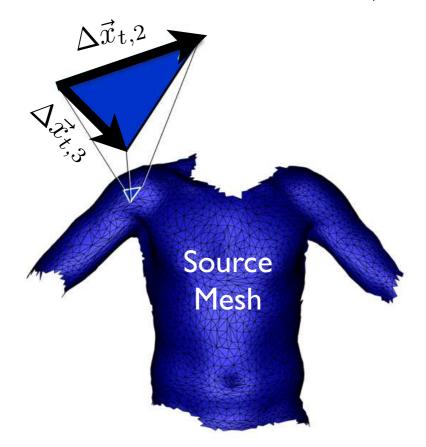
# Registration

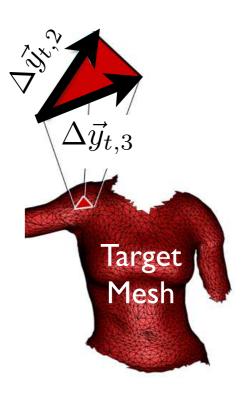


[Sumner and Popovic, 2004]

#### 3x3 transform for every triangle

$$\mathbf{A}_t \left[ \Delta \vec{x}_{t,2} , \Delta \vec{x}_{t,3} \right] = \left[ \Delta \vec{y}_{t,2} , \Delta \vec{y}_{t,3} \right]$$

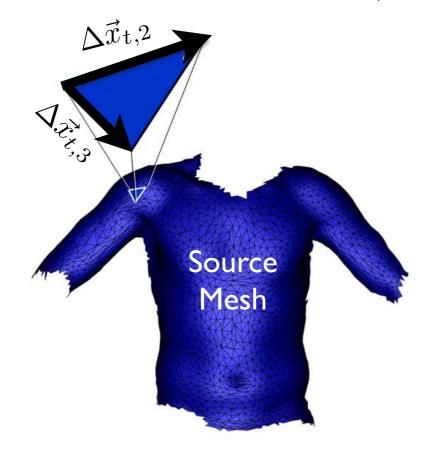


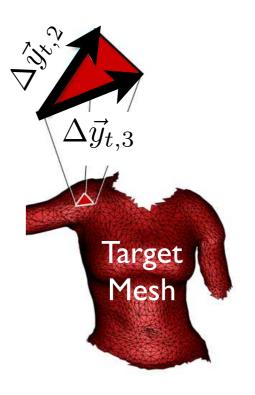


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[Image from Alexandru Balan]

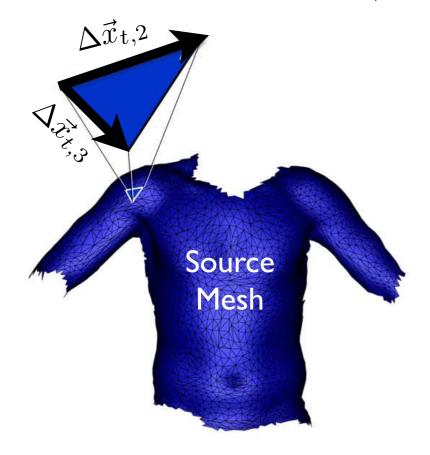
#### Estimation:

$$\underset{\{\mathbf{A}_1,\cdots,\mathbf{A}_T\}}{\operatorname{arg\,min}} \sum_{t=1}^T \sum_{k=2,3} ||\mathbf{A}_t \Delta \vec{x}_{t,k} - \Delta \vec{y}_{t,k}||^2$$

[Sumner and Popovic, 2004]

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[Image from Alexandru Balan]

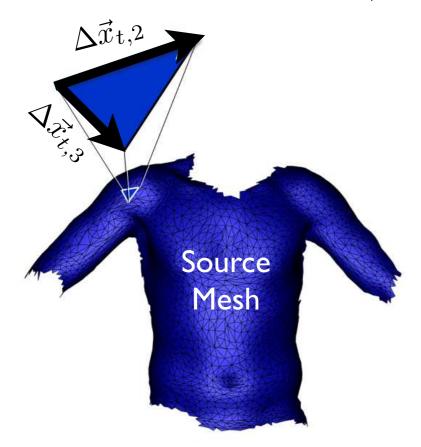
#### Estimation:

$$\underset{\{\mathbf{A}_1,\cdots,\mathbf{A}_T\}}{\operatorname{arg\,min}} \sum_{t=1}^T \sum_{k=2,3} \left| \left| \mathbf{A}_t \Delta \vec{x}_{t,k} - \Delta \vec{y}_{t,k} \right| \right|^2 \quad \text{under-constrained}$$

[Sumner and Popovic, 2004]

#### 3x3 transform for every triangle

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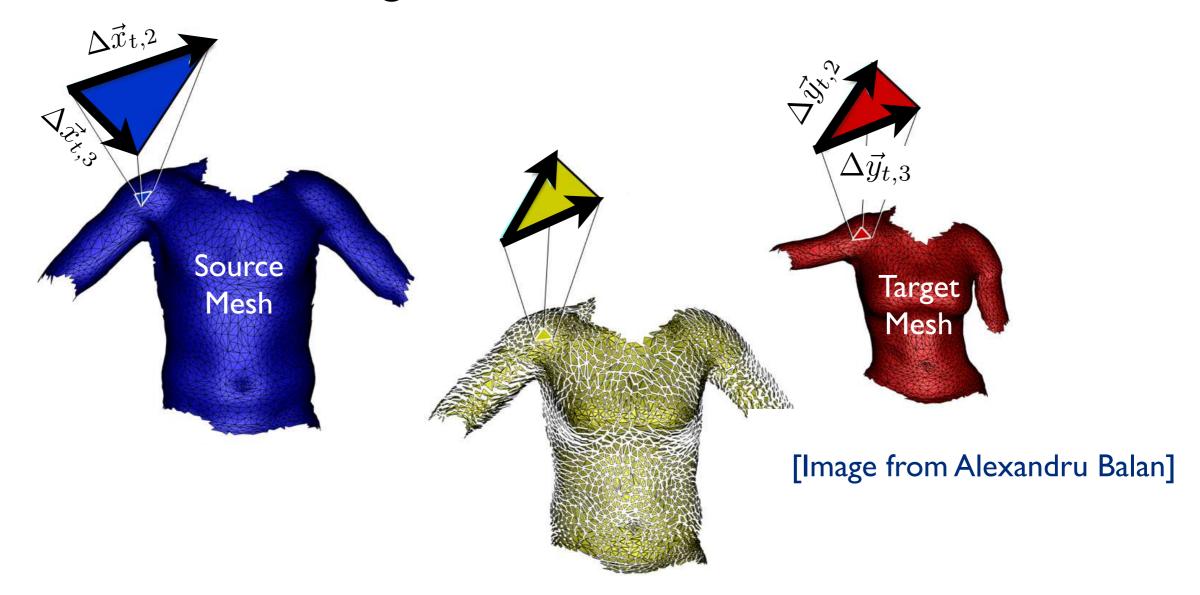
[Image from Alexandru Balan]

#### **Estimation:**

$$\underset{\{\mathbf{A}_{1},\cdots,\mathbf{A}_{T}\}}{\operatorname{arg\,min}} \sum_{t=1}^{T} \sum_{k=2,3} ||\mathbf{A}_{t} \Delta \vec{x}_{t,k} - \Delta \vec{y}_{t,k}||^{2} + w_{s} \sum_{t_{1},t_{2} \text{ adj}} ||\mathbf{A}_{t_{1}} - \mathbf{A}_{t_{2}}||_{F}^{2}$$

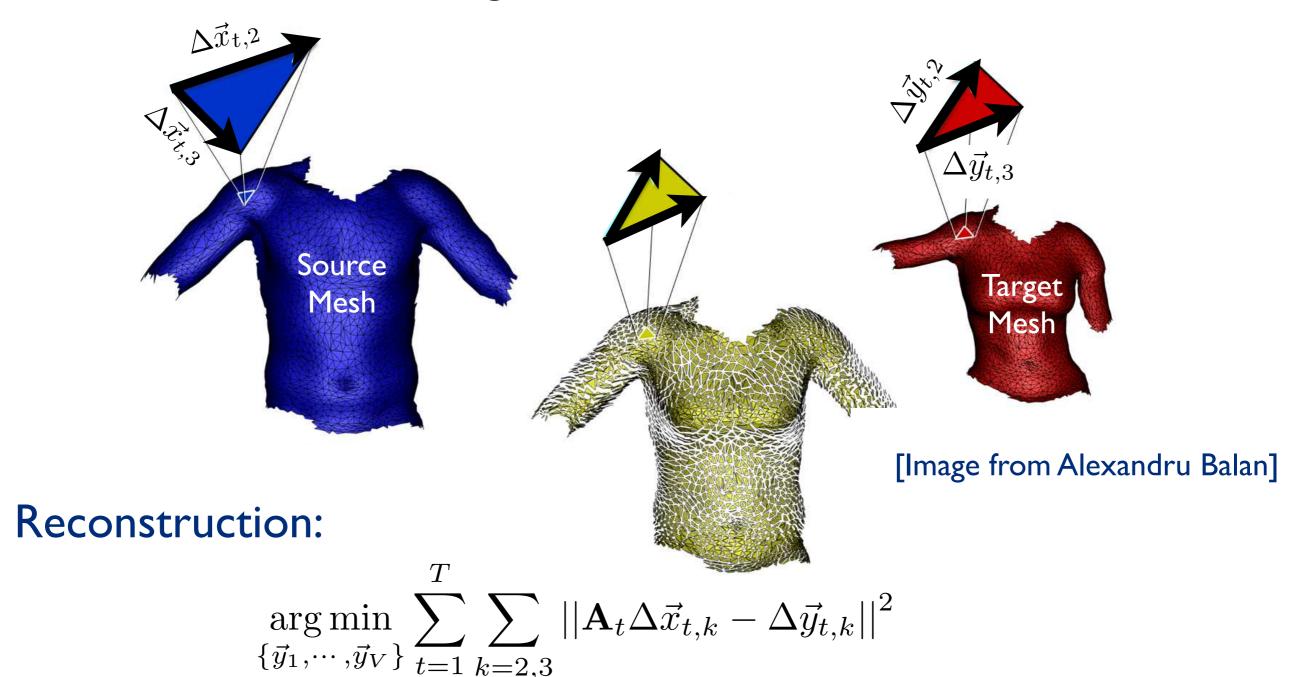
[Sumner and Popovic, 2004]

Applying deformation gradients typically leads to inconsistent edges and structures



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# SCAPE: Shape Completion and Animation of PEople [Angelov et al., ACM TOG, 2005]

Key Idea: factor mesh deformation for a person into:

- (I) Articulated rigid deformations
- (2) Non-rigid deformations
- (3) Body shape deformations

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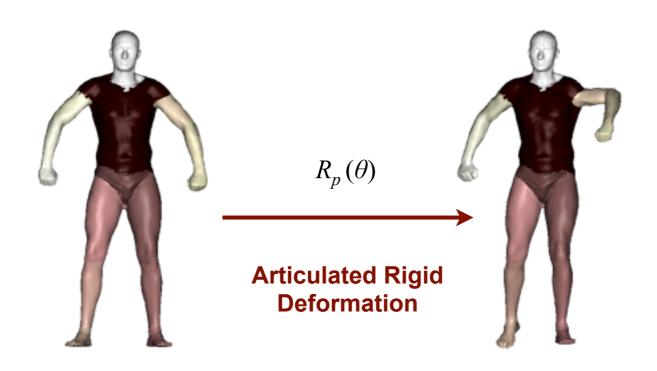
- (I) Articulated rigid deformations
- (2) Non-rigid deformations
- (3) Body shape deformations

Gives a parametric model of any person in any pose!

## Articulated Rigid Deformation

[Angelov et al., ACM TOG, 2005]

## This is basically rigid skinning



 $\theta$  – joint angles

## Non-rigid Deformations

[Angelov et al., ACM TOG, 2005]



From a dataset of one person in different poses, learn residual deformations

$$\underset{\{\mathbf{Q}_{1}^{i}, \dots, \mathbf{Q}_{T}^{i}\}}{\operatorname{arg\,min}} \sum_{t=1}^{T} \sum_{k=2,3} \left| \left| \mathbf{R}_{p[t]}^{i} \mathbf{Q}_{t}^{i} \Delta \vec{x}_{t,k} - \Delta \vec{y}_{t,k}^{i} \right| \right|^{2} + w_{s} \sum_{\substack{t_{1}, t_{2} \text{ adj} \\ p[t_{1}] = p[t_{2}]}} \left| \left| \mathbf{Q}_{t_{1}}^{i} - \mathbf{Q}_{t_{2}}^{i} \right| \right|_{F}^{2}$$

## Non-rigid Deformations

[Angelov et al., ACM TOG, 2005]

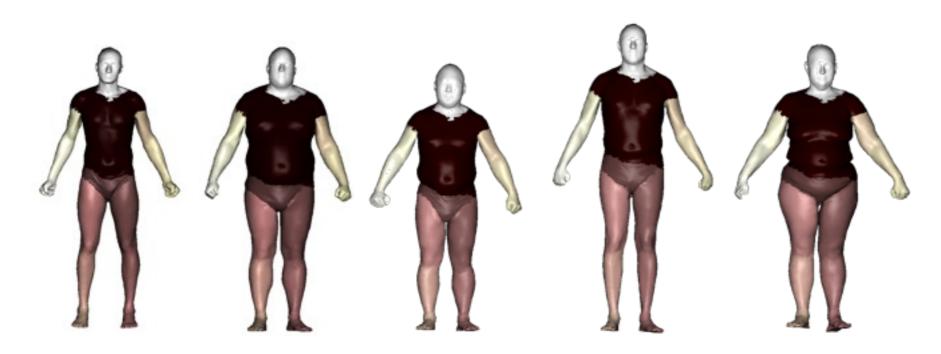
## Let non-rigid deformations be linear functions of pose





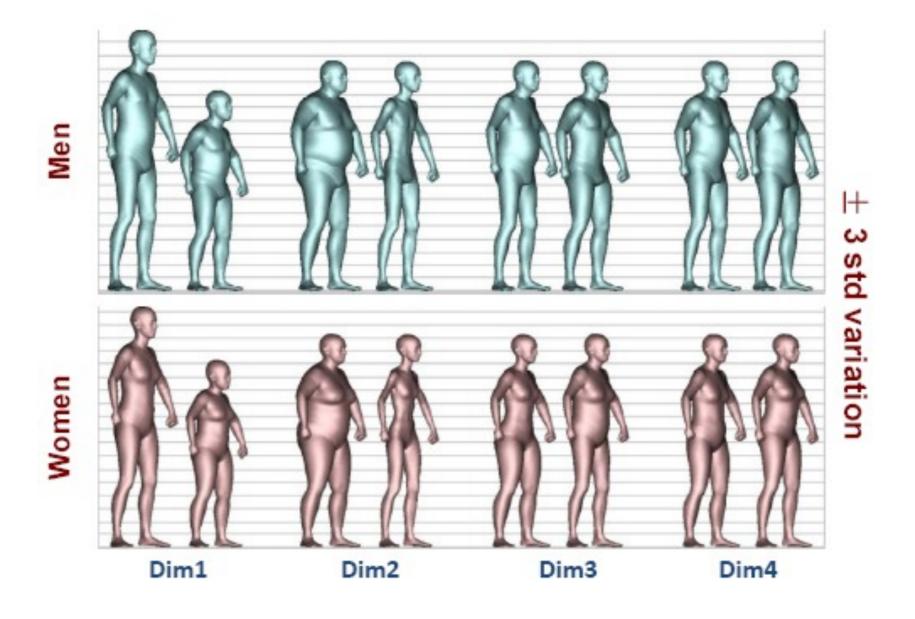
Models bulging of muscles, etc.

[Angelov et al., ACM TOG, 2005]



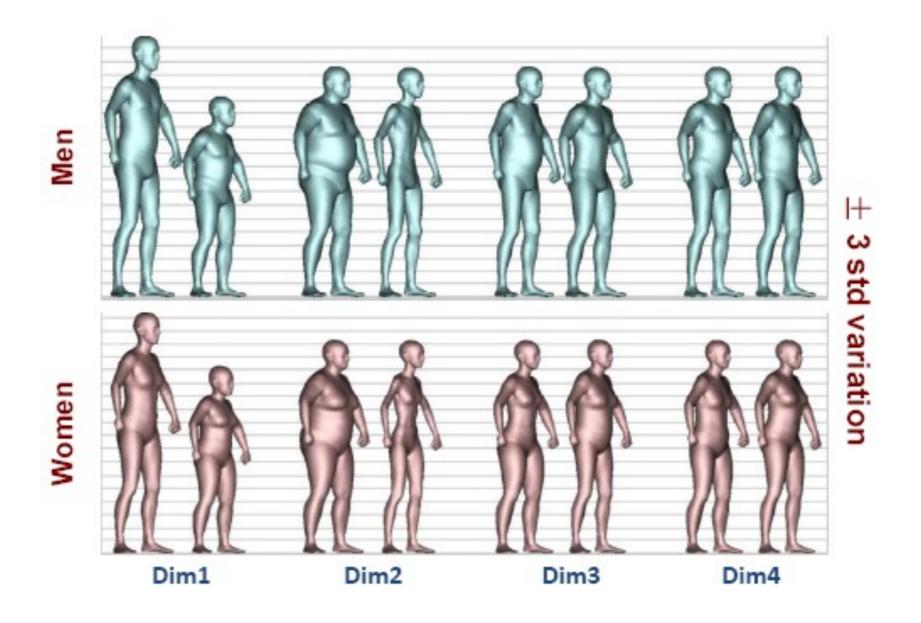
From a dataset of many people in one pose learn variations

- Extract mesh deformation gradients
- Do PCA on them (vectorizing them first)
  - 6 PCA dimensions can capture > 80% of variation



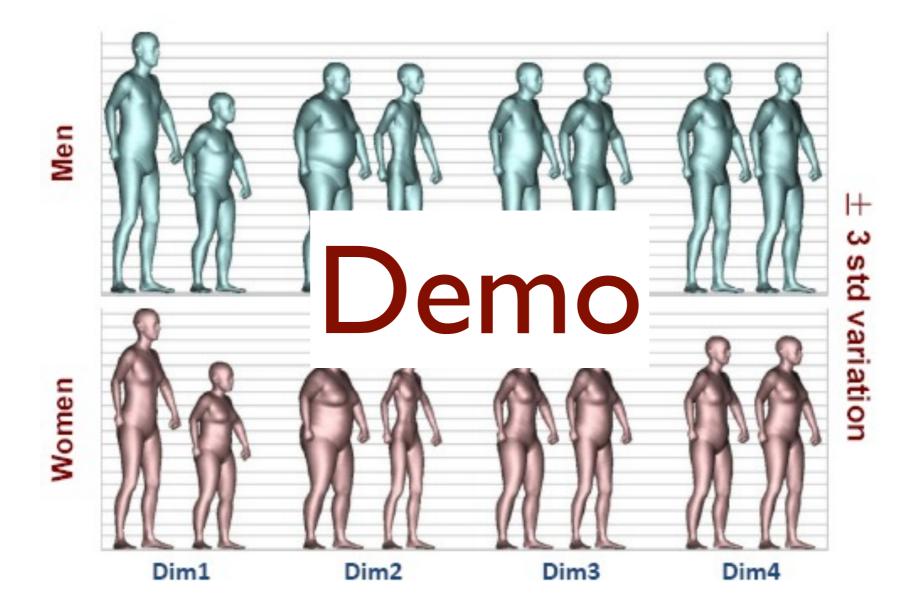
[Image from Peng Guan]

It is also possible to create semantic parameters and regress from them to PCA coefficients



[Image from Peng Guan]

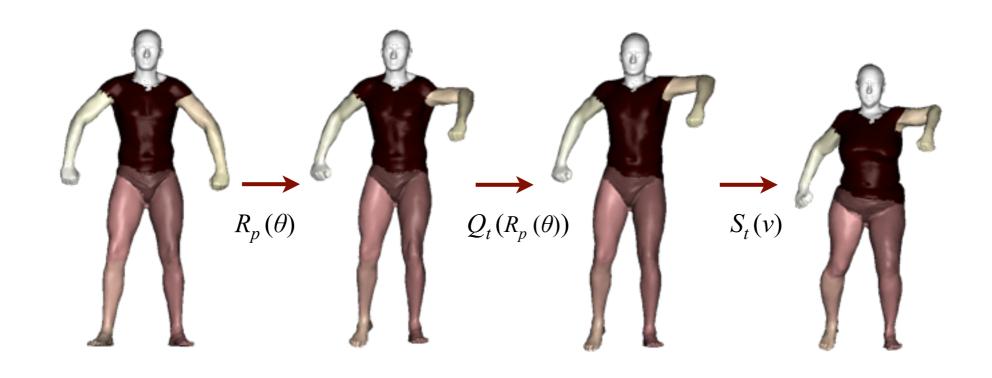
It is also possible to create semantic parameters and regress from them to PCA coefficients



[Image from Peng Guan]

## SCAPE: Putting it all together

[Angelov et al., ACM TOG, 2005]

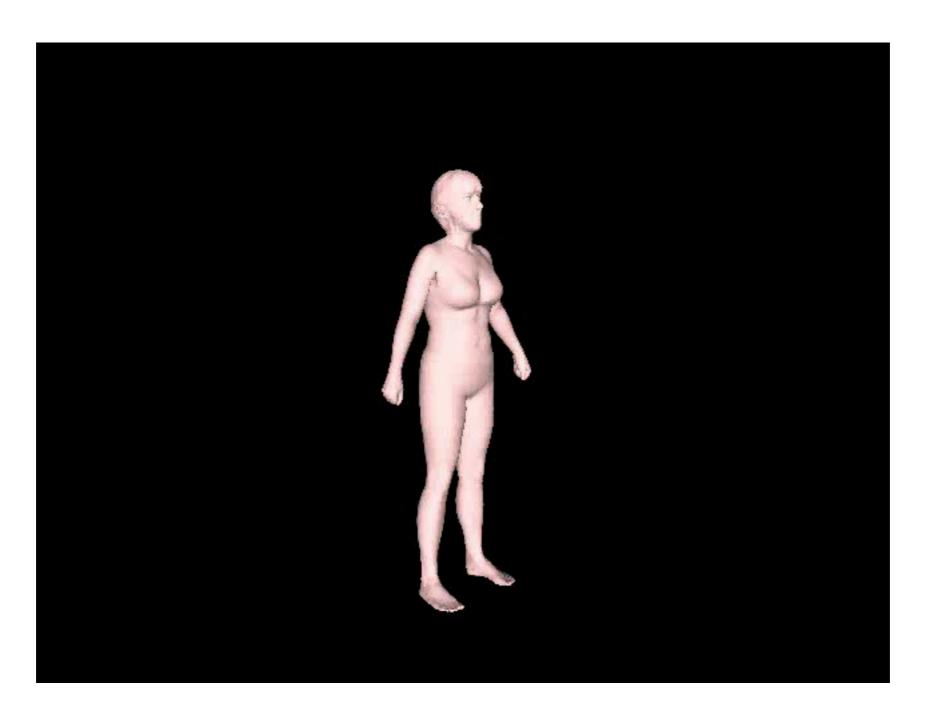


 $\theta$  – joint angles

v – shape parameters

We can simply concatenate all the deformations by multiplying them together

## **SCAPE Model**



[Video curtesy of Peng Guan]

## Applications: Shape Estimation

[Sigal et al., NIPS'2007]

Goal: learn functional mapping from image features to pose and shape parameters of the SCAPE model

(from synthesized input-output pairs)

[Sigal et al., NIPS'2007]

Goal: learn functional mapping from image features to pose and shape parameters of the SCAPE model

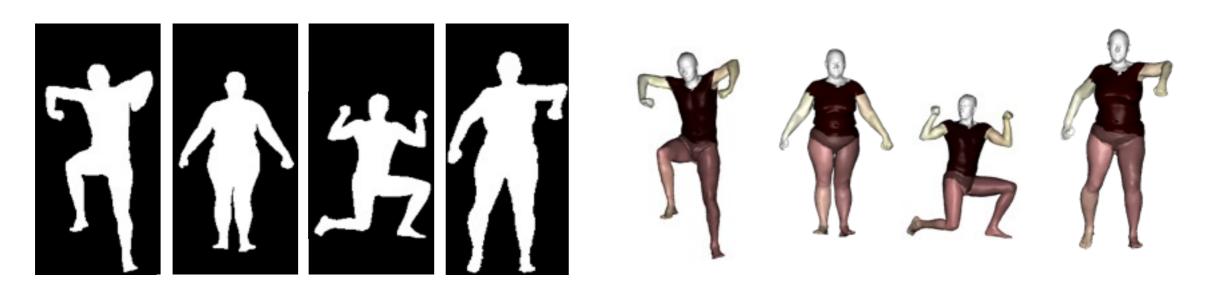
(from synthesized input-output pairs)

Remember how Kinect works? Let's try that for shape

[Sigal et al., NIPS'2007]

Goal: learn functional mapping from image features to pose and shape parameters of the SCAPE model

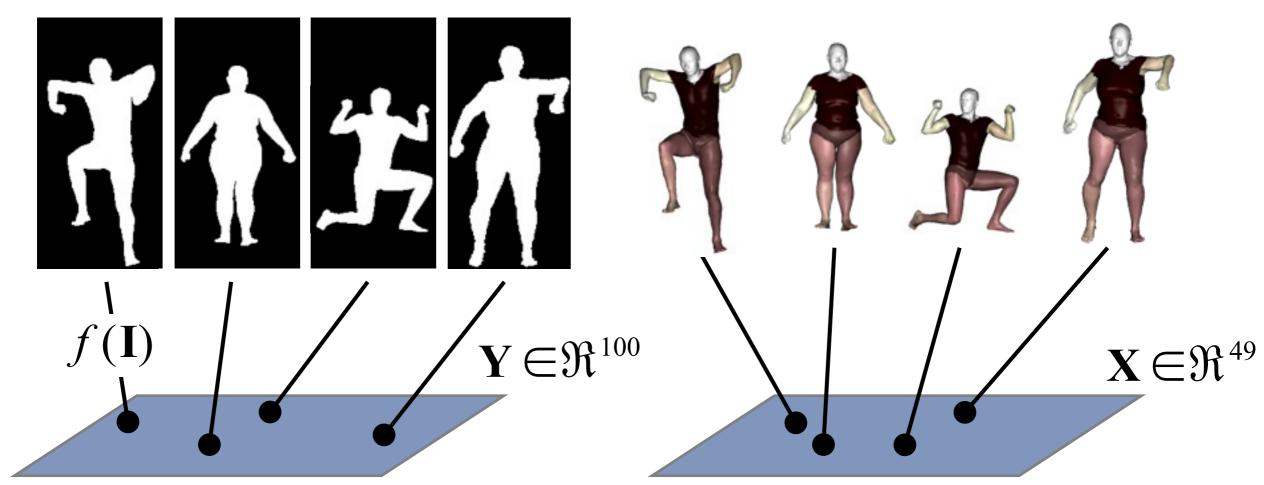
(from synthesized input-output pairs)



[Sigal et al., NIPS'2007]

Goal: learn functional mapping from image features to pose and shape parameters of the SCAPE model

(from synthesized input-output pairs)



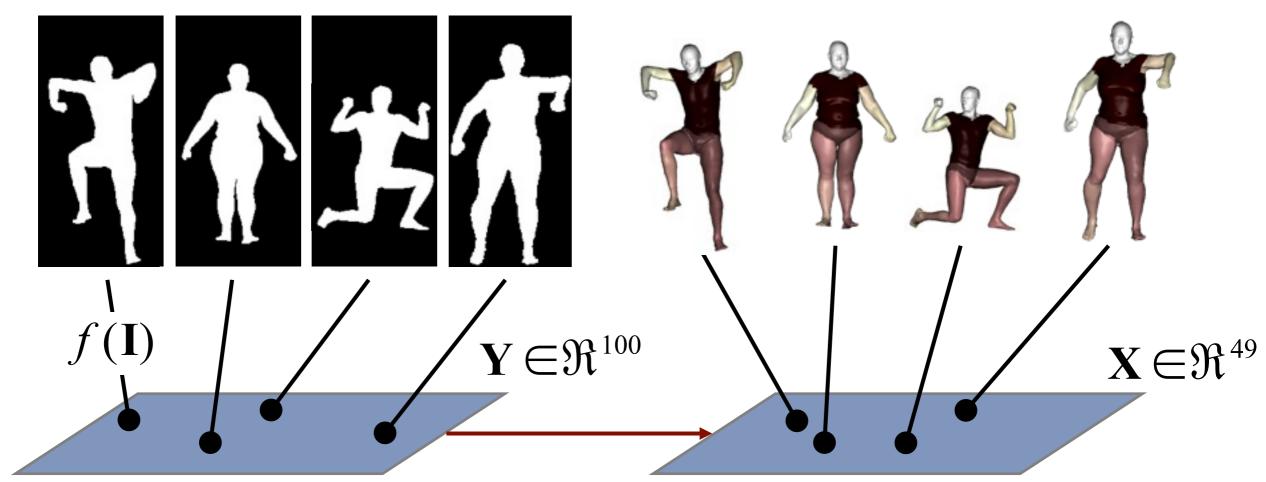
feature space

SCAPE space

[Sigal et al., NIPS'2007]

Goal: learn functional mapping from image features to pose and shape parameters of the SCAPE model

(from synthesized input-output pairs)

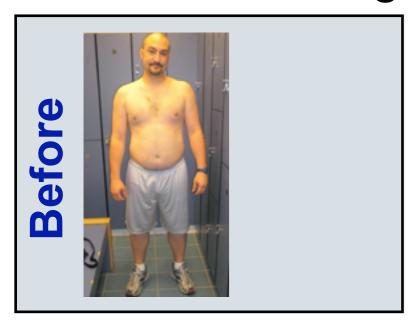


feature space

SCAPE space

SCAPE parameters = g (features)

[Sigal et al., NIPS'2007]



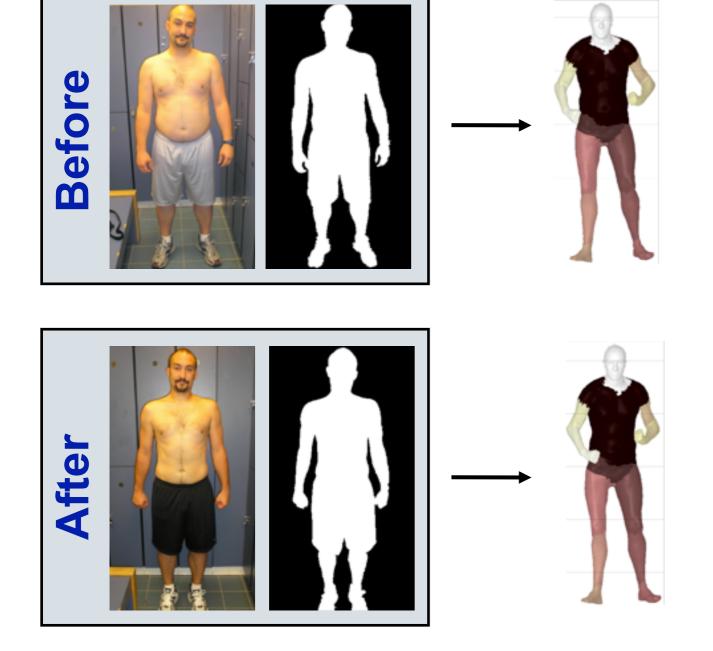


[Sigal et al., NIPS'2007]





[Sigal et al., NIPS'2007]



[Sigal et al., NIPS'2007]

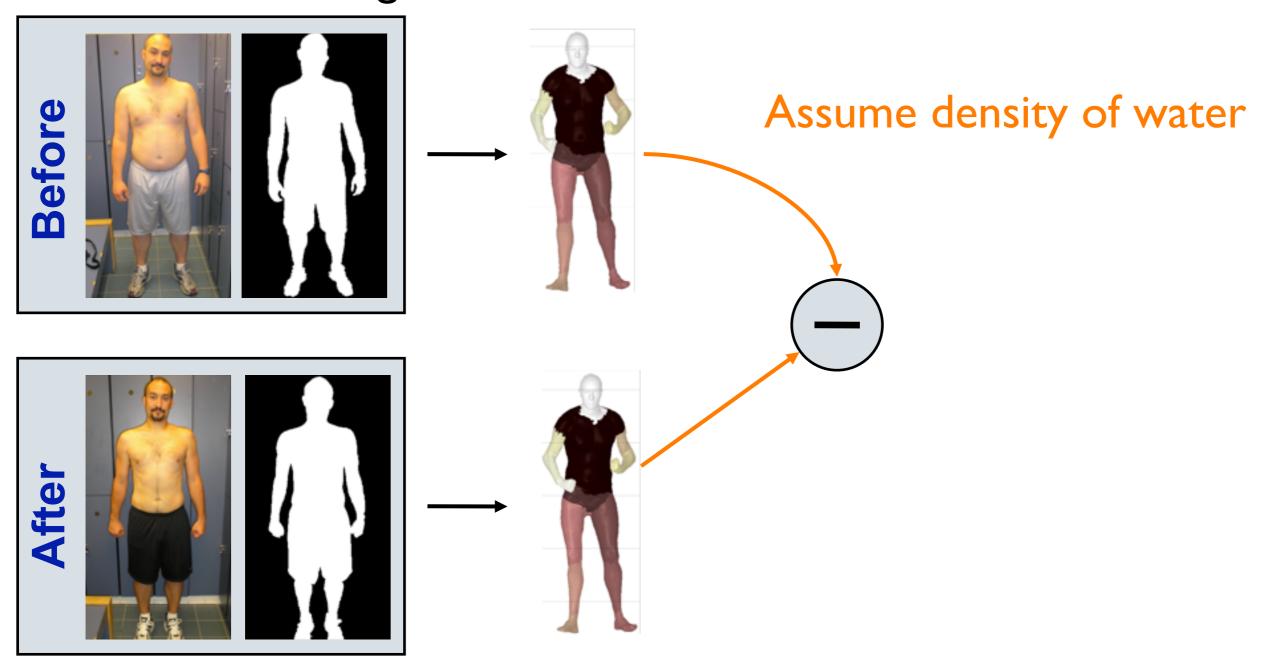
Can we estimate weight loss discriminatively from monocular images?



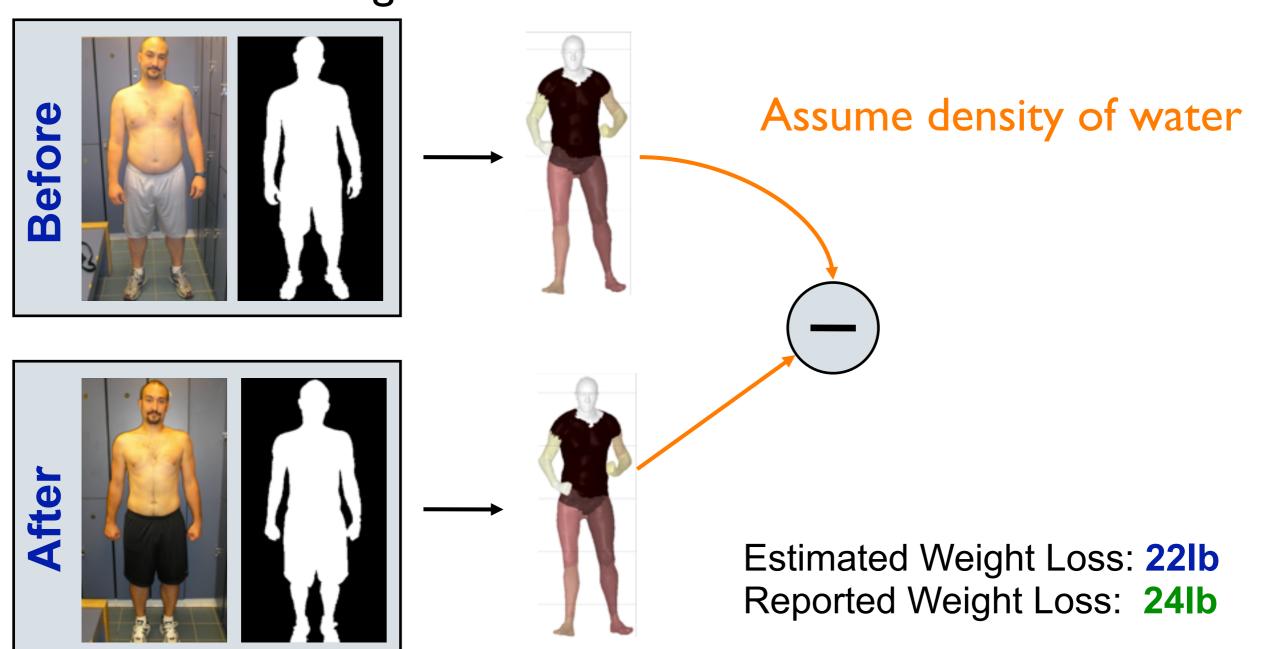
Assume density of water



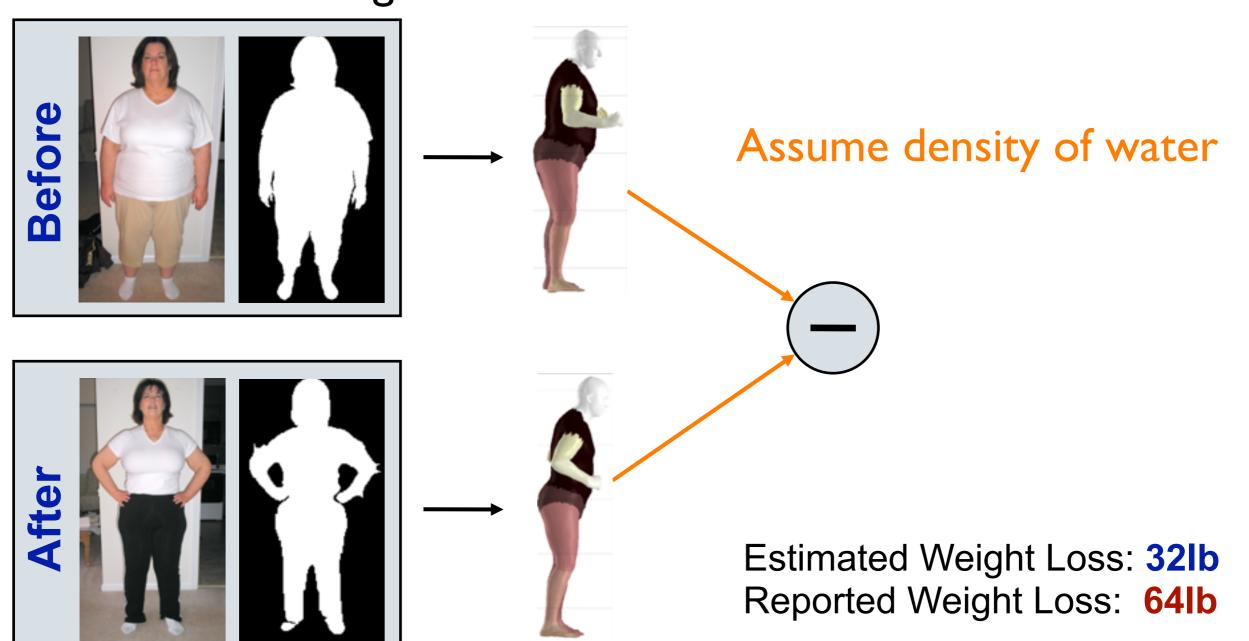
[Sigal et al., NIPS'2007]



[Sigal et al., NIPS'2007]

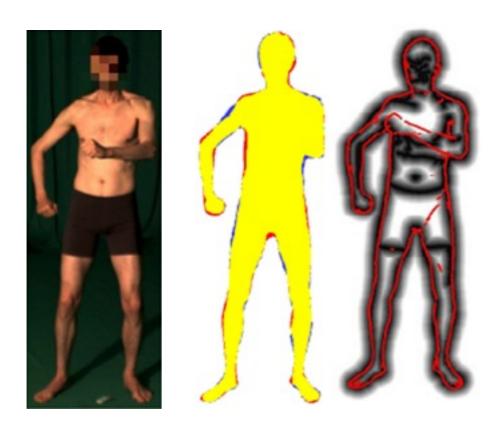


[Sigal et al., NIPS'2007]

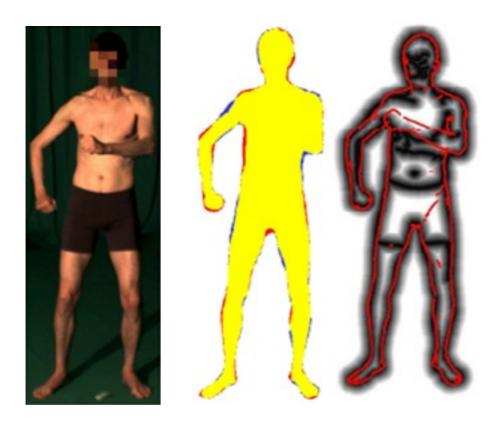




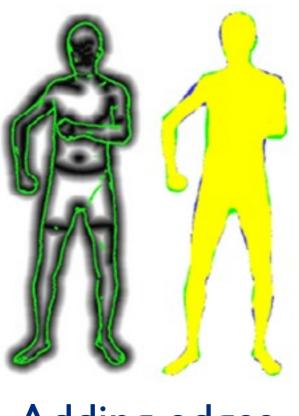
Silhouettes are ambiguous



Silhouettes are ambiguous

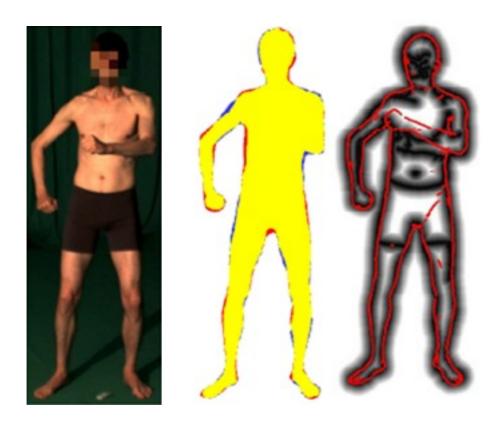


Silhouettes are ambiguous

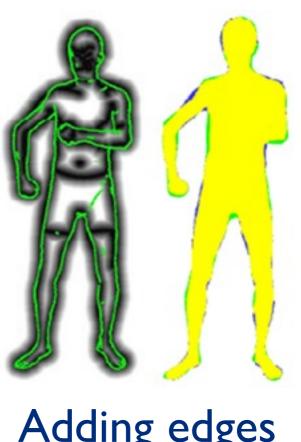


Adding edges

[Guan et al., ICCV, 2009]



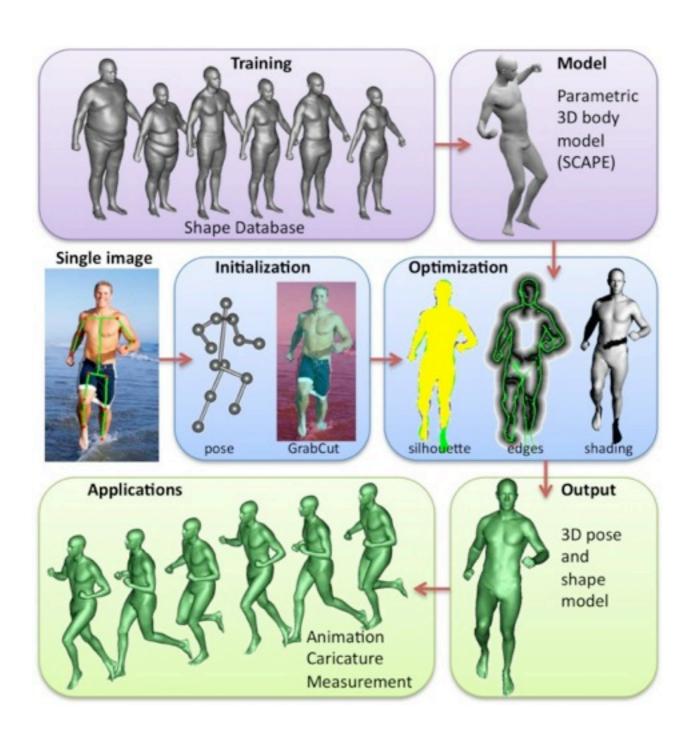
Silhouettes are ambiguous



Adding edges

They also add shading cues

# Estimating Pose and Shape from Image



#### Fun Results

[Guan et al., ICCV, 2009]

#### Internet Images:

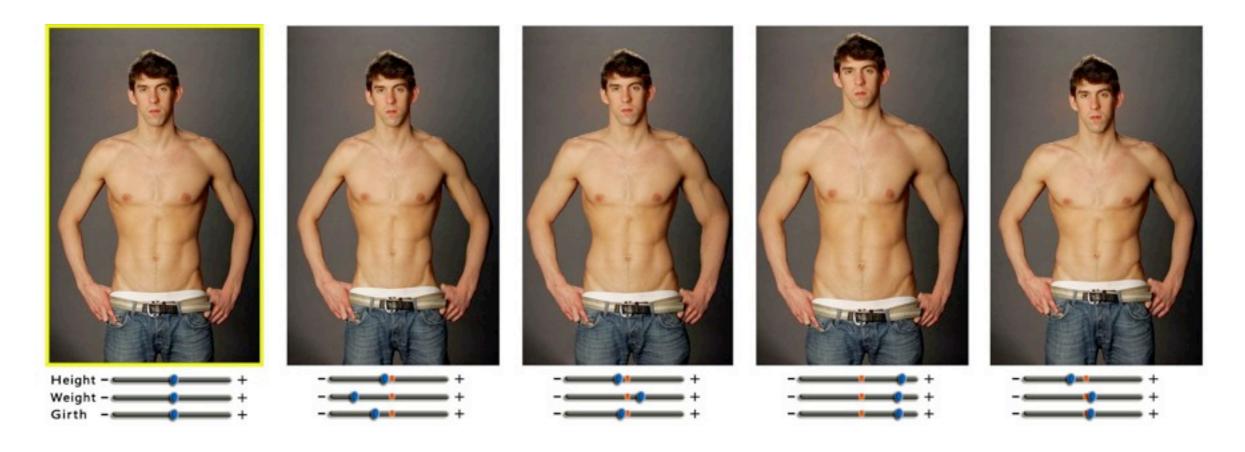


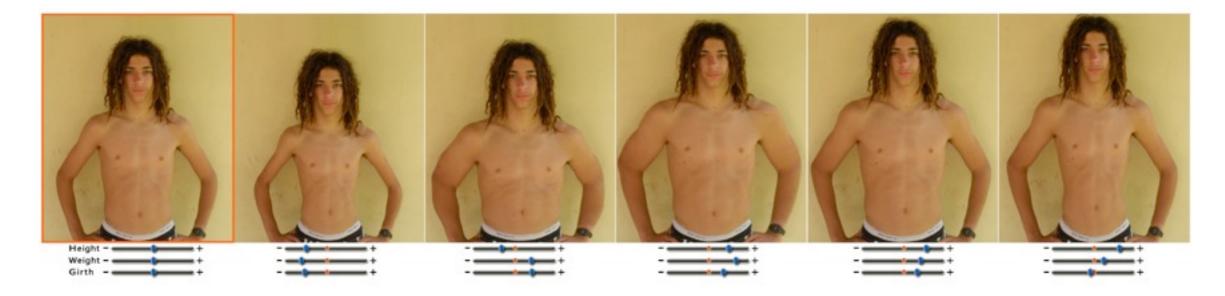
#### Paintings:



# Parametric Body Reshaping

[Zhou et al., ACM TOG, 2010]





# Parametric Body Reshaping

[Zhou et al., ACM TOG, 2010]

