

Graduate Computational Genomics

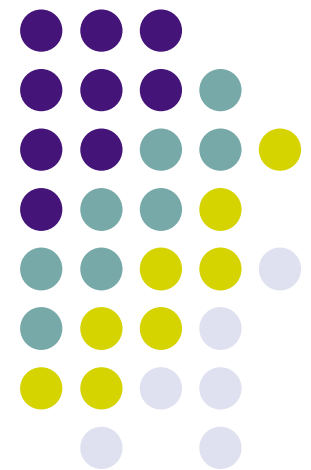
02-710 / 10-810 & MSCBIO2070

Modeling Regulatory Networks (part II)

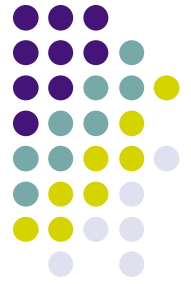
Takis Benos

Lecture #25a, April 24, 2007

Reading: handouts & papers



GRNs: the data sources



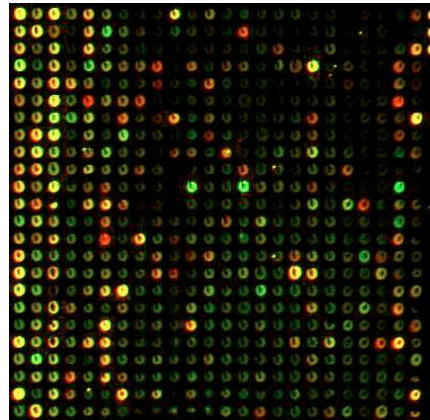
Gene expression



✓ Microarrays

- SAGE
- Real-time RT-PCR

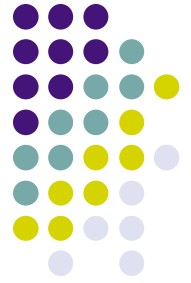
ChIP-chip



✓ Promoter arrays

- Tiling arrays

The study that changed everything



Transcriptional Regulatory Networks in *Saccharomyces cerevisiae*

Tong Ihn Lee,^{1*} Nicola J. Rinaldi,^{1,2*} François Robert,^{1*}
Duncan T. Odom,¹ Ziv Bar-Joseph,³ Georg K. Gerber,³
Nancy M. Hannett,¹ Christopher T. Harbison,^{1,2}
Craig M. Thompson,^{1†} Itamar Simon,¹ Julia Zeitlinger,¹
Ezra G. Jennings,^{1,2} Heather L. Murray,¹ D. Benjamin Gordon,¹
Bing Ren,^{1‡} John J. Wyrick,^{1§} Jean-Bosco Tagne,¹
Thomas L. Volkert,¹ Ernest Fraenkel,¹ David K. Gifford,³
Richard A. Young^{1,2||}

We have determined how most of the transcriptional regulators encoded in the eukaryote *Saccharomyces cerevisiae* associate with genes across the genome in living cells. Just as maps of metabolic networks describe the potential pathways that may be used by a cell to accomplish metabolic processes, this network of regulator-gene interactions describes potential pathways yeast cells can use to regulate global gene expression programs. We use this information to identify network motifs, the simplest units of network architecture, and demonstrate that an automated process can use motifs to assemble a transcriptional regulatory network structure. Our results reveal that eukaryotic cellular functions are highly connected through networks of transcriptional regulators that regulate other transcriptional regulators.

Lee et al.: the method

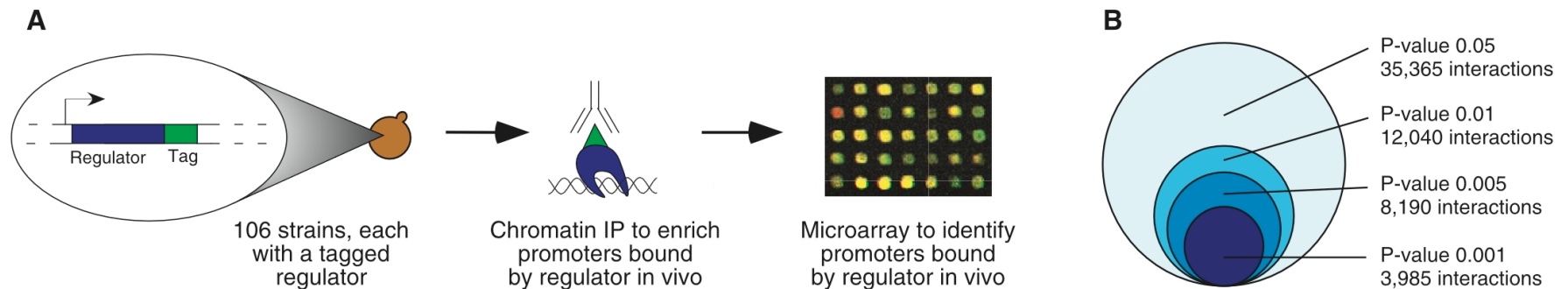
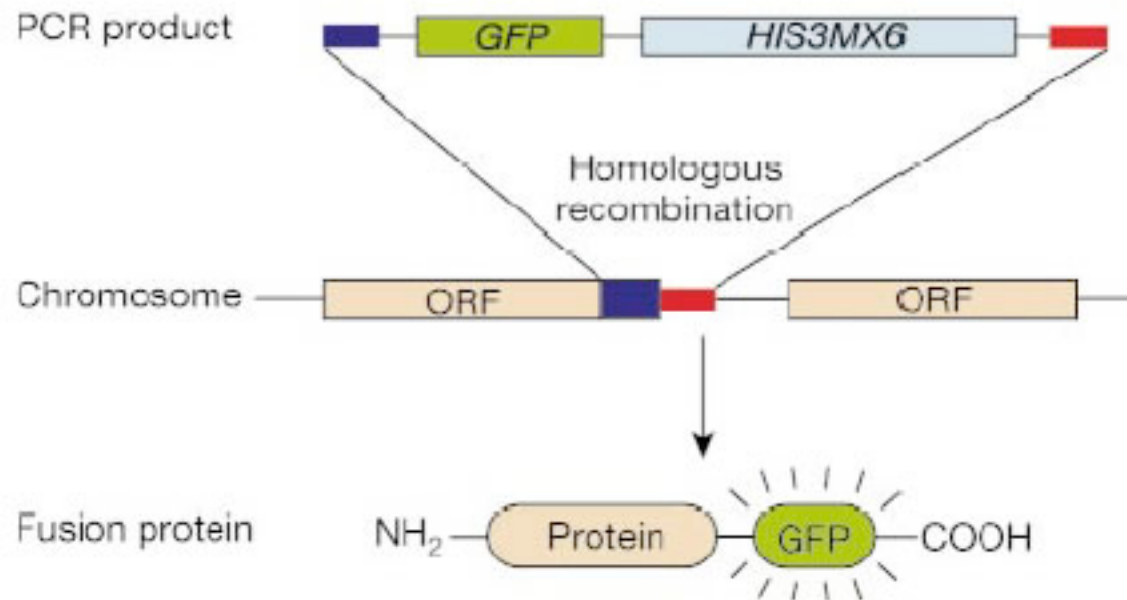
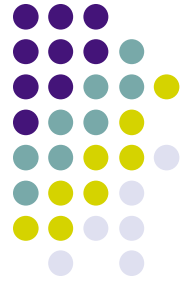


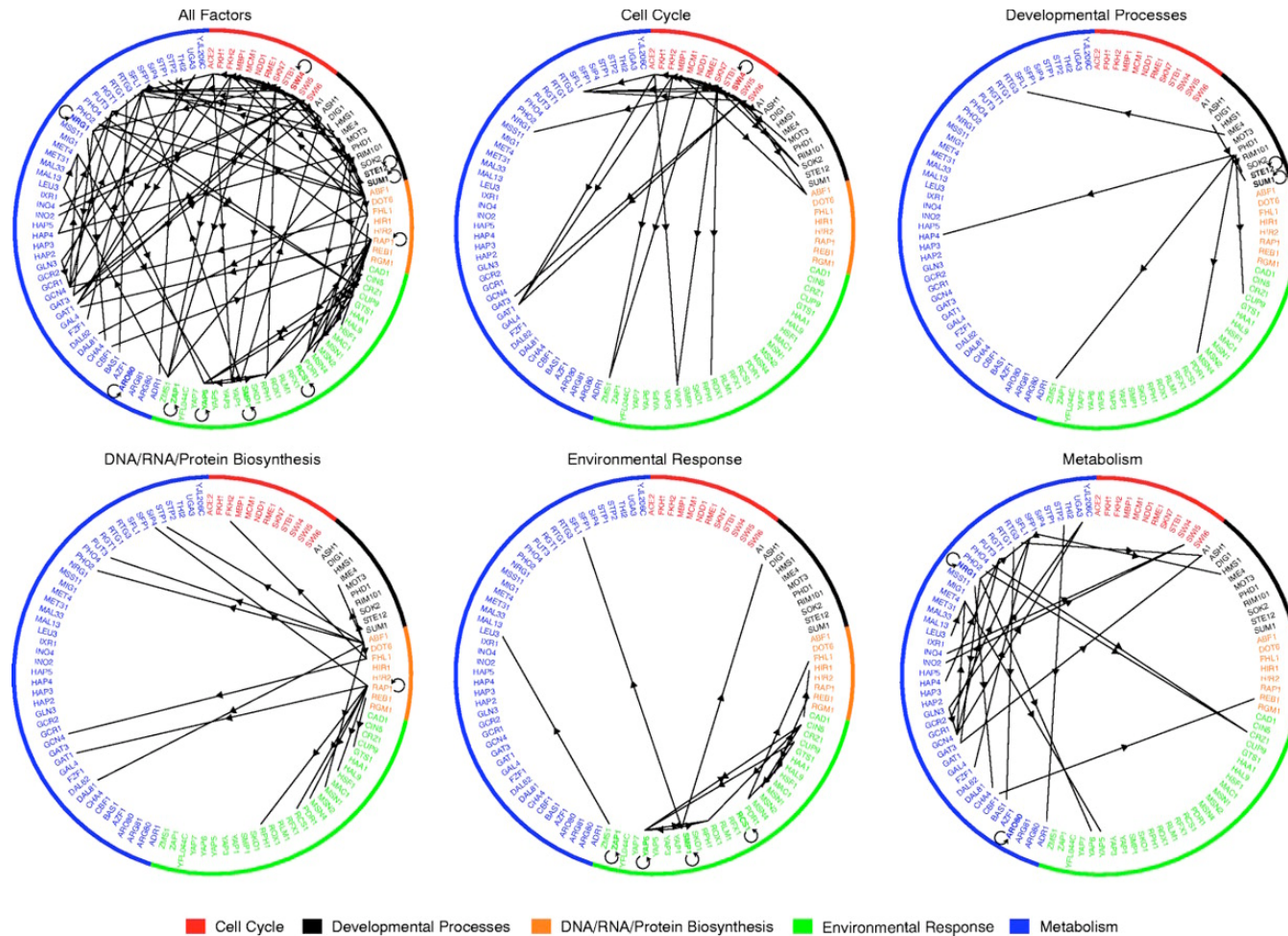
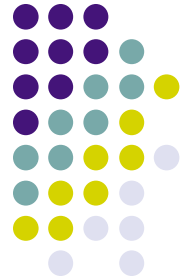
Fig. 1. Systematic genome-wide location analysis for yeast transcription regulators. **(A)** Methodology. Yeast transcriptional regulators were tagged by introducing the coding sequence for a *c-myc* epitope tag into the normal genomic locus for each regulator. Of the yeast strains constructed in this fashion, 106 contained a single epitope-tagged regulator whose expression could be detected in rich growth conditions. Chromatin immunoprecipitation (ChIP) was performed on each of these

106 strains. Promoter regions enriched through the ChIP procedure were identified by hybridization to microarrays containing a genome-wide set of yeast promoter regions. **(B)** Effect of *P* value threshold. The sum of all regulator-promoter region interactions is displayed as a function of varying *P* value thresholds applied to the entire location data set for the 106 regulators. More stringent *P* values reduce the number of interactions reported but decrease the likelihood of false-positive results.

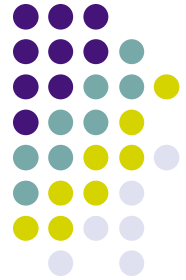
Homologous recombination



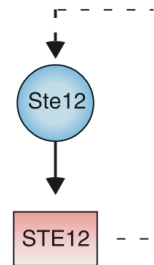
Lee et al.: the results



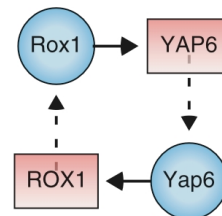
Lee et al.: the results (*cntd*)



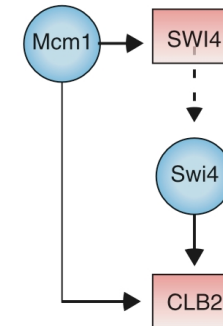
Autoregulation



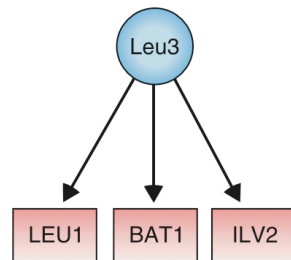
Multi-Component Loop



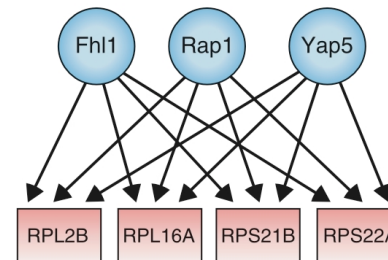
Feedforward Loop



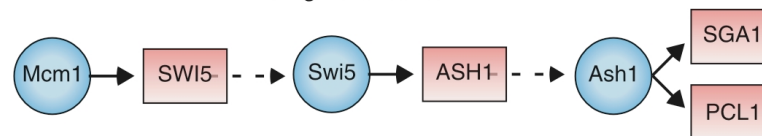
Single Input Motif



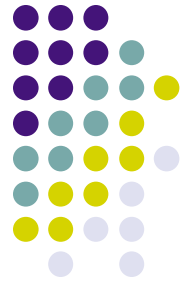
Multi-Input Motif



Regulator Chain



Gao *et al.*: combining ChIP-chip and microarray data



Research article

Highly accessed

Open Access

Defining transcriptional networks through integrative modeling of mRNA expression and transcription factor binding data

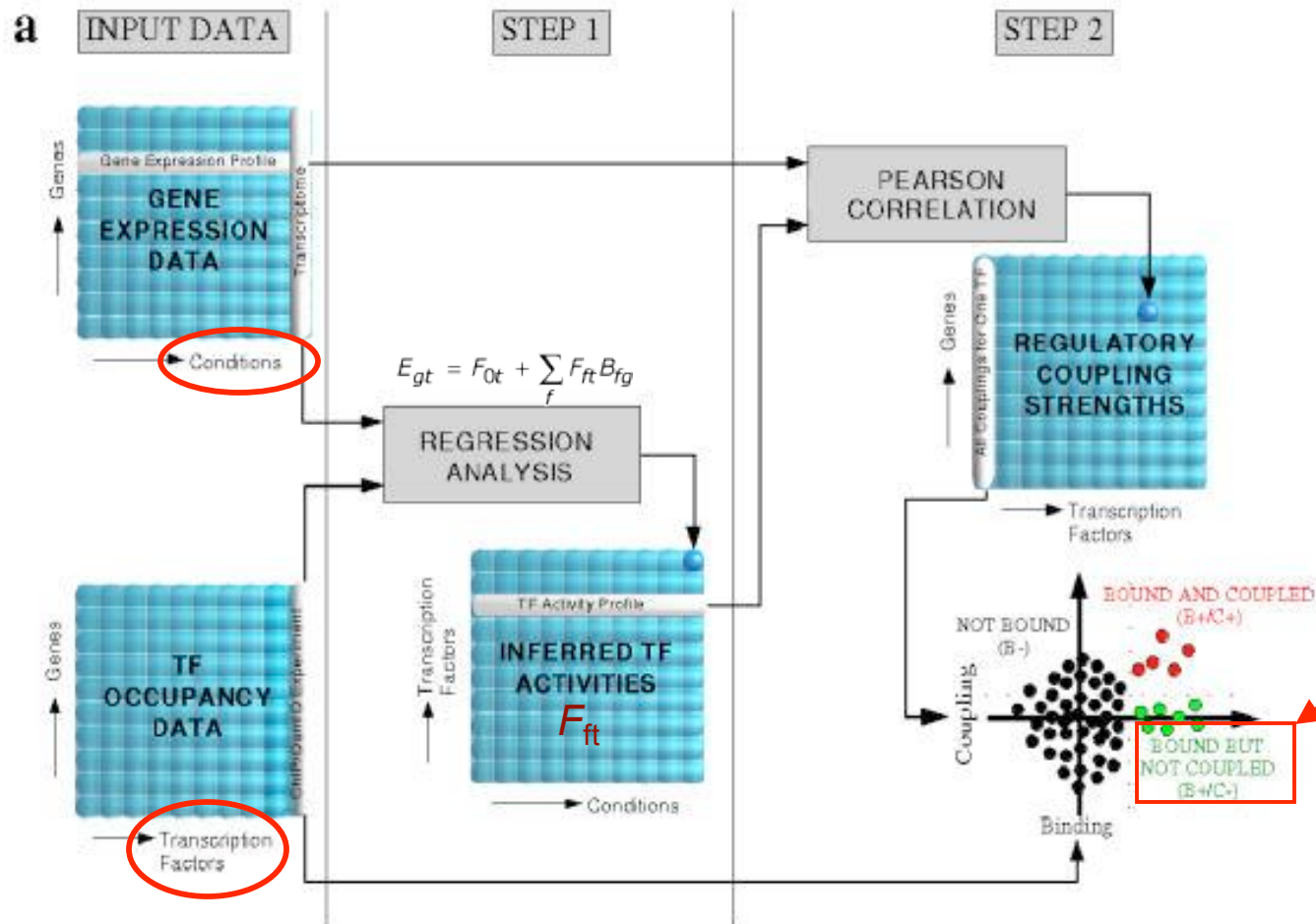
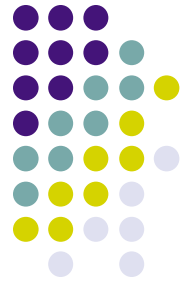
Feng Gao¹ ✉, **Barrett C Foat¹** ✉ and **Harmen J Bussemaker^{1,2}** ✉

¹Department of Biological Sciences, Columbia University, New York, New York 10027, U.S.A

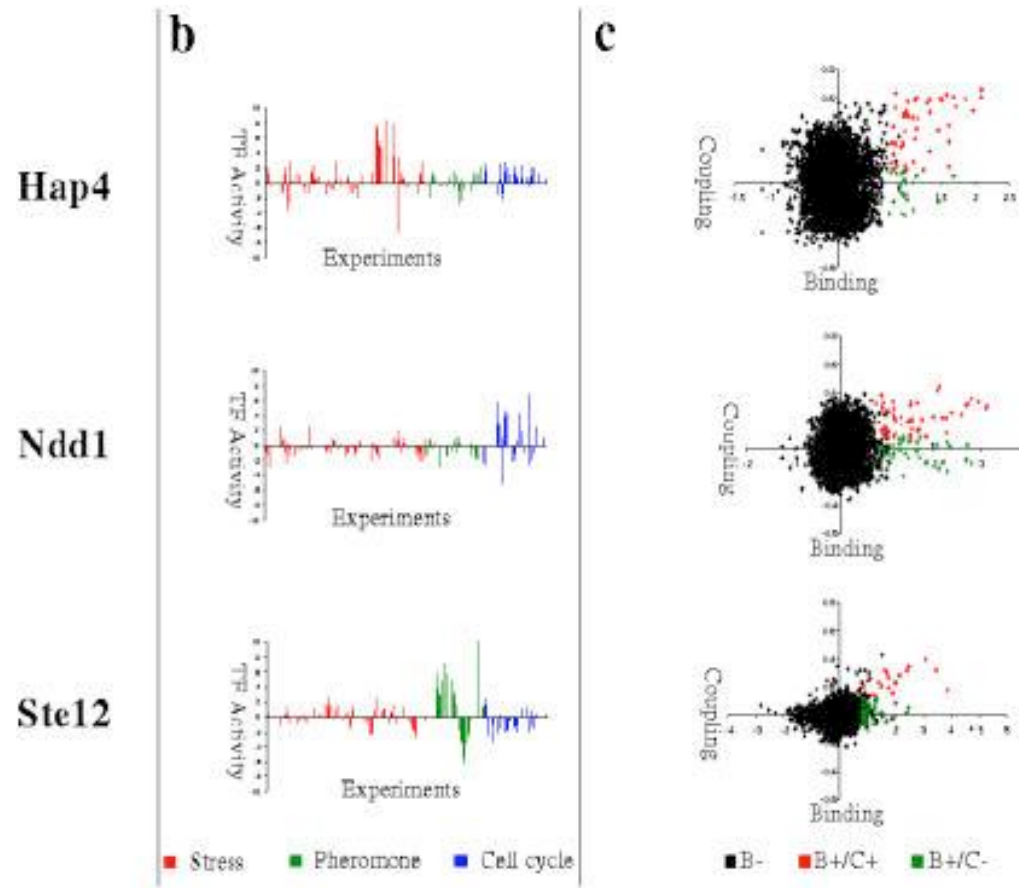
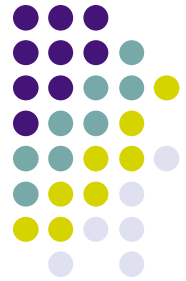
²Center for Computational Biology and Bioinformatics, Columbia University, New York, New York 10032, U.S.A

BMC Bioinformatics 2004, **5**:31 doi:10.1186/1471-2105-5-31

Gao *et al.*: the method



Gao *et al.*: results





Gao *et al.*: results (cntd)

Classification of genes according to ChIP data and inferred regulatory coupling.

TF	B-	B+/C+	B+/C-	Unclassified*
Abf1	5638	138	136	470
Ace2	5843	33	33	473
Arg81	5985	11	10	376
Bas1	5975	28	13	366
Cad1	5854	26	13	489
Dal81	5823	24	16	519
Dig1	5872	20	11	479
Fhl1	5754	146	37	445
Fkh2	5261	61	45	1015
Gal4	5149	20	20	1193
Gat3	5891	40	29	422
Gcn4	5919	58	21	384
Hal9	5948	4	13	417
Hap4	5939	47	21	375
Hir1	5963	19	10	390

Gao *et al.*: results (cntd)



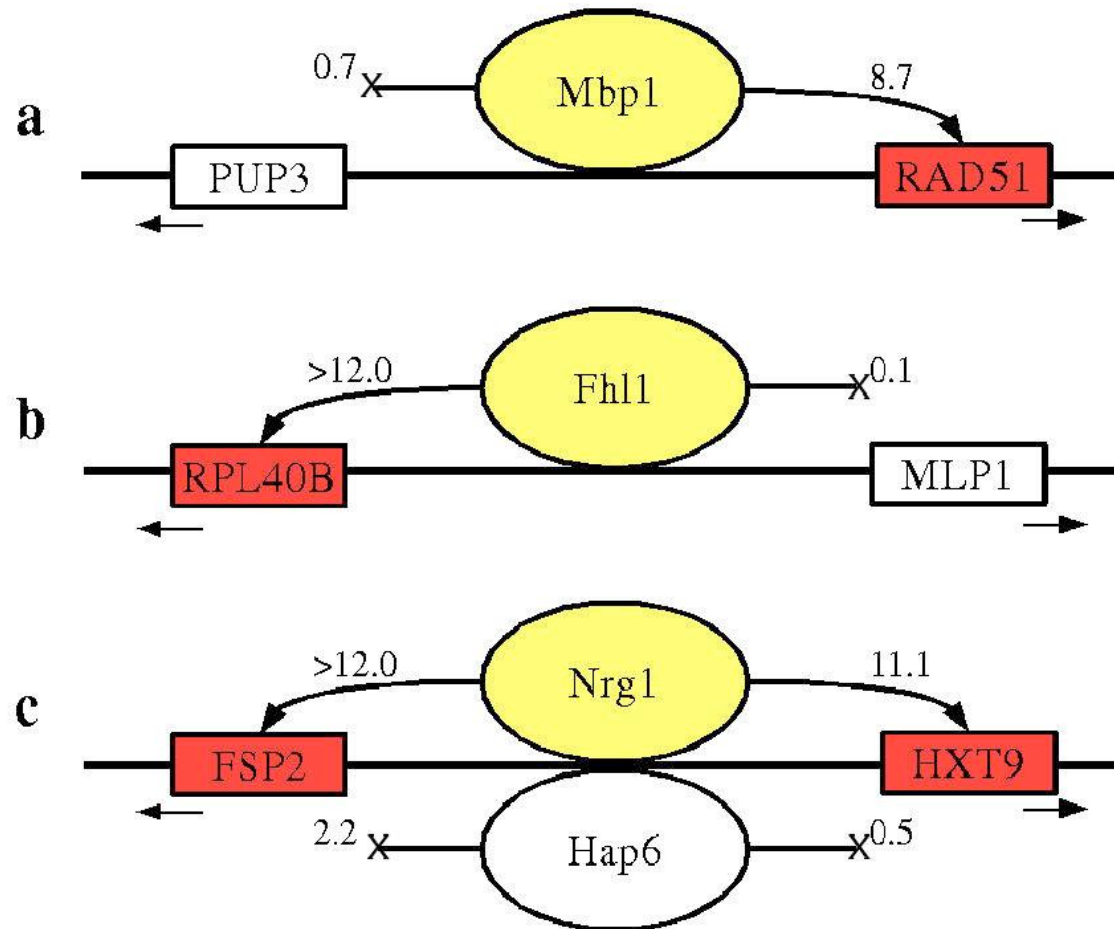
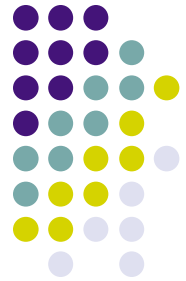
Table 2

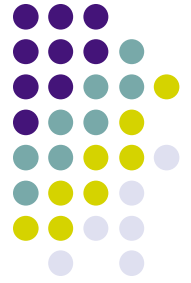
Analysis of transcriptional response to transcription factor deletion.

Transcription Factor	Genomewide		B+/C+			B+/C-		
	Mean	SD	Mean	SD	$-\log_{10}(p)$	Mean	SD	$-\log_{10}(p)$
Dig1	0.759	0.198	0.567	0.360	3.76	0.846	0.080	0.04
Gcn4	0.785	0.177	0.294	0.329	28.23	0.793	0.170	0.24
Hir2	0.724	0.218	0.180	0.295	4.00	0.760	0.194	0.14
Mbp1	0.830	0.121	0.541	0.324	27.86	0.770	0.172	2.79
Swi4	0.524	0.338	0.348	0.352	4.89	0.533	0.333	0.24
Swi5	0.744	0.204	0.583	0.373	5.98	0.759	0.186	0.17
Yap1	0.756	0.201	0.471	0.376	7.66	0.587	0.337	2.67

The mean and the standard deviation of gene expression log-ratio between mutant and wild type as obtained in Hughes *et al.* were calculated for all genes in the genome as well as for the B+/C+ and B+/C- groups [21]. A sample t-test was performed to determine the significance of the change in expression. The B+/C+ genes show a significant change in mRNA expression for the 7 transcription factors for which deletion and ChIP data is available. By contrast, the response of the B+/C- genes is insignificant for most transcription factors.

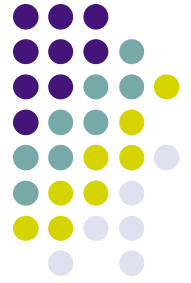
Gao *et al.*: results (cntd)





Gao *et al.*: Conclusions

- A new method that combines both ChIP and gene expression data to assess transcription regulation.
- Half of the TF targets resulting from the ChIP assay ($p < 10^{-3}$) are non-functional. (*why?*)
 - ChIP false positives
 - Competition with other factors
 - Chromatin structure



For some reading

- Lee *et al.*, “*Transcriptional regulatory networks in Saccharomyces cerevisiae*” (2002) *Science* **298**: 799-804.
- Gao *et L.*, “*Defining transcriptional networks through integrative modeling of mRNA expression and transcription factor binding data*” (2004) *BMC Bioinformatics* **5**: 31.

Graduate Computational Genomics

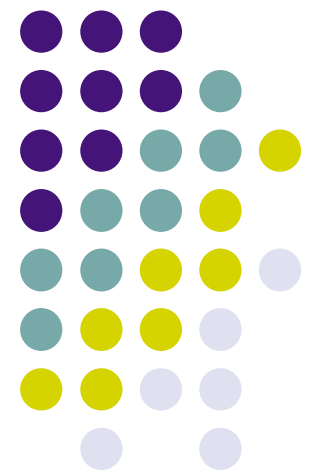
02-710 / 10-810 & MSCBIO2070

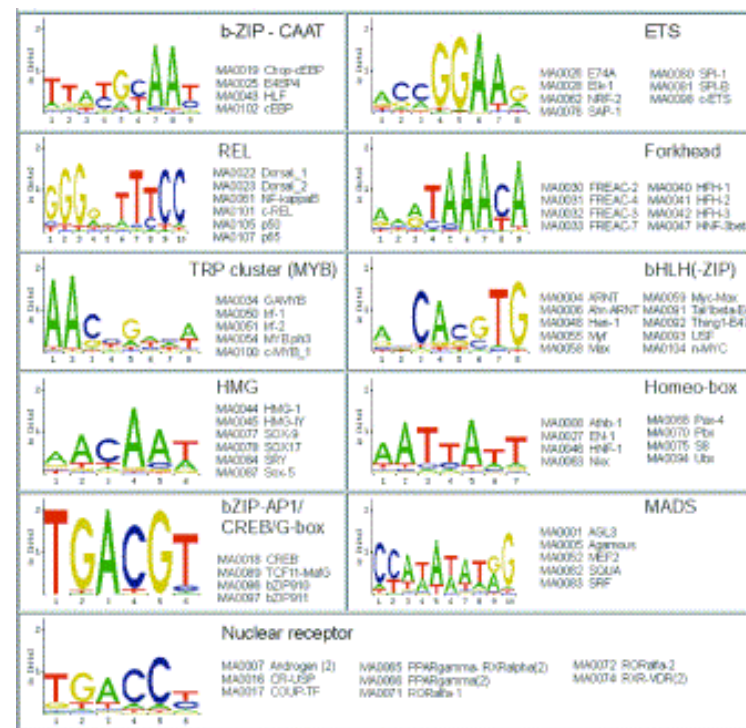
Evolution of regulatory regions and binding motifs

Takis Benos

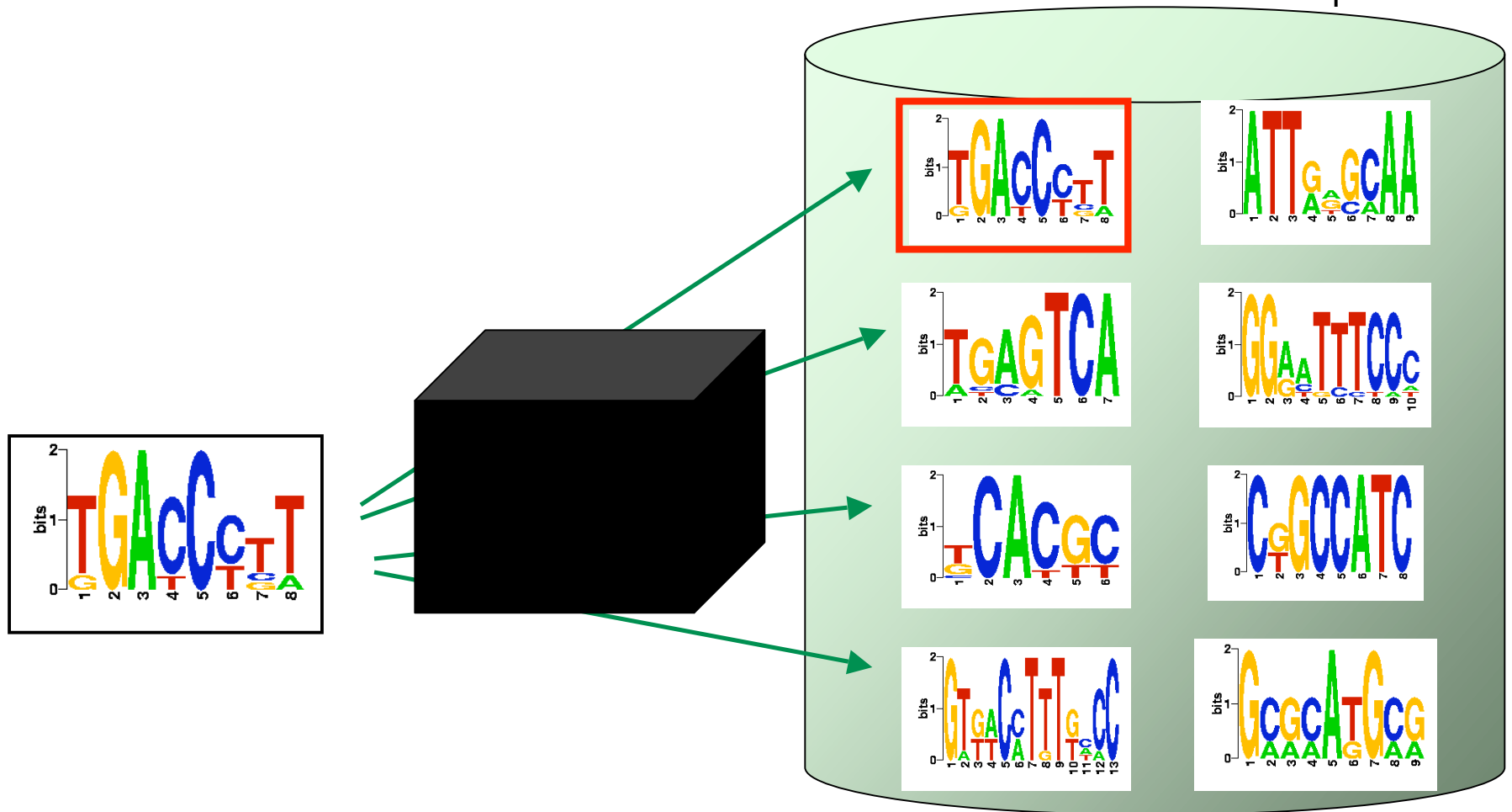
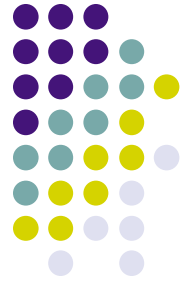
Lecture #25b, April 24, 2007

Reading: handouts & papers



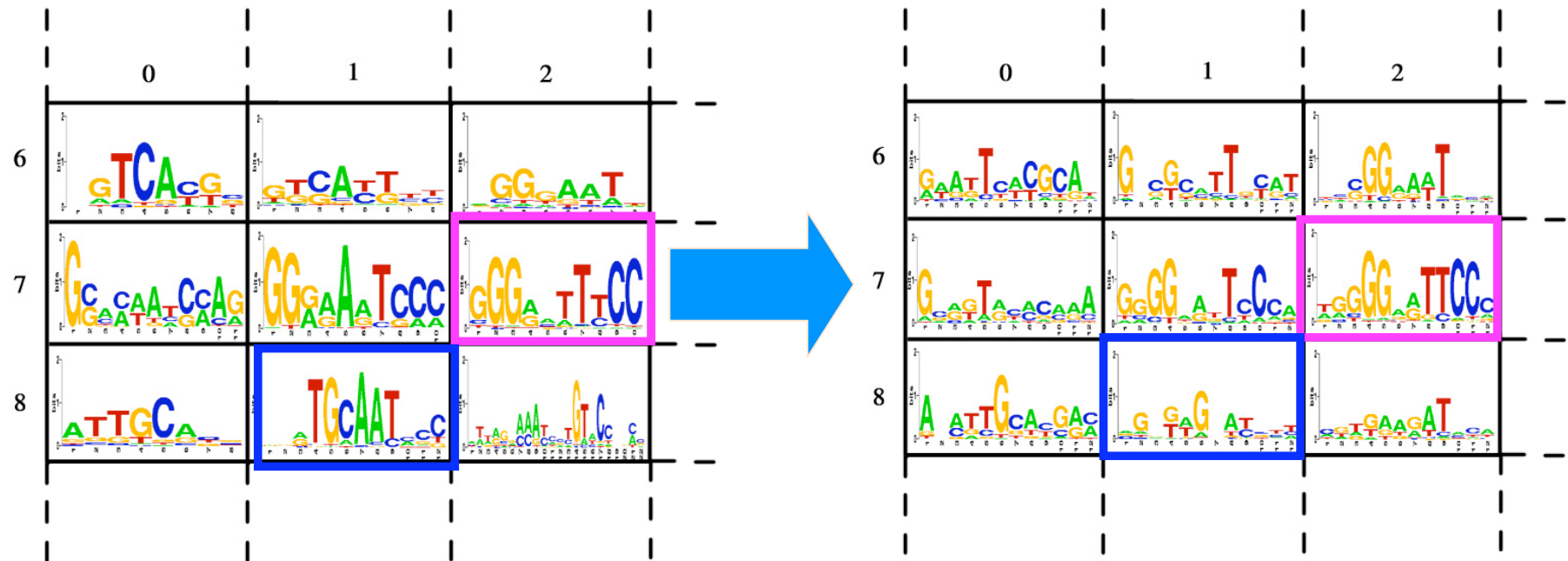


Comparing motifs



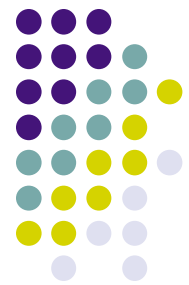


SOMBRERO & FBP Priors



Start: BP-SOM trained on 257 mammalian PSSMs (incl. REL)

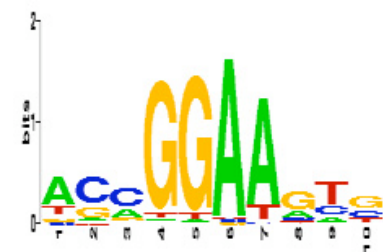
Finish: SOMBRERO used to find motifs of NF- κ B (REL-class).



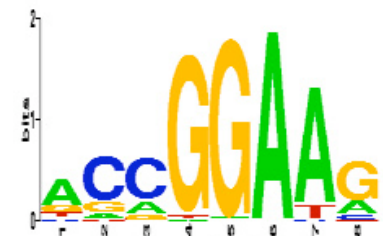
Binding Profile SOM (BP-SOM)

bHLH Tallbeta-E47S bHLH Thing1-E47	NUCLEAR Androgen HMG HMG-1	REL Dorsal_1	TRP-CLUSTER MYB.ph3 TRP-CLUSTER c-MYB_1 TRP-CLUSTER GAMYB
FORKHEAD HFH-2 FORKHEAD HNF-3b FORKHEAD HFH-1 FORKHEAD HFH-3 FORKHEAD FREAC-2 FORKHEAD FREAC-4	MADS AGL3 MADS MEF2 FORKHEAD FREAC-7	NUCLEAR RORalfa-1 NUCLEAR RORalfa-2	ETS SAP-1 ETS SPI-B ETS NRF-2 ETS SPI-B ETS E74A ETS c-ETS ETS Elk-1
MADS Agamous	MADS SRF	HMG SOX-9 HMG Sox-5 HMG SOX17 HMG SRY	HOMEO Nkx HOMEO S8
bZIP HLF bZIP E4BP4 bZIP cEBP bZIP CREB	bHLH-ZIP Max bHLH-ZIP USF bHLH-ZIP n-MYC bHLH-ZIP Myc-Max bHLH ARNT bZIP bZIP911 bZIP TCF11 bZIP bZIP910	TRP_CLUSTER Irf-1 TRP_CLUSTER Irf-2	bHLH Hen-1 bHLH Ahr-ARNT FORKHEAD FREAC-3
MADS SQUA HOMEO HNF-1 HMG HMG-IY	bHLH Myf	NUCLEAR CFI-USP NUCLEAR COUP-TF NUCLEAR RXR-VDR NUCLEAR PPARgamma NUCLEAR PPARgamma-rxr	REL p65 REL NF-kB REL p50 REL Dorsal_2 REL c-REL HOMEO EN-1 bZIP Chop-cEBP

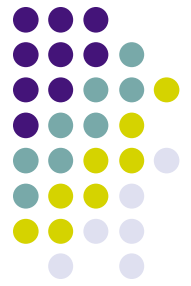
ETS



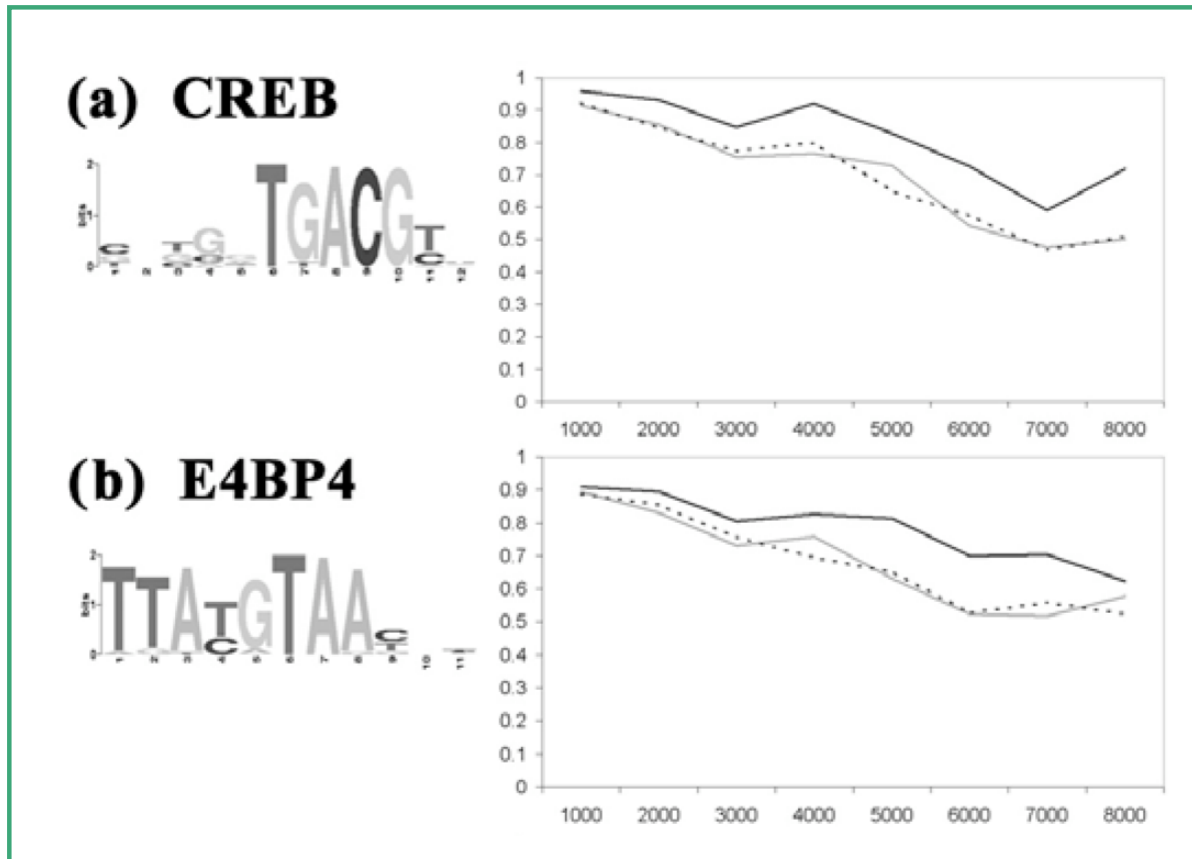
BP-SOM



Sandelin
&
Wasserman

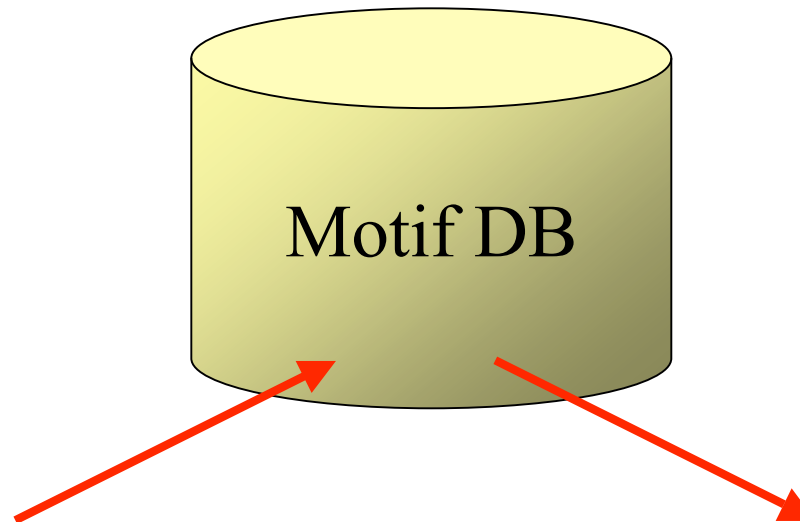
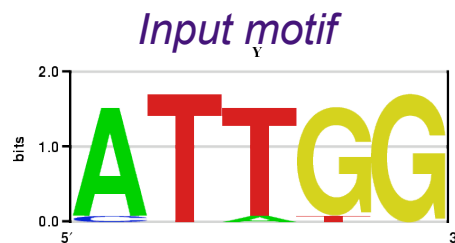
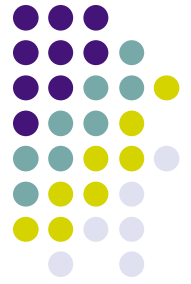


SOMBRERO: results



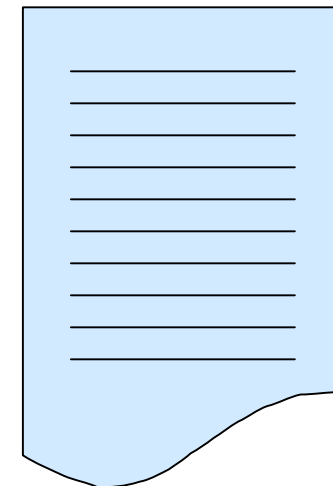
— Gradient-Random Initialization
..... Random Initialization
— Prior Initialization

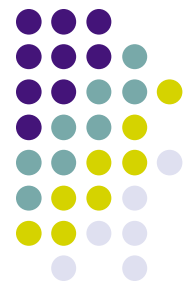
BLAST-like motif searches



Name	No. of TFs	Accuracy	
		Best-hit	Bayesian learning
bZIP	93	0.94	0.92
C2H2	74	0.76	0.77
C4	52	0.98	0.91
Homeo	50	0.82	0.85
Forkhead	49	0.90	0.83
bHLH	37	0.81	0.88
<i>Average</i>		0.87	0.86

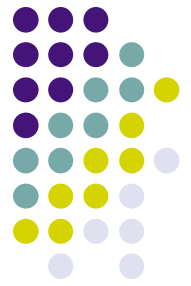
List of motif "hits"



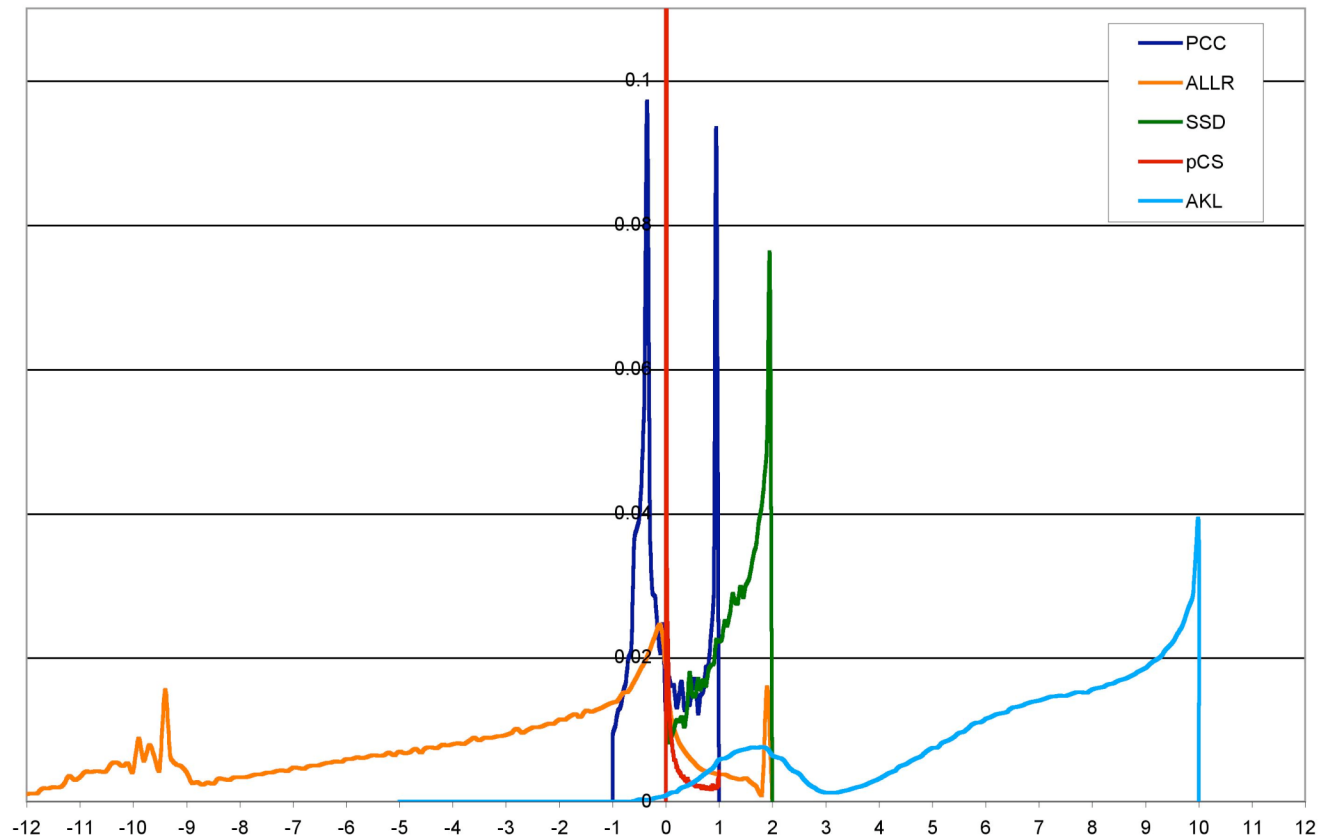


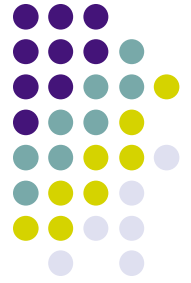
The tools: distance metrics

Similarity metric	Formula
Pearson Correlation Coefficient (PCC)	$PCC(X,Y) = \frac{\sum_{b=A}^T (f_X(b) - \overline{f_X}) \cdot (f_Y(b) - \overline{f_Y})}{\sqrt{\sum_{b=A}^T (f_X(b) - \overline{f_X})^2 \cdot \sum_{b=A}^T (f_Y(b) - \overline{f_Y})^2}}$
Chi-square (pCS) (1 - p-value of)	$\chi^2_3(X,Y) = \sum_{K=\{X,Y\}} \sum_{b=A}^T \frac{(n_K(b) - n_K^e(b))^2}{n_K^e(b)}$
Average Kullback-Leibler (AKL)	$AKL(X,Y) = 10 - \frac{\sum_{b=A}^T f_X(b) \cdot \log \frac{f_X(b)}{f_Y(b)} + \sum_{b=A}^T f_Y(b) \cdot \log \frac{f_Y(b)}{f_X(b)}}{2}$
Sum of squared distances (SSD)	$SSD(X,Y) = 2 - \sum_{b=A}^T (f_X(b) - f_Y(b))^2$
Average Log-likelihood Ratio (ALLR)	$ALLR(X,Y) = \frac{\sum_{b=A}^T n_X(b) \cdot \log \frac{f_Y(b)}{p_{ref}(b)} + \sum_{b=A}^T n_Y(b) \cdot \log \frac{f_X(b)}{p_{ref}(b)}}{\sum_{b=A}^T (n_X(b) + n_Y(b))}$
ALLR with Lower Limit (ALLR_LL)	Same as above, but a lower limit of -2 is imposed on the score (see text)

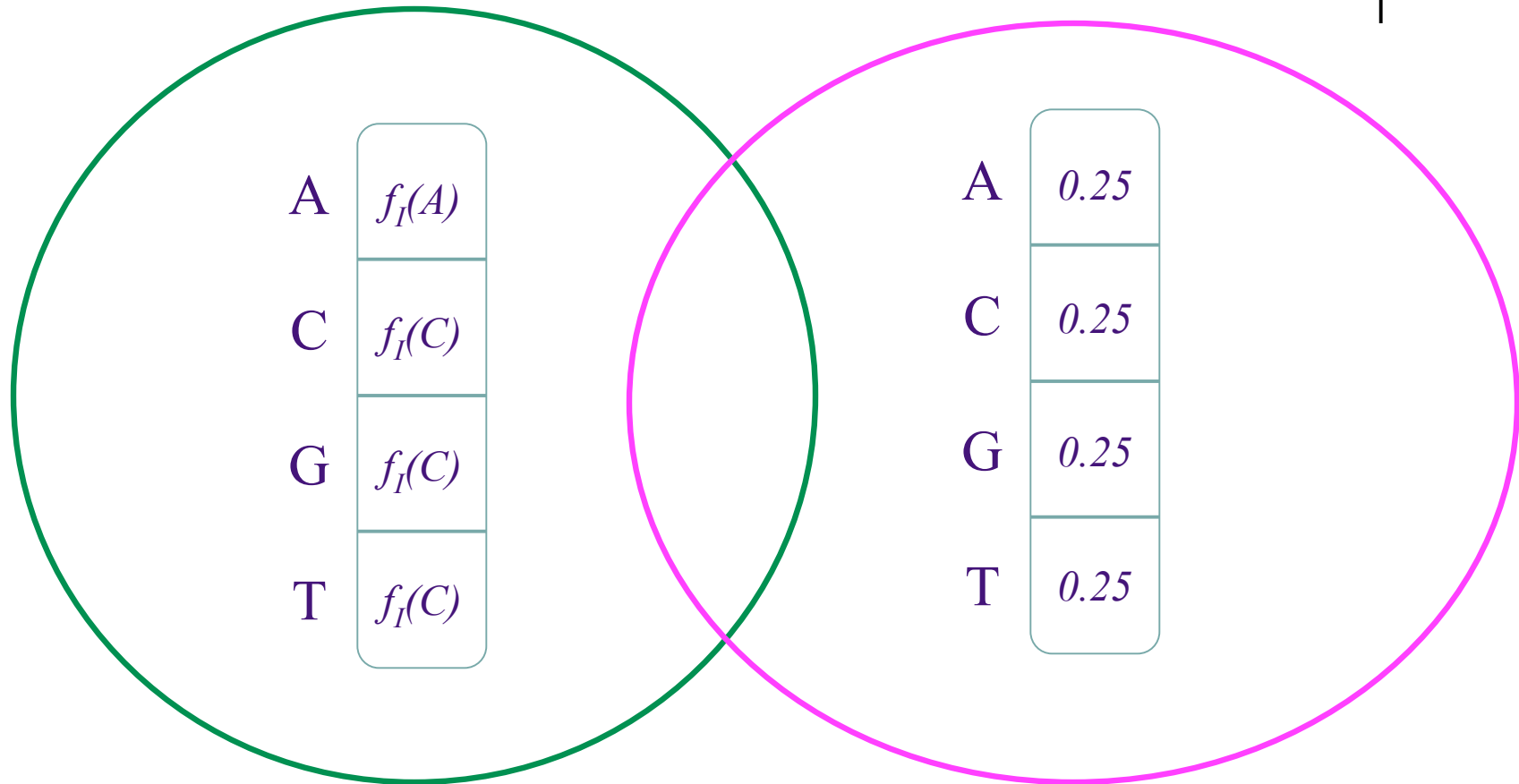


Distance metrics (cntd)



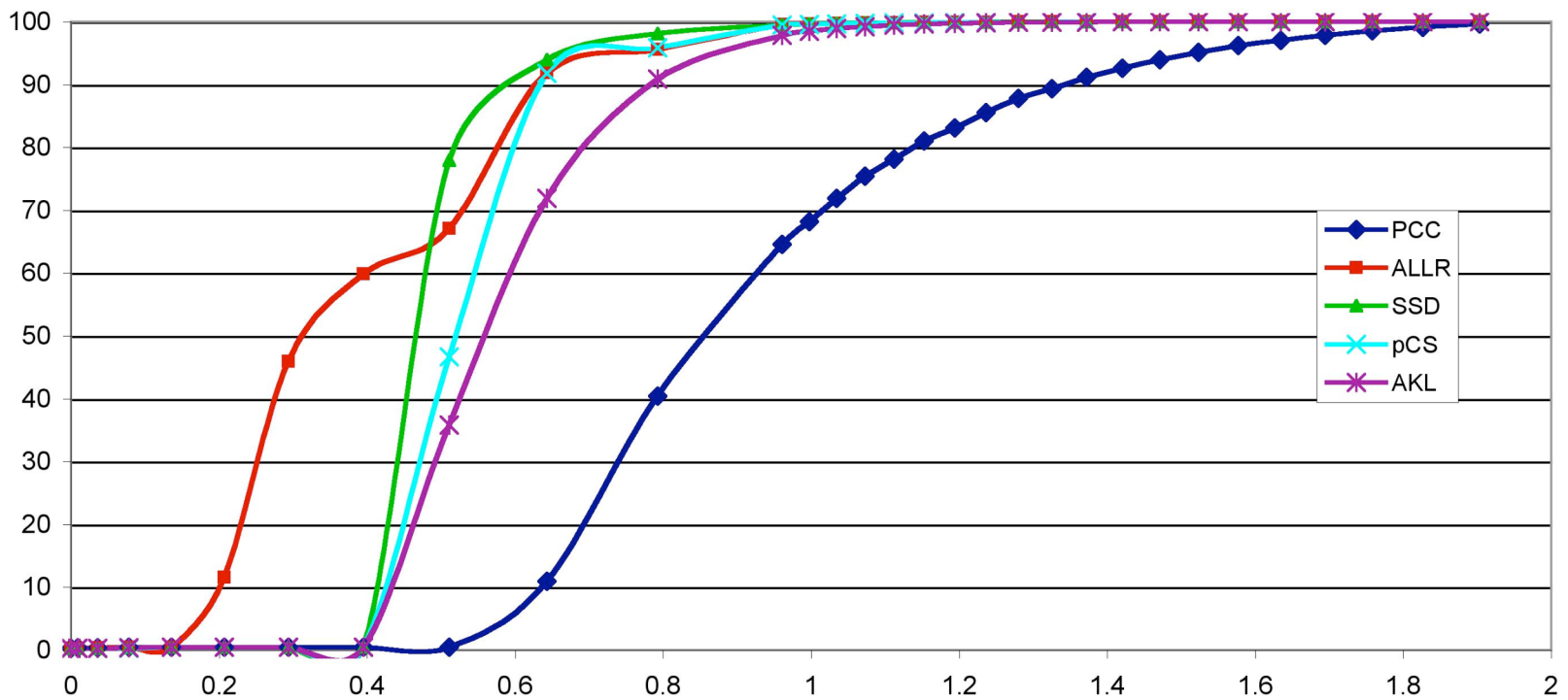
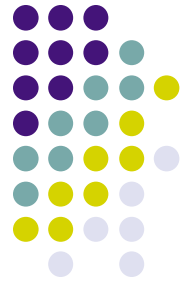


Distance metrics (cntd)

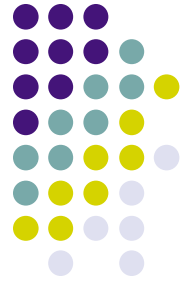


$$H = \sum_{b=A}^T f_I(b) \cdot \log_2 f_I(b)$$

Distance metrics (cntd)



The tools: alignments and trees



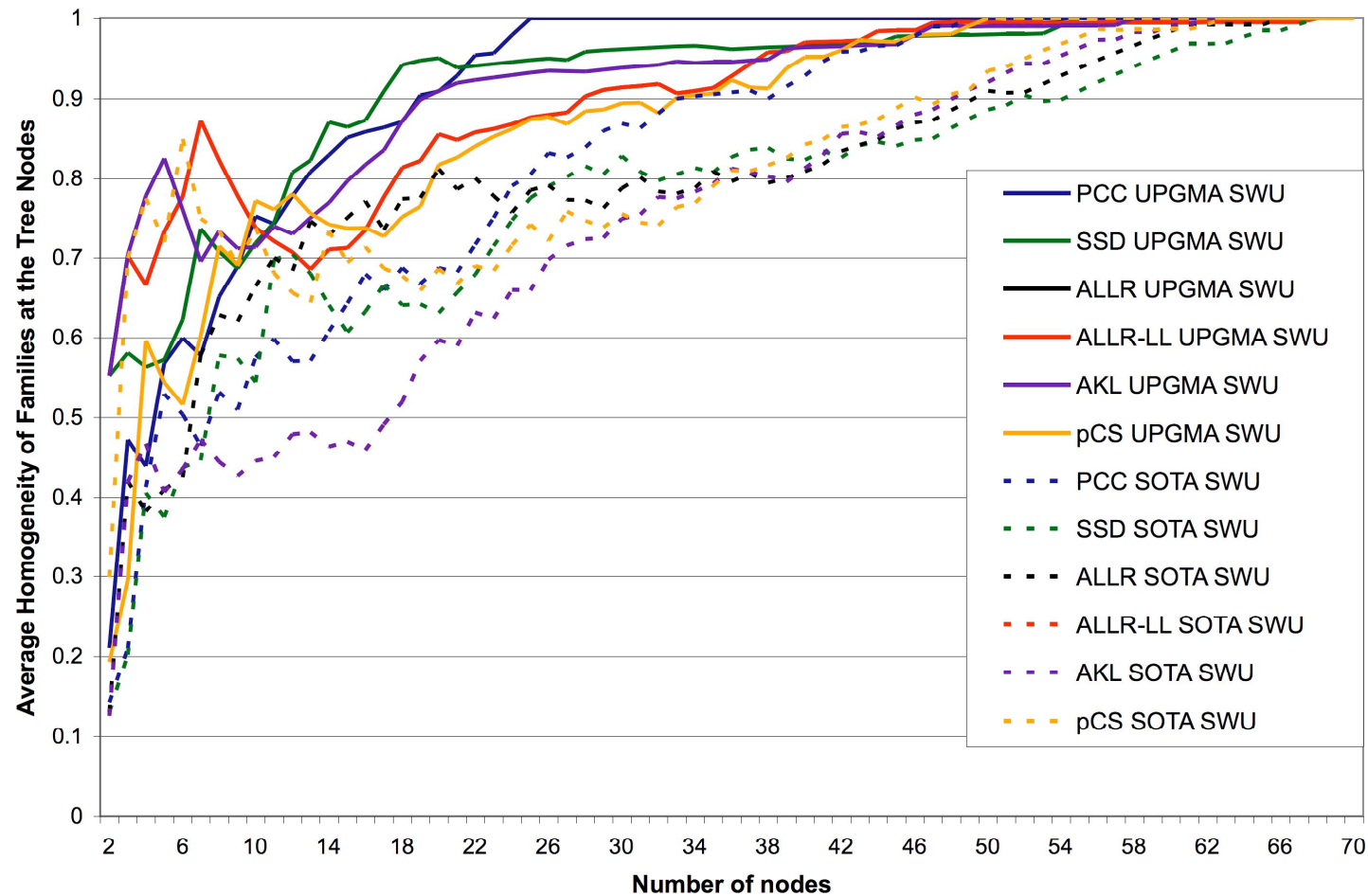
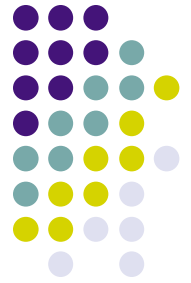
- Alignment methods:
 - Needleman-Wunsch
 - Smith-Waterman
- Tree-building methods:
 - UPGMA
 - SOTA

Motif alignments



Alignment algorithm	Similarity metric	Gap open	JASPAR non-ZNF	JASPAR ZNF	TRANSFAC non-ZNF	TRANSFAC ZNF	Avg
S W	SS D	1.00	0.845	0.480	0.833	0.788	0.811
SW (ovrlp)	SS D	1.00	0.845	0.480	0.833	0.788	0.811
S W	SS D	0.75	0.845	0.440	0.831	0.794	0.809
SW (ovrlp)	SS D	0.75	0.845	0.440	0.831	0.794	0.809
S W	SS D	0.50	0.845	0.520	0.824	0.794	0.808
SW (ovrlp)	SS D	0.50	0.845	0.520	0.824	0.794	0.808
S W	PCC	1.50	0.845	0.520	0.817	0.800	0.808
S W	SS D	0.25	0.859	0.560	0.808	0.806	0.804
SW (ovrlp)	SS D	0.25	0.859	0.560	0.808	0.806	0.804
S W	PCC	1.00	0.831	0.600	0.815	0.788	0.802
SW (ovrlp)	PCC	1.00	0.831	0.600	0.812	0.788	0.801
SW (ungap)	PCC	N/A	0.887	0.600	0.812	0.763	0.801
S W	PCC	1.50	0.845	0.520	0.810	0.800	0.801
N W	SS D	1000	0.859	0.480	0.817	0.781	0.801
S W	SS D	1000	0.859	0.480	0.817	0.781	0.801
...	...	...	...	...	...	...	...
N W	pCS	0.75	0.662	0.600	0.657	0.675	0.660
N W	pCS	1.00	0.662	0.440	0.653	0.688	0.654
N W	pCS	0.50	0.690	0.560	0.653	0.650	0.652
N W	pCS	0.25	0.634	0.640	0.650	0.656	0.650
N W	ALLR	5.00	0.634	0.480	0.648	0.619	0.633
N W	AKL	4.00	0.704	0.400	0.594	0.600	0.600
N W	pCS	2.00	0.563	0.400	0.596	0.656	0.600
N W	SS D	1.00	0.634	0.480	0.585	0.581	0.585
N W	PCC	1.50	0.606	0.520	0.580	0.581	0.581
N W	PCC	2.00	0.521	0.480	0.423	0.500	0.453
N W	ALLR	10.00	0.394	0.440	0.343	0.400	0.365
N W	SS D	2.00	0.437	0.400	0.324	0.375	0.350
N W	ALLR	15.00	0.268	0.400	0.261	0.381	0.295
N W	PCC	4.00	0.282	0.480	0.282	0.269	0.286
N W	ALLR	20.00	0.268	0.440	0.232	0.306	0.261

Tree-building



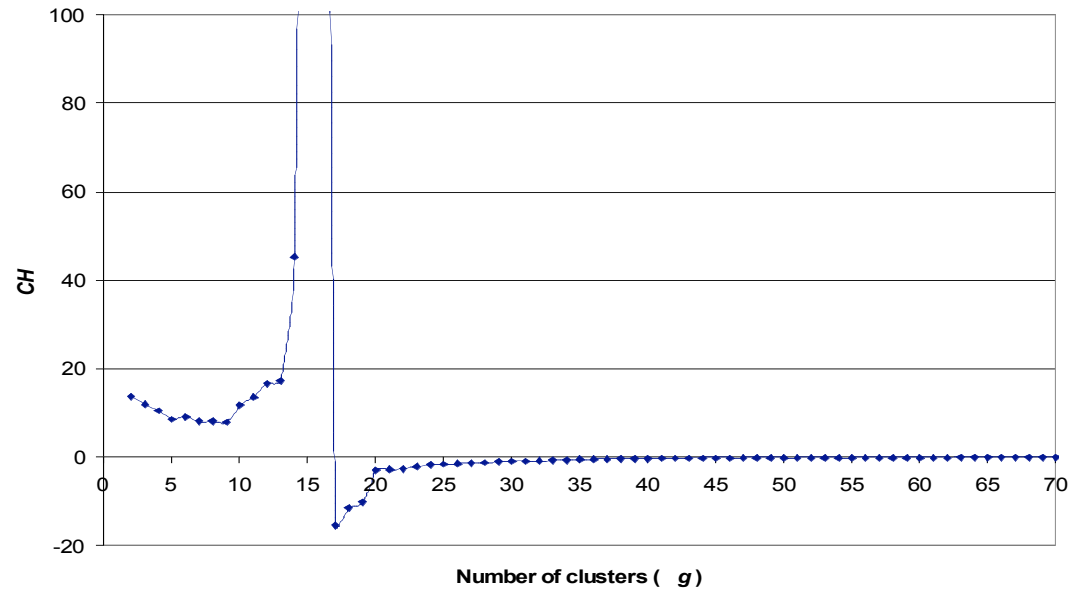
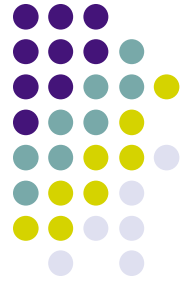


Automatic clustering statistics



Statistic	Formula
Hastie, Tibshirani, Walter (<i>HTW</i>)	$Gap_n(g) = E_n^*(\log(W_g)) - \log(W_g)$
Calinski & Harabasz (<i>CH</i>)	$CH = \frac{\mathbf{B}/(g-1)}{\mathbf{W}/(n-g)}$
Log-modified Calinski & Harabasz (<i>CH_{log}</i>)	$CH_{\log} = \frac{\log(\mathbf{B})/(g-1)}{\log(\mathbf{W})/(n-g)}$

Automatic motif clustering

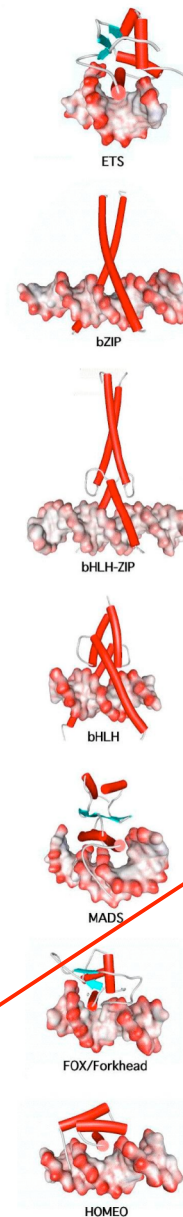
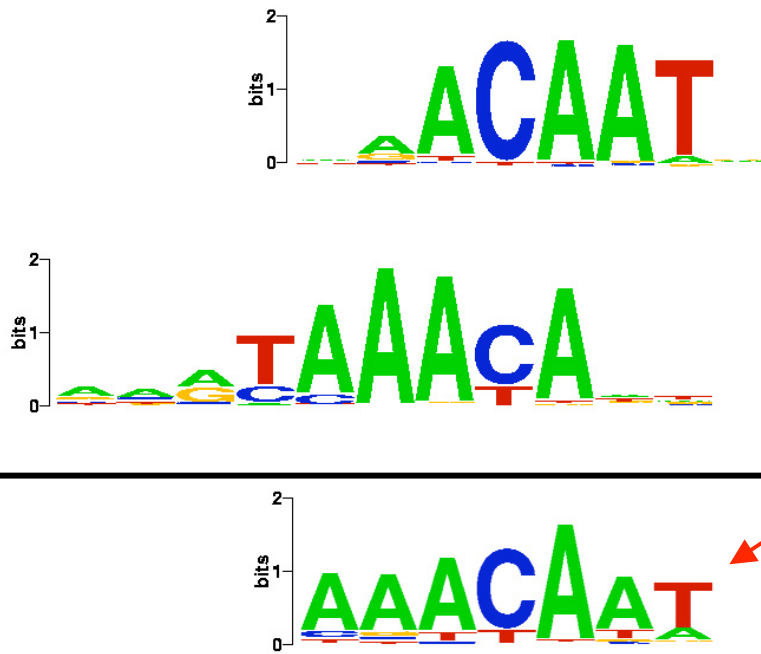


Dataset	Jackknife cross-validation	
	STAMP	Sandelin & Wasserman
Full set (79 motifs)	91% (72/79)	76% (60/79)
Non-zinc fingers (71 motifs)	94% (67/71)	87% (62/71)

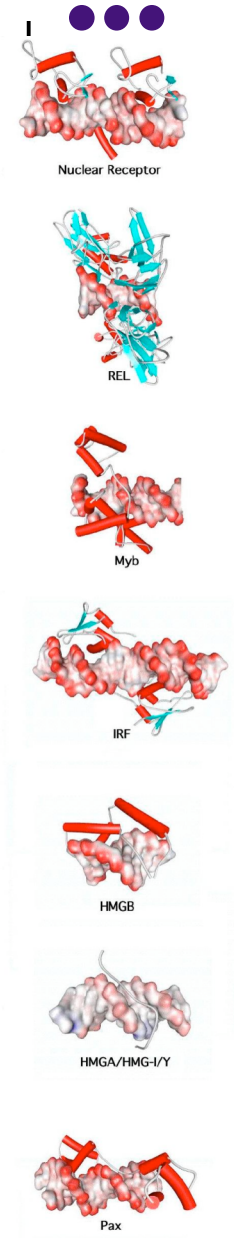
New FBP's!

Forkhead Subgroup: HMG Subgroup:
Foxd1, Foxf2, Foxq1, Sox5, Sox9,
Foxi1, Foxa2, Foxd3 Sox17, SRY

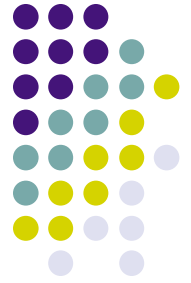
**HMG/Forkhead
Group FBP**



ETS Members: ETS: c-ETS, SP1, SPIB, ELK1, ELK4, E74A, GABPA	Nuclear Receptor Members: Nuclear Receptor: PPARG-RXRα, NR2F1, RXRA, RXR, RXR-VDR, PPARG, C/EBP
bZIP CREB Subgroup Members: bZIP CREB: TCF11-MaTG, CREB1, bZIP911, bZIP910	REL-like group Members: REL: Dorsal 1, Dorsal 2, REL, NF-κB, RELA, NFKB1, HOME: Ets1, bZIP, C/EBP
bHLH-ZIP Members: bHLH: Arnt-Ahr, MYC-MAX, MAX, Arnt, USF1, Myc	bHLH Subgroup 1 Members: bHLH: TAL1-TCF3, HAND1-3
bHLH Subgroup 2 Members: bHLH: Myf, NHLH1	TRP-cluster, Myb Subgroup Members: TRP-cluster: GAMYB, Myb, MYB p13
bZIP cEBP Subgroup Members: bZIP cEBP: cEBP, NLI3, HLF	TRP-cluster, IRF Subgroup Members: TRP-cluster: IRF1, IRF2
MADS Members: MADS: Agmatin, SRF, ME2A, AGL3, SQUA	HMG/Forkhead Group 1 Members: Forkhead: FOXD1, FOXF2, Foxq1, FOXH1, Foxa2, Foxd3, HMG: Sox17, Sox9, SRY, Sox, HOME: Pax
HMG/Forkhead Group 2 Members: HMG: HMG-1, Forkhead: FOXC1	HMG/HOME Mix. Members: HMG: HMG-1Y, HOME: Pax-4
HOME Subgroup Members: HOME: Ubx, Nkx2-5, Pbx2, Atf1-1, TCF1	FOX11 Singleton Members: Forkhead: FOX11
Ar Singleton Members: Nuclear Receptor: Ar	



For some more reading



- Mahony, Auron, Benos, “*DNA Familial Binding Profiles made easy: comparison of various motif alignment and clustering strategies*” (2007) *PLoS Comput Biol* **3**: e61.