

CMU

15-826: Multimedia Databases and Data Mining

Lecture #10: Fractals - case studies - I

C. Faloutsos



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Must-read Material

 Christos Faloutsos and Ibrahim Kamel, <u>Beyond Uniformity and Independence:</u> <u>Analysis of R-trees Using the Concept of</u> <u>Fractal Dimension</u>, Proc. ACM SIGACT-SIGMOD-SIGART PODS, May 1994, pp. 4-13, Minneapolis, MN.

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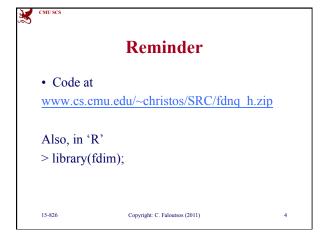
Optional Material

Optional, but **very** useful: Manfred Schroeder *Fractals, Chaos, Power Laws: Minutes from an Infinite Paradise* W.H. Freeman and Company, 1991 (on reserve in the WeH library)

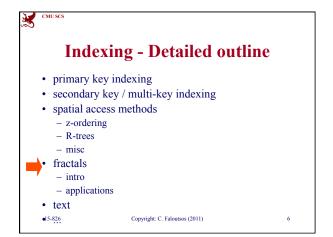


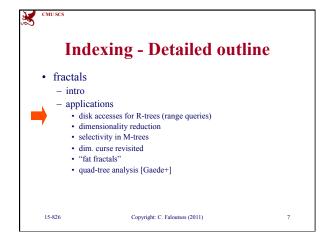
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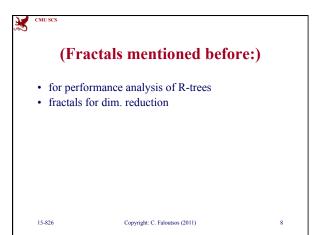
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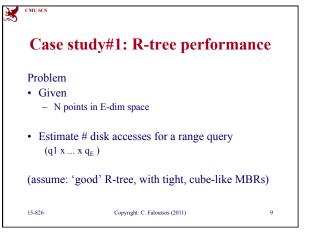


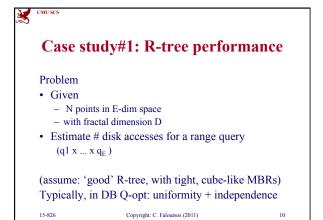


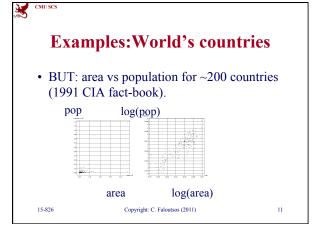


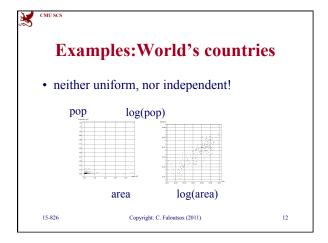


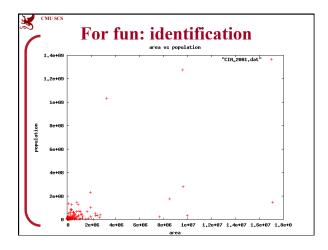


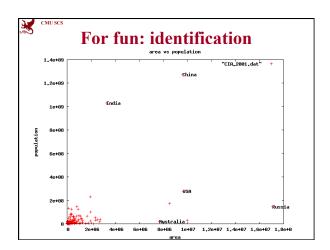


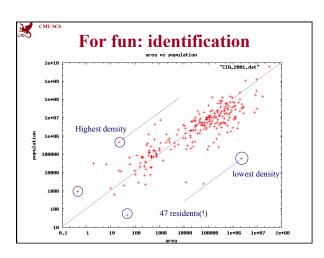


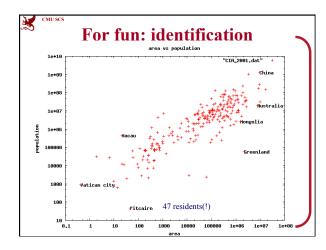


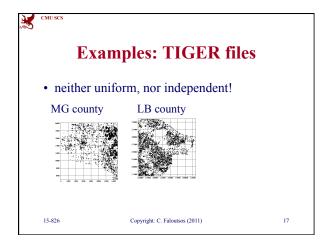




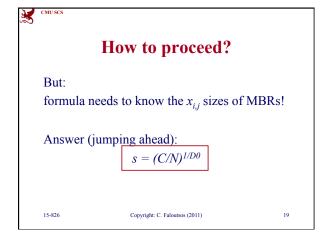


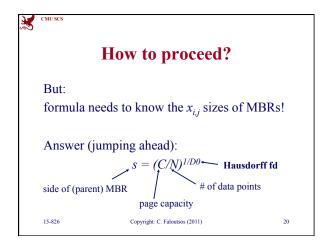




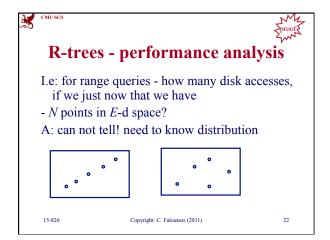


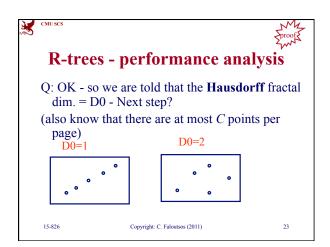
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	How to proceed?	
	• recall the [Pagel+] formula, for range queries of size q1 x q2	
	#DiskAccesses($q1,q2$) = $sum (x_{i,1} + q1) * (x_{i,2} + q2)$	
	But:	
	formula needs to know the $x_{i,j}$ sizes of MBRs!	
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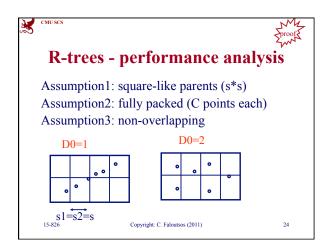




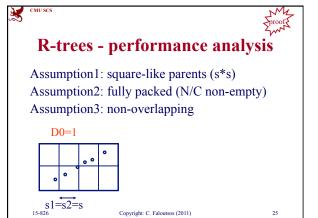
CMU SCS	Let's see the rationale	
	$s = (C/N)^{1/D\theta}$	
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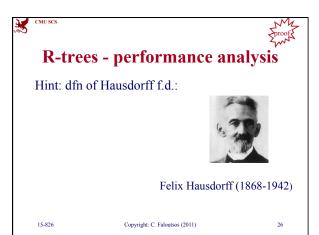


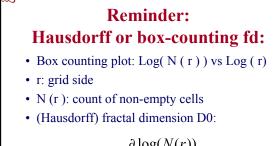




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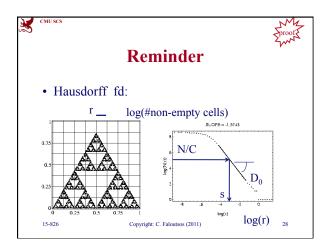


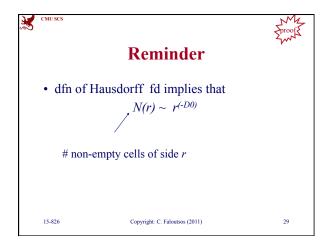
$$D_0 = -\frac{\partial \log(N(r))}{\partial \log(r)}$$

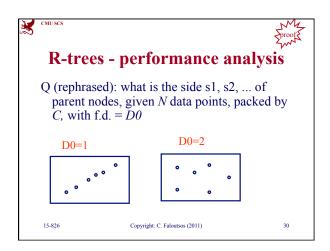
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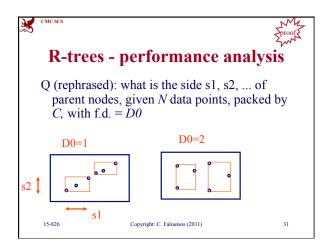
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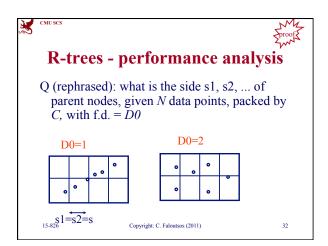
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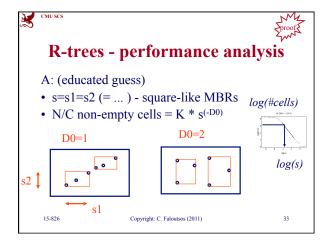


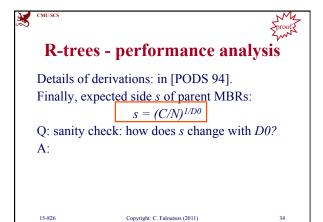


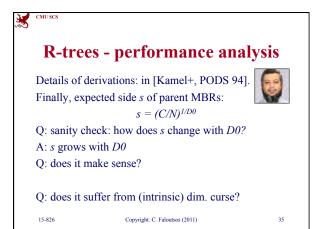


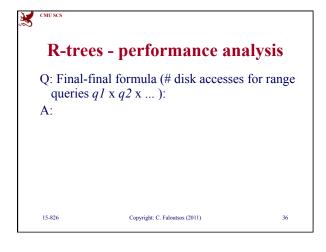












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R-trees - performance analysis

Q: Final-final formula (# disk accesses for range queries q1 x q2 x ...):

A: # of parent-node accesses:

$$N/C * (s + q1) * (s + q2) * ... (s + q_E)$$

A: # of grand-parent node accesses

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A: # of grand-parent node accesses

$$N/(C^2) * (s' + q1) * (s' + q2) * ... (s' + q_E)$$

 $s' = ??$

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R-trees - performance analysis

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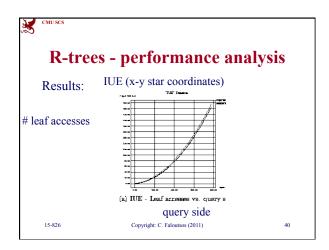
A: # of grand-parent node accesses

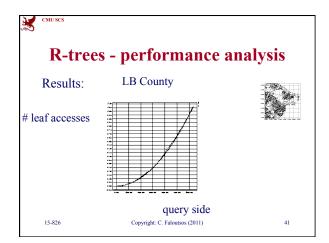
$$N/(C^2) * (s' + q1) * (s' + q2) * ... (s' + q_E)$$

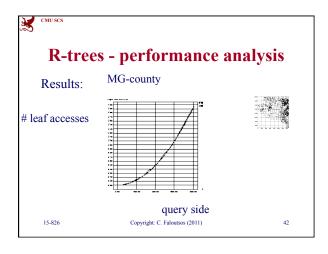
$$s' = (C^2/N)^{1/D0}$$

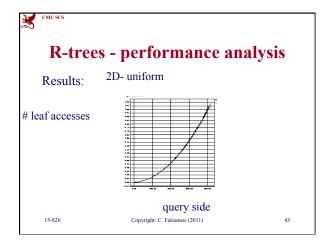
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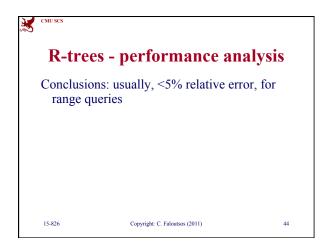
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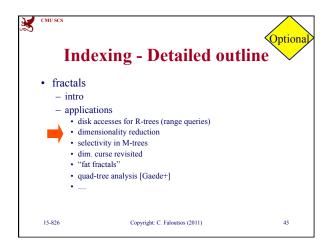


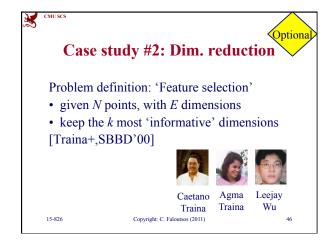


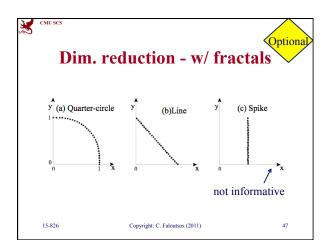


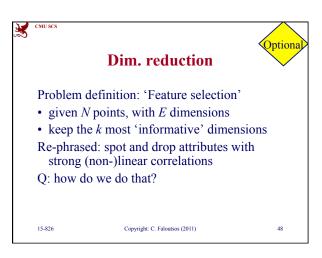


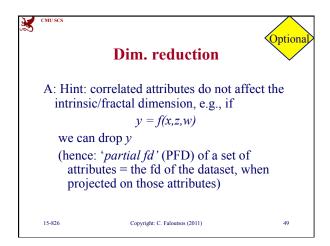


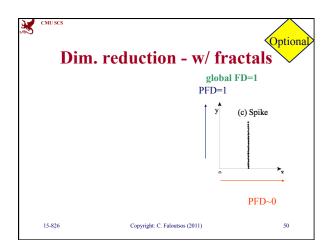


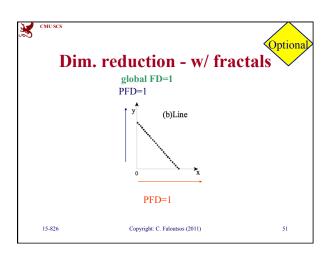


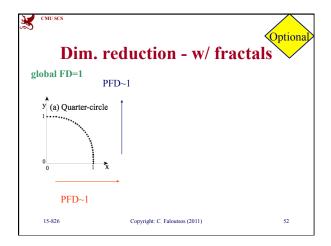


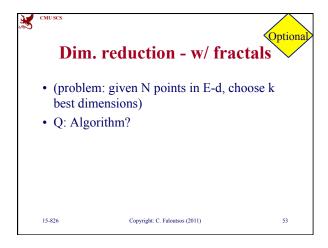


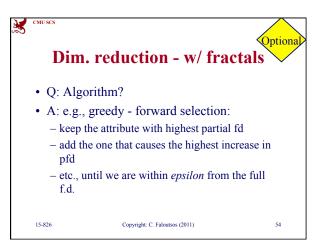


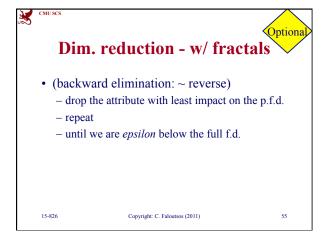


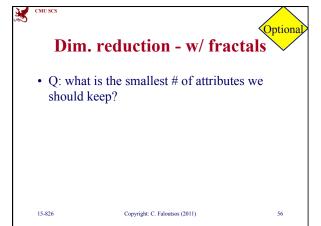


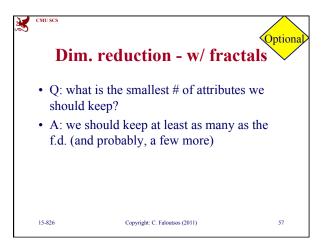


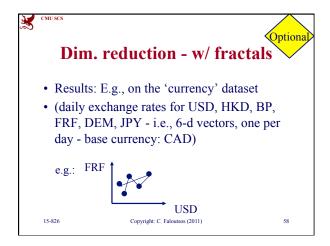


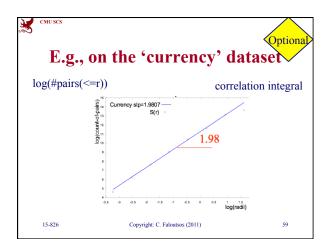


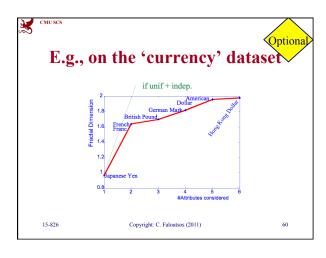


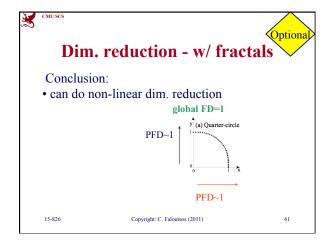












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References

- [PODS94] Faloutsos, C. and I. Kamel (May 24-26, 1994). Beyond Uniformity and Independence: Analysis of R-trees Using the Concept of Fractal Dimension. Proc. ACM SIGACT-SIGMOD-SIGART PODS, Minneapolis, MN.
- [Traina+, SBBD'00] Traina, C., A. Traina, et al. (2000). *Fast feature selection using the fractal dimension*. XV Brazilian Symposium on Databases (SBBD), Paraiba, Brazil.

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