



CMU SCS

15-826: Multimedia Databases and Data Mining

Lecture #7: Spatial Access Methods - IV
Grid files, dim. curse
C. Faloutsos



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Must-read material

- Textbook, Chapter 5.3
- Ramakrinshan+Gehrke, Chapter 28.5

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Outline

Goal: 'Find **similar** / **interesting** things'

- Intro to DB
- ➔ • Indexing - similarity search
- Data Mining

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Indexing - Detailed outline

- primary key indexing
- secondary key / multi-key indexing
- spatial access methods
 - problem dfin
 - z-ordering
 - R-trees
 - misc
- text
- ...

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SAMs - Detailed outline

- spatial access methods
 - problem dfin
 - z-ordering
 - R-trees
 - misc topics
 - grid files
 - dimensionality curse; dim. reduction
 - metric trees
 - other nn methods
- text, ...

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Grid files

- problem: spatial queries in k -d point-sets
- Main idea: try to generalize hashing to k -d
- (how?)



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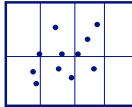
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Grid files



Jurg Nievergelt

- A: put a grid
- specs: [Nievergelt +, 84]
 - symmetric to all attributes
 - 2 disk accesses for exact match queries
 - adaptive to non-uniform distr.
- Q: details?

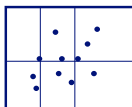


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Grid files

- cuts: all the way through
- cuts: at $\frac{1}{2}$, $\frac{3}{4}$, $\frac{1}{4}$ etc; but on demand
- each cell $\rightarrow$ disk page



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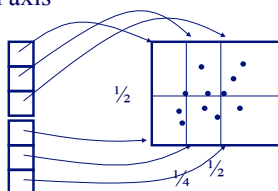
Grid files

Thus, we only need:

- cut-points for each axis
- k-d directory

x-cuts $\frac{1}{4}$ $\frac{1}{2}$

y-cuts $\frac{1}{2}$



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Grid files

Search (for exact match) – eg., (0.3; 0.3)

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Grid files

Search (for exact match) – eg., (0.3; 0.3)

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Grid files

- specs: [Nievergelt +, 84]
 - symmetric to all attributes
 - ✗ 2 disk accesses for exact match queries
 - adaptive to non-uniform distr.

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Grid files

partial match – eg., $0 < x < 0.3$

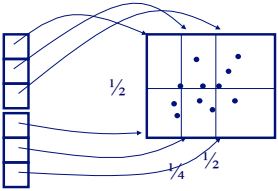
x-cuts

$\frac{1}{4}$

$\frac{1}{2}$

y-cuts

$\frac{1}{2}$



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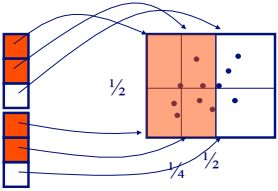
Grid files

partial match – eg., $0 < x < 0.3$

$\frac{1}{4}$

$\frac{1}{2}$

$\frac{1}{2}$



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exactly the symmetric algo for eg., $0 < y < 0.3$

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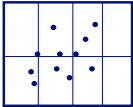
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Grid files

- specs: [Nievergelt +, 84]
- ✗ symmetric to all attributes
- ✗ 2 disk accesses for exact match queries
- adaptive to non-uniform distr.



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Grid files

Q: How to split an overflowing page?

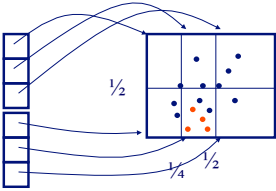
x-cuts

1/4

1/2

y-cuts

1/2



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Grid files

A: pick the ‘best’ axis, and cut all the way through

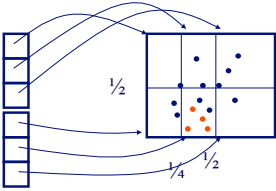
x-cuts

1/4

1/2

y-cuts

1/2



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Grid files

A: pick the 'best' axis, and cut all the way through...

x-cuts: $\frac{1}{4}$ $\frac{3}{8}$ $\frac{1}{2}$

y-cuts: $\frac{1}{2}$

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Grid files

... updating the directory appropriately (ouch!)

x-cuts: $\frac{1}{4}$ $\frac{3}{8}$ $\frac{1}{2}$

y-cuts: $\frac{1}{2}$

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Grid files

- specs: [Nievergelt +, 84]
 - ✗ symmetric to all attributes
 - ✗ 2 disk accesses for exact match queries
 - ✗ adaptive to non-uniform distr.

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Grid files

- it meets the three goals
- had follow-up work [twin grid files, multi-level; etc]
- BUT: has some disadvantages (which ones?)

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Grid files - disadvantages

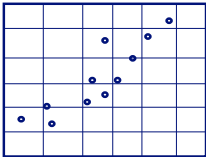
- #1: problems in high-d: directory splits can be expensive

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Grid files - disadvantages

- #2: even in low-d, suffers on correlated attributes:

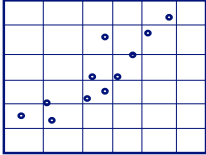


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Grid files - disadvantages

- (Q: how to fix, for 2-d, linearly correlated points?)

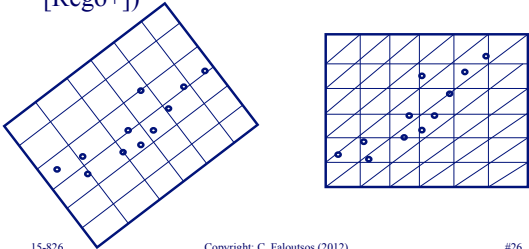


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Grid files - disadvantages

- (A1: rotate [Hinrichs+]; A2: triangular cells [Rego+])

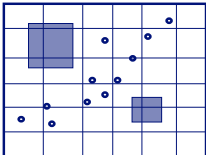


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Grid files - disadvantages

- #3: how about region data?



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Grid files - disadvantages

- #3: how about region data?
- if we ‘cut’ them, then we have $O(\text{volume})$ pieces (while z-ordering: $O(\text{surface})$)
- what to do?

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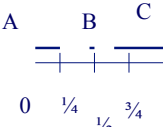
#28

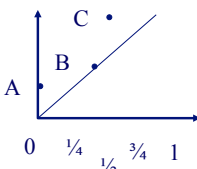
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Grid files - disadvantages

- what to do?
- Translation to 2k – d points! (clever, BUT, still has subtle problems) E.g., 1-d ‘regions’

A B C x-end





0 1/4 1/2 3/4 1 x-start

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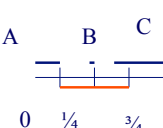
#29

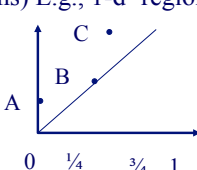
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Grid files - disadvantages

- what to do?
- Translation to 2k – d points! (clever, BUT, still has subtle problems) E.g., 1-d ‘regions’

A B C x-end





0 1/4 1/2 3/4 1 x-start

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Grid files - disadvantages

- what to do?
- Translation to 2k – d points! (clever, BUT, still has subtle problems) E.g., 1-d ‘regions’

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Grid files - disadvantages

- what is the problem, then?

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Grid files - disadvantages

- what is the problem, then?
- A: dimensionality curse; large query regions

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Grid files – conclusions

- works OK in low-d un-correlated points
- but z-ordering/R-trees seem to work better for higher-d
- smart idea to translate k-d rectangles into 2^k - points (but: dim. curse)

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SAMs - Detailed outline

- spatial access methods
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 - other nn methods
- text, ...

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Dimensionality ‘curse’

- Q: What is the problem in high-d?

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Dimensionality ‘curse’

- Q: What is the problem in high-d?
- A: indices do not seem to help, for many queries (eg., k-nn)
 - in high-d (& uniform distributions), most points are equidistant -> k-nn retrieves too many near-neighbors
 - [Yao & Yao, '85]: search effort $\sim O(N^{(1-1/d)})$

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Dimensionality ‘curse’

- (counter-intuitive, for db mentality)
- Q: What to do, then?

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Dimensionality ‘curse’

- A1: switch to seq. scanning
- A2: dim. reduction
- A3: consider the ‘intrinsic’/fractal dimensionality
- A4: find approximate nn

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Dimensionality ‘curse’

- A1: switch to seq. scanning
 - X-trees [Kriegel+, VLDB 96]
 - VA-files [Schek+, VLDB 98], ‘test of time’ award

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Dimensionality ‘curse’

- A1: switch to seq. scanning
- ➔ • A2: dim. reduction
- A3: consider the ‘intrinsic’/fractal dimensionality
- A4: find approximate nn

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Dim. reduction

a.k.a. feature selection/extraction:

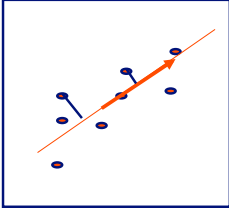
- SVD (optimal, to preserve Euclidean distances)
- random projections
- using the fractal dimension [Traina+ SBBD2000]

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Singular Value Decomposition (SVD)

- SVD ($\sim$ LSI $\sim$ KL $\sim$ PCA $\sim$ spectral analysis...)



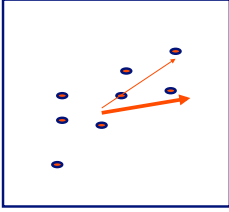
LSI: S. Dumais; M. Berry
KL: eg, Duda+Hart
PCA: eg., Jolliffe
MANY more details: soon

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Random projections

- random projections(Johnson-Lindenstrauss thm [Papadimitriou+ pods98])



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Random projections

- pick 'enough' random directions (will be $\sim$ orthogonal, in high-d!!)
- distances are preserved probabilistically, within epsilon
- (also, use as a pre-processing step for SVD [Papadimitriou+ PODS98])

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Dim. reduction - w/ fractals

- Main idea: drop those attributes that don't affect the intrinsic ('fractal') dimensionality [Traina+, SBBB 2000]

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Dim. reduction - w/ fractals

global FD=1

(a) Quarter-circle (b) Line (c) Spike

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Dimensionality 'curse'

- A1: switch to seq. scanning
- A2: dim. reduction
- ➔ A3: consider the 'intrinsic'/fractal dimensionality
- A4: find **approximate** nn

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Intrinsic dimensionality

- before we give up, compute the intrinsic dim.:
- the lower, the better... [Pagel+, ICDE 2000]
- more details: under 'fractals'

intr. d = 2





intr. d = 1

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Dimensionality 'curse'

- A1: switch to seq. scanning
- A2: dim. reduction
- A3: consider the 'intrinsic'/fractal dimensionality
- ➔ A4: find approximate nn

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Approximate nn

- [Arya + Mount, SODA93], [Patella+ ICDE 2000]
- Idea: find k neighbors, such that the distance of the k-th one is guaranteed to be within epsilon of the actual.

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Conclusions

- Dimensionality ‘curse’:
 - for high-d, indices slow down to $\sim O(N)$
- If the **intrinsic** dim. is low, there is hope
- otherwise, do seq. scan, or sacrifice accuracy (approximate nn)

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ANN library:
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