Adaptive Selectivity Estimation Using Query Feedback^{*}

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Abstract

In this paper, we propose a novel approach for estimating the record selectivities of database queries. The real attribute value distribution is adaptively approximated by a curvefitting function using a query feedback mechanism. This approach has the advantages of requiring no extra database access overhead for gathering statistics and of being able to continuously adapt the value distribution through queries and updates. Experimental results show that the estimation accuracy of this approach is comparable to traditional methods based on statistics gathering.

1 Introduction

In most database systems, the task of query optimization is to choose an efficient execution plan. Best plan selection requires accurate estimates of the *costs* of alternative plans. One of the most important factors that affects plan cost is *selectivity*, which is the number of tuples satisfying a given predicate. Therefore, in most cases, the accuracy of selectivity estimates directly affects the choice of best plan.

A study on error propagation [IC91] revealed that selectivity estimation errors can increase exponentially with the number of joins and thus affect the decisions in query optimization. Accurate selectivity estimation has become even more important in today's systems of much larger database sizes, possibly distributed over a LAN or a WAN. In such systems, the query plans are expected to diverge much more in cost due to the database size and the volume of data transmission. Nick Roussopoulos Department of Computer Science University of Maryland College Park, MD 20742 nick@cs.umd.edu

Therefore, accurate selectivity estimation is even more crucial.

The issue of selectivity estimation has attracted popular interest, and different methods have been proposed [MO79, Chr83b, Chr83a, PSC84, KK85, HOT88, Lyn88, MD88, LN90, SLRD93, Ioa93]. They can be categorized into four classes: the *non-parametric method*, the *parametric method*, *sampling*, and *curve fitting*. In the following paragraphs, we review the essential approaches for each of these four classes. A detailed survey of the first two classes can be found in [MCS88].

- Non-Parametric Method Methods in this class maintain attribute value distributions using ad hoc data structures and algorithms. The most common method is the *histogram*, which divides an attribute domain into intervals and counts the number of tuples holding values which fall into each of the intervals. Variations of the histogram method can be found in [MO79, PSC84, MD88, Lyn88, Ioa93]. The histogram is simple, but tradeoff between the computation/storage overhead and the estimation accuracy must be considered. Satisfactory accuracy will not be reached until the domain is divided into a sufficient large number of small intervals. In addition to the histogram, a pattern recognition technique was used by [KK85] to construct discrete cells of distribution table, and [Lyn88] used a keyterm-oriented approach to keep counts of the most frequently queried attribute values.
- **Parametric Method** Parametric methods approximate the actual distribution with a mathematical distribution function of a certain number of free statistical parameter(s) to be estimated (we call such a function a *model* function). Examples of the model function include the uniform, normal, Pearson family and Zipf distributions. In these methods, statistics must be collected, either by scanning through or by sampling from the relation, in order to estimate the free parameter(s). These methods usually

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require less storage overhead and provide more accurate estimation than non-parametric methods (if the model function fits the actual distribution). The disadvantage of this method is that the "shape" of the actual distribution must be known a priori in order to choose a suitable model function. Moreover, when the actual distribution is not shaped like any of the known model functions, any attempt to approximate the distribution by this method will be in vain. Contributions to research of parametric methods can be found in [S⁺79, SB83, Fed84, Chr83b, Chr83a].

- **Curve Fitting** In order to overcome the inflexibility of the parametric method, [LST83] and [SLRD93] used a general polynomial function and applied the criterion of least-square-error to approximate attribute value distribution. First, the relation is exhaustively scanned, and the number of occurrences of each attribute value is counted. These numbers are then used to compute the coefficients of the optimal polynomial that minimizes the sum of the squares of the estimation errors over all distinct attribute values. Polynomial approximation has been widely used in data analysis; however, care must be taken here to avoid the problem of oscillation (which may lead to negative values) and rounding error^{1} (which may propagate and result in poor estimation when the degree of the polynomial is high, say, more than 10).
- Sampling The sampling method has recently been investigated for estimating the resulting sizes of queries. Sample tuples are taken from the relations, and queries are performed against these samples to collect the statistics. Sufficient samples must be examined before desired accuracy can be achieved. Variations of this method have been proposed in [HOT88, LN90, HS92]. Though the sampling method usually gives more accurate estimation than all other methods (suppose suffucient samples are taken), it is primarily used in answering statistical queries (such as COUNT(...)). In the context of query optimization where selectivity estimation is much more frequent, the cost of the sampling method is prohibitive and has essentially prevented its practical use.

Although accuracy is very important for selectivity estimates, the cost of obtaining such estimates must be confined if they are to be cost effective. In all the above methods, however, extra I/O accesses to the database are required for the very purpose of collecting statistics. This procedure might be expensive and, as suggested, should be done off-line or when the system is light-loaded. In a static database where updates are rare, this overhead is acceptable. However, in the presence of updates, the procedure must be re-run either periodically or whenever the updates exceed a given threshold. This process not only incurs more overhead, but also degrades the query optimizer before the outdated statistics are refreshed.

In the following, we present a novel approach which approximates the attribute value distribution using query feedbacks and totally avoids the overhead of statistics collection. The idea is to use subsequent query feedbacks to "regress" the distribution gradually, in the hope that as queries proceed, the approximation will become more and more accurate. We say that the adaptive approximation "learns" from the query executions in the sense that it not only "remembers" and "recalls" the selectivities of repeating query predicates, but can also "infer" (predict) the selectivities of new query predicates. This approach is advantageous in the following respects:

- Efficiency Unlike the previous methods, no offline database scans or on-line sampling are needed to form the value distribution. Also, unlike all the other methods (except sampling [Wil91]), where the statistics collection and computation overhead is proportional to the relation size, the overhead of our method has a negligible cost in constant time for each query feedback, regardless of the relation size.
- Adaptation The technique we use here adapts the approximating value distribution to queries and updates. None of the previous methods achieve this. They neither take into account query information when approximating the value distribution (only relations are scanned), nor continuously adjust the distribution to updates (re-computation is invoked only after the updates exceed a threshold).

The rest of this paper is organized as follows: Section 2 describes the adaptive selectivity estimator in detail. Section 3 presents some of our experimental results. Finally, conclusions are given in Section 4.

2 Adaptive Selectivity Estimation

In this section, we describe the implementation of an Adaptive Selectivity Estimator (ASE). At the heart of our approach is a technique called *recursive least-square-error* (RLSE), which is adopted to adjust the approximating distribution according to subsequent feedbacks. Before exploring the details, we first define some notations used throughout this paper.

¹The problem caused by rounding errors is usually termed a case of being *ill-conditioned*. This can always be avoided by representing the approximating polynomial with a more *numerically stable* basis. For example, the Legendre polynomials are used as the basis in [LST83].

Let A be an attribute of relation R, and let range $D = [d_{min}, d_{max}]$ be the domain of A. In this study, we consider only numerical domains (either discrete or continuous).² Let D' be the collection of all sub-ranges of D, and define $f_A : D' \to N$ as the actual distribution of A, i.e., for each sub-range $d \subseteq D$, $f_A(d) = |\{t \in R : t.A \in d\}|$ is the number of tuples in R whose values of attribute A belong to range d. Notice that the above notation is well-defined for both discrete and continuous cases. We denote a selection query $\sigma_{l \leq R.A \leq h}(R)$, where $l \leq h$, as q = (l, h). The selectivity of query q, defined as $s = f_A([l, h])$, is the number of tuples in the query result. The query feedback from query q is then defined as $\zeta = (l, h, s)$.

2.1 Customizing RLSE for Query Feedback

The goal of our approach is to approximate f_A by an easily evaluated function f which is able to selfadjust from subsequent query feedbacks. Thus, given a sequence of queries q_1, q_2, \ldots , we can view f as a sequence f_0, f_1, f_2, \ldots where f_{i-1} is used to estimate the selectivity of q_i , and, after q_i is optimized and executed, f_{i-1} is further adjusted into f_i using feedback ζ_i (which contains the actual selectivity, s_i , of query q_i obtained after the execution).

We use a general form $f(x) = \sum_{i=0}^{n} a_i \phi_i(x)$ as the underlying approximating function, where $\phi_i(x)$, $i = 0, \ldots, n$, are n + 1 pre-chosen functions (called *model* functions), and a_i are coefficients to be adjusted from the query feedbacks. The corresponding cumulative distribution of f(x) is given as $F(x) = \sum_{i=0}^{n} a_i \Phi_i(x)$, where $\Phi_i(x)$ is the indefinite integral of $\phi_i(x)$. Using this form of approximation, the estimated selectivity of query q = (l, h), denoted by \hat{s} , is computed as:

$$\hat{s} = \int_{l}^{h+1} f(x) dx = F(h+1) - F(l) = \sum_{j=0}^{n} a_{j} [\Phi_{j}(h+1) - \Phi_{j}(l)]$$

Now suppose a sequence of query feedbacks ζ_1, \ldots, ζ_m , where $m \ge n$, have been collected. A reasonable criterion for tuning f(x) is to find the optimal coefficients a_i that minimize the sum of the squares of the estimation errors (thus referred to as *least-square-error* (LSE)):

$$\sum_{i=1}^{m} (\hat{s}_i - s_i)^2 = \sum_{i=1}^{m} (\sum_{j=0}^{n} a_j [\Phi_j(h_i + 1) - \Phi_j(l_i)] - s_i)^2.$$
(1)

The above problem can be reformulated in linear algebra form as:

$$minimize ||X * A - Y||^2, \tag{2}$$

where $||\cdot||^2$ denotes the sum of the squares of all elements in the vector, and

$$X = \begin{bmatrix} \Phi_0(h_1+1) - \Phi_0(l_1) & \dots & \Phi_n(h_1+1) - \Phi_n(l_1) \\ \Phi_0(h_2+1) - \Phi_0(l_2) & \dots & \Phi_n(h_2+1) - \Phi_n(l_2) \\ \dots & \dots & \dots \\ \Phi_0(h_m+1) - \Phi_0(l_m) & \dots & \Phi_n(h_m+1) - \Phi_n(l_m) \end{bmatrix}$$
$$Y = \begin{bmatrix} s_1 \\ s_2 \\ s_2 \end{bmatrix}, \quad A = \begin{bmatrix} a_0 \\ a_1 \\ s_1 \end{bmatrix}. \tag{3}$$

 $\begin{bmatrix} 1 & - \\ s_m \end{bmatrix}, \begin{bmatrix} 1 & - \\ s_m \end{bmatrix}, \begin{bmatrix} 1 & - \\ a_n \end{bmatrix}$ Let X^t be the transpose of X; the solution to Eq. 2 is

obtained as

$$A^* = (X^t X)^{-1} X^t Y.$$
 (4)

The above computation has one drawback; the space requirement of X and Y increases in proportion to the number of query feedbacks m, and each time a new query feedback is added, the whole thing must be re-computed. This concern can be relieved with some rearrangement of the above computation. Let $P = X^t X$ and $N = X^t Y$. It is not hard to see that P is a $n \times n$ matrix and N is a $n \times 1$ vector—both of whose dimensions are independent from the number of feedbacks m. A more careful look into P and N shows that

$$P = X^{t}X = \sum_{i=1}^{m} X_{i}^{t}X_{i}, \quad N = \sum_{i=1}^{m} X_{i}^{t}s_{i}, \quad (5)$$

where X_i is the *i*th row of X, and X_i^t its transpose. Now, let $\zeta_1, \zeta_2, \ldots, \zeta_i, \ldots$ be a sequence of query feedbacks, and A_i^* be the optimal coefficients of f(x) corresponding to the first *i* feedbacks. According to Eqs. 4 and 5 we have

$$A_i^* = P_i^{-1} N_i, \text{ for } i = n + 1, n + 2, \dots, \text{ where}$$
(6)
$$P_i = P_{i-1} + X_i^t X_i, \quad N_i = N_{i-1} + X_i^t s_i, \text{ for } i = 1, 2, \dots,$$
(7)

with initial condition $P_0 = N_0 = 0$. Note that for $i \leq n$, P_i^{-1} dose not exist and thus a default distribution (e.g., uniformity) must be used temporarily. Later in this context, we will relax this restriction. Also notice that by using Eqs. 6 and 7, only two constant size arrays, P and N, need to be maintained.

The above equations can be further transformed into another form where the expensive matrix inversion P_i^{-1} need not be explicitly computed. [You84] derived the following recursive formulas, referred to as *Recursive Least-Square-Error* (RLSE), from Eqs. 6 and 7 :

$$A_i^* = A_{i-1}^* - G_i X_i^t (X_i A_{i-1}^* - s_i),$$
(8)

$$G_{i} = G_{i-1} - (G_{i-1}X_{i}^{t}) (1 + X_{i}G_{i-1}X_{i}^{t})^{-1} (X_{i}G_{i-1}), \quad (9)$$

for i = 1, 2, ..., while A_0 and G_0 can be of any arbitrary values. In this expression, no explicit matrix inverse operation is needed, and only an $n \times n$ matrix G(called a *gain matrix*) needs to be maintained (actually,

²Non-numerical domains can be mapped into numerical ones using certain mapping techniques. The mapping functions should be provided by the database creators who know the semantic meaning of the attributes.

 $G = P^{-1}$). The computation complexity is in the order of $O(n^2)$. Since n is a pre-chosen small integer, the computation overhead per query feedback is small and is considered constant, regardless of the relation size. The initial values G_0 and A_0 may affect the convergence rate of A_i^* and, thus, the rate at which f_i converges to f_A . We describe later in this section how to initialize G_0 and A_0 with appropriate values. It is interesting to see that the computation of A_i^* resembles the technique of *stochastic approximation* [AG67], in the sense that A_i^* is adjusted from A_{i-1}^* by subtracting a correction term which is the product of the estimation error $(X_i A_{i-1}^* - s_i)$ and the gain value $G_i X_i^t$. Because of their simplicity and efficiency in both space requirement and computation, Eqs. 8 and 9 were adopted in the ASE.

Accommodating Update Adaptiveness (with Weighted LSE)

The RLSE can be further generalized to accommodate adaptability to updates. We accomplish this by associating different weights with the query feedbacks so that the outdated feedbacks can be suppressed by assigning smaller weights to them. In Eq. 1, we now associate an *importance weight* β_i to the estimation error of the *i*th query, and a fading weight α_i to the estimation errors of all the preceding queries. That is, instead of minimizing Eq. 1, we now want to minimize:

$$\sum_{i=1}^{m} [(\prod_{j=i+1}^{m} \alpha_j) \cdot \beta_i \cdot (\hat{s}_i - s_i)]^2.$$
 (10)

The recursive solution to the above is similar to Eqs. 8 and 9 (derivation details can be found in [CR94]):

$$A_{i}^{*} = A_{i-1}^{*} - \beta_{i}^{2}G_{i}X_{i}^{t}(X_{i}A_{i-1}^{*} - s_{i}), \qquad (11)$$

$$G_{i} = \left(\frac{1}{\alpha_{i}}\right)^{2}G_{i-1} - \left(\frac{\beta_{i}}{\alpha_{i}}\right)^{2}(G_{i-1}X_{i}^{t})(\alpha_{i}^{2} + \beta_{i}^{2}X_{i}G_{i-1}X_{i}^{t})^{-1}(X_{i}G_{i-1})(12)$$

for i = 1, 2, ... Intuitively, β_i s determine the "importance" of individual feedbacks; α_i s determine the "forgetting" rate of previous feedbacks. Note that Eqs. 8 and 9 offer a special case of Eqs. 11 and 12 with $\alpha_i = \beta_i = 1$, for all *i*. Apparently, different weights affect the adaptation behavior of the approximating function. As an innovation, we consider only fixed-value weights. We set $\beta_i = \alpha_i = 1$ for all *i*, except that α_i is assigned another positive number less than 1 if ζ_i is the first feedback after update. The smaller the α_i , the more the knowledge from previous feedbacks is to be forgotten. Note that we cannot set $\alpha_i = 0$, because it appears as a denominator in Eq. 12. Nonetheless, the same effect (of discarding all previous knowledge) can be achieved by assigning an extremely small number to α_i . Experiments with different values of α_i are given in the next section.

Initializing A_0 and G_0

The initial values of G_0 and A_0 must be determined before the recursive formulas in Eqs. 11 and 12 can be used. Theoretically, arbitrary initial values can be used for G_0 and A_0 [You84], though they differ greatly in convergence rates. To speed up convergence, we compute A_0^* and $G_0(=P_0^{-1})$ using Eqs. 4 and 5 by substituting the following (n+1) manual feedbacks into Eq. 3:

$$l_i = h_i = d_{min} + \frac{i-1}{n-1} * \Delta, \ s_i = \frac{|R|}{\Delta}, \ \text{for } i = 1 \dots n$$
 (13)

$$l_{n+1} = d_{min}, \ h_{n+1} = d_{max}, \ s_{n+1} = |R|, \tag{14}$$

where $\Delta = d_{max} - d_{min}$, |R| denotes the number of tuples in relation R. The intention here is to force ASE to begin with a uniform distribution (enforced by Eq. 13), and to keep knowledge of the relation cardinality in the gain matrix (enforced by Eq. 14).

Choosing the Model Functions

The remaining problem now is to choose the model functions $\phi_i(x)$. The polynomial function is a good candidate due to its generality and simplicity and has been used in [LST83] and [SLRD93]. We adopted polynomials of degree 6 throughout our experiments, i.e., the approximating function is of the form $f(x) = \sum_{i=0}^{6} a_i x^i$. Whereas polynomials of higher degrees have the pontential problem of being ill-conditioned, polynomials of lower degrees might not be flexible enough to fit the variety of actual distributions. Therefore, our choice of degree 6 is a compromise between these concerns 3 . Another interesting class of functions is the *spline* functions [dB78], which are piecewise polynomial functions. Splines have many advantages over polynomials in the aspects of adaptability and numerical stability. However, they are more complex in computation and particularly in representation. We are currently investigating this approach and will not discuss it here.

A practical problem of polynomials is the negative values which are undesired in distribution approximations. This poses no problem so long as the negative values occur only outside the attribute domain, or so long as the resulting estimated selectivity of the query of interest is still positive (even if some negative values do occur within the domain). If a negative selectivity is ever estimated for a query, we simply use zero instead (and note that if the error is large, it will be tuned

³ In our experiments using degree 6, the "ill-conditioned" problem did not arise. However, for higher degrees we might need to use another basis (such as Legendre polynomials or B-splines) since the basis of x^i , i = 1, ..., n is in general ill-conditioned for large values of n.

through feedback). Finally, we summarize ASE in the following description.

Variables

- A: the (adaptable) coefficients of a polynomial f of degree 6; let F be the indefinite integral of f;
- G: the gain matrix;

Initialization

Use the manual feedbacks listed in Eqs. 13 and 14 to compute the initial values for A and G from Eqs. 3, 4 and 5.

Selectivity Estimation

The selectivity of query $q_i = (l_i, h_i)$ is estimated as $F(h_i + 1) - F(l_i)$; if it is negative, simply return 0.

Feedback and Adaptation

After the execution of q_i , get feedback $\zeta_i = (l_i, h_i, s_i)$ where s_i is the actual selectivity of q_i obtained from execution. If q_i is the first query after the latest update, set the fading weight α_i to a positive number less than 1. Use ζ_i to adjust Aand G, as shown in Eqs. 11 and 12.

Comparison with [SLRD93]

Sun, Ling, Rishe, and Deng proposed in [SLRD93] a method of approximating the attribute distribution using a polynomial with the criterion of least-squareerror. While both their method and ours use polynomial approximations, there are several differences between the two methods. First, their approach is *static* in the sense it is necessary to scan the database and count the frequencies of distinct attribute values, and, once computed, the approximating distribution remains unchanged until the next re-computation. Our method is *dynamic* and depends only on query feedbacks, with no access to the database. For a relation which is large and/or is updated regularly, the overhead of collecting or refreshing the statistics can be very expensive. Our approach totally avoids such overhead. Besides, in an environment where queries exhibit highly temporal or spatial locality on certain attribute ranges, ASE's dynamic adaptation to queries will perhaps be of greater benefit. Finally, ASE's adaptiveness to updates not only eliminates the overhead of statistics re-collection, but also provides a more graceful performance degradation for selectivity estimations through a query session interleaved with updates.

2.2 An Example

We use an example to demonstrate how the ASE works by using successive query feedbacks to approximate the data distribution. The experimental data is from a

	queries	1	2	2 3	
	$[l_i, h_i]$	[1935, 1966]	[1925, 1950]	[1904, 1939]	[1890, 1923]
	s î	1073	1138	1248	567
	<i>s</i> _i	1872	1399	890	136
	5	6	7	8	9
[1908, 1913]		[1948, 1989]	[1957, 1980]	[1964, 1989]	[1916, 1981]
2		1956	1103	1041	3173
14		2033	1130	1134	3045



Figure 1: Adaptation Dynamics of ASE - an Example

movie database, courtesy of Dr. Wiederhold of Stanford University, which records 3424 movies produced during the years 1890-1989. Figure 1 snapshots the evolution of the approximating distribution for a sequence of query feedbacks. The queries are listed in the table, where $[l_i, h_i]$ denotes the selected range of the *i*th query, \hat{s}_i denotes the selectivity estimated (by ASE) before the query execution, and s_i denotes the actual selectivity obtained after the query execution. In each frame, the curve of the approximating distribution f_i , drawn in solid line, is compared to the real distribution, drawn in discrete points. In frame 1, uniform distribution is assumed at the very beginning, as no queries have been issued. Note that knowledge of the relation cardinality (3424 tuples) has been implicitly enforced in the initial approximating distribution f_0 , using the initialization scheme explained in the previous section. After the execution of two queries, as shown in frame 2, the approximating curve becomes closer to the actual distribution. However, f_2 is relatively inaccurate for attribute ranges outside [1925, 1966] which have not been queried yet (and, thus, no distribution information is yet known). The third query and its feedback $\zeta_3 = (1904, 1939, 890)$ tunes f_2 into f_3 with better accuracy for range [1904, 1939]. It is worth mentioning that at the same time, f_3 improves the distribution of years greater than 1966, though no queries against this range have ever been posed. This is attributed to ASE's ability to infer and properly shape the unknown ranges using knowledge about the relation cardinality and distribution information obtained from queries on other attribute ranges. Subsequently, frame 4 shows the curve after nine query feedbacks, by which time the approximation has become even closer to the real distribution.

3 Experimental Results

A comprehensive set of experiments was performed to evaluate the ASE. We ran the experiments using the mathematics package MAPLE, developed by the Symbolic Computation Group of the University of Waterloo; MAPLE was chosen for its provision of immediate access to matrix operations and random number generators. We experimented also with the method proposed in [SLRD93] (referred to as SLR in what follows) for comparisons whenever appropriate. The selectivity estimation errors and the adaptation dynamics of ASE were observed and graphed for demonstration. However, to interpret and compare the estimation errors correctly, both *absolute error* and *relative error* are presented; they are calculated as:

abs. err.
$$= \frac{|\hat{s} - s|}{|R|} \times 100$$
, rlt. err. $= \frac{|\hat{s} - s|}{s} \times 100$

where \hat{s} and s are the estimated and actual query result sizes, respectively; |R| is the cardinality of the queried relation. Our reason for using both is that neither one alone can provide evidence of good or poor estimation in all cases. For example, a 200% relative error for a query of selectivity of 1 tuple by no means represents a poor estimate; in fact, it is the stringent selectivity (of 1 tuple) that causes such an exaggerated relative error. It must be pointed out that we do not compare the computation overhead since our method, which costs only negligible CPU time for query feedback computation, is definitely superior to all other methods which require extra database accesses (either off-line or on-line) for statistics gathering or sampling.

Both real and synthetic data were used in the experiments. The use of real data validates the usefulness of our method in practice (as has been demonstrated in the example); the use of synthetic data allows systematic evaluation of ASE under diverse data and query distributions. Throughout the experimentation, only selection queries were considered. Each query is represented as a range $[x - \delta/2, x + \delta/2]$, where $d_{min} \leq x \leq d_{max}$, $0 \leq \delta \leq d_{max} - d_{min}$. In this paper, we report only results from those experiments where x and δ are generated randomly from their respective domains using

Notations	Meaning
$N(\mu, \sigma)$	normal distribution with mean μ_1 standard
	deviation σ
$\chi^2(n)$	chi-square distribution with n degrees of freedom
F(m, n)	F distribution with m and n degrees of freedom
	for numerator and denominator, respectively
$B(u_{1+}\sigma_{1+}$	a bi-modal distribution which is an overlap of
$u_{2}, \sigma_{2})$	$N(u_1,\sigma_1)$ and $N(u_2,\sigma_2)$

Table 1: <u>Distribution Notations</u>

Distribution	$\begin{bmatrix} d_{min}, d_{max} \end{bmatrix}$	cardinality
N(200, 150)	-150,550	10,000
$\chi^{2}(10)$	[0, 1200]	20,000
F(10, 4)	[0, 800]	10,000
B(250,150,450,50)	[-150, 550]	12,500

Table 2: Customized Experiment Parameters

	avera	ge error of 1	lst - 50th queries				
	ASE		$_{\rm SLR}$				
	abs. err.	rlt. err.	abs. err.	rlt. err.			
N	0.73	4.43	0.16	2.4			
χ^2	1.36	13.0	0.33	8.0			
F	2.2	28.6	1.7	28.2			
B	1.40	8.75	0.60	3.08			
-							
	average error of 10th - 50th queries						
	ASE		SLR				
	abs. err.	rlt. err.	abs. err.	rlt. err.			
N	0.16	3.66	0.16	2.73			
χ^2	0.33	8.36	0.40	8.93			
F	1.10 15.3		1.76	30.1			
B	0.80	5.11	0.60	3.13			

Table 3: Average Errors in Various Data Distributions

a random number generator. Experimental results regarding the impacts of different distributions of x and δ on the convergence rate of ASE are prepared in a more detailed version of this paper.

Three sets of experimental results are presented here. The first set shows the adaptability of ASE to various data distributions. The second set shows how ASE adapts to *query locality*, in the sense that it provides more accurate selectivity estimates for the attribute sub-ranges which are queried most. In the last set, we demonstrate ASE's elegant adaptation through database updates which require no overhead for database re-scan and statistics re-computation.

3.1 Adaptation to Various Distributions

To observe ASE's adaptability to various data distributions, synthetic data generated from each of the following four customized distributions were tested: normal distribution, chi-square distribution, the F distribution, and a "bi-modal" distribution.⁴ The notations and customized parameters of each distribution are described in Tables 1 and 2. For each data distribution, three random query streams (each of which contains 50 queries)

⁴We do not present the results of uniform distribution since the ASE assumes uniform distribution from the very beginning.

were run for both ASE and SLR.

Table 3 lists the average error per query of ASE and SLR under each data distribution. In order to achieve a fair comparison between ASE and SLR, the average errors, which exclude the first 10 queries of each query stream (during which ASE is still in its "learning" stage), are also calculated for comparison. The first table shows that ASE is slightly inferior to SLR in estimation accuracy; however, the second table shows that after ASE converges (after 10 queries), its accuracy is very comparable to that of SLR. Figures 2 through 5 depict the corresponding dynamics of ASE and SLR for one of the query streams under each data set. In the figures to the left marked (a), curve g corresponds to the approximating distribution computed from SLR; curve f_i denotes the adaptive approximating distribution of ASE after i query feedbacks. Figures (b) compare the estimation errors of ASE and SLR by plotting them along with the query streams. The adaptiveness of ASE can be clearly observed from the decreasing trend of errors as queries proceed. The occasionally high relative errors of ASE are either caused by stringently small selectivities (as evidenced by the high relative errors of SLR for the same queries), or are indications of the moments where feedbacks take place for the first time on the queried ranges. However, as can be seen from all the figures, after sufficient query feedbacks have covered the whole attribute domain, ASE converges the approximating distribution to a stable curve and provides estimations with constantly small errors.

3.2 Adaptiveness of ASE to Query Locality

No matter what method is used to estimate the data distribution, the computation *capacity* of the method is always limited (e.g., the *number of intervals* in a histogram, the *degree* of a polynomial). It is not uncommon for the distribution to be approximated to be too detailed to be modeled by the limited capacity. Therefore, we believe that instead of approximating the overall distribution evenly, the limited capacity should be used to approximate more accurately the local distribution of a rather narrow attribute subrange which imposes either a temporal or spatial query locality. ASE inherits this merit: the more query feedbacks obtained from a local area, the more accurate the resulting approximating distribution for this area.

An "event" database which contains 431,258 records of events during 1948-1978 was used in this experiment. Three levels of query localities, as outlined in Table 4, were designed to compare ASE and SLR. For each level of locality, three random query streams (each of which contains 50 queries) were tested for both ASE and SLR. Table 5 summarizes the average errors for the 10th to 50th queries (we excluded the first 10 queries during

	Queried Range	Locality
LowQL	Jan. 1948 - Dec. 1978	Low
MedQL	Jan. 1948 - June 1960	Medial
HighQL	Jan. 1948 - Jan. 1953	High

Table 4: Three Levels of Query Localities

	ASE		SLR		
	abs. err.	rlt. err.	abs. err.	rlt. err	
LowQL	1.1	5.6	0.93	5.0	
MedQL	0.33	6.3	0.66	10.6	
HighQL	HighQL 0.086		0.14	21.3	

 Table 5: Average Errors in Different Query Localities

which ASE has not yet converged). The curves of the approximating functions and the estimation errors of ASE and SLR are graphed for comparison, according to the three levels of localities, in Figures 6, 7, and 8. It can be seen both from the tables and figures that ASE and SLR behave almost the same for low locality, but that as locality increases, ASE turns out to be better. This is because ASE is computed dynamically according to the query feedbacks and thus implicitly takes into account the query locality; in contrast, SLR is statically computed from the underlying data.

3.3 Adaptiveness to Updates (ASE Performance under Updates)

In this section, we show the elegant adaptation of ASE to updates. The normal distribution data from Section 3.1 is used again. Table 6 briefs the characteristics of three different update workloads to be interleaved with the query streams (more details about the update workloads are given in the appendix). Orthogonal to the update loads are three versions of ASE, namely, $ASE_{0.01}$, $ASE_{0.1}$, and $ASE_{0.5}$, with different fading weights (as indicated in the subscripts). For each update workload, three random query streams (each of which contains 40 selection queries interleaved with updates) are generated, and each of them is tested with all three fading weights. Table 7 tabulates the average errors; Figures 9, 10, and 11 correspond to the adaptation dynamics of ASE in the three different update loads. The corresponding curves for the three fading weights are grouped and graphed in each figure.

It can be seen from the figures that ASE adapts elegantly to all update loads. For example, in Figure 9.b, the errors go up over a few queries after the 10th query where update occurs, and then decline back to a stable low level. This adaptation can also be observed in Figure 9.a, where frames 2 through 4 show the adaptation of the approximating curves to the local distribution change at interval [-50, 250]. It is interesting to note from Table 7 that ASE_{0.01}, ASE_{0.1}, and ASE_{0.5} are respectively the best in update loads LOAD1, LOAD3,

	update occurrences	no. of total tuples updated	change of distribution shape	update transition
LOAD1	at 11	4,500	local, big increase	in batch
LOAD2	at 11, 17, 23, 29	000,9	global, slightly increase	gradual
LOAD3	at 11, 17, 23, 29	9,000	global, drastic	gradual

Update	ASE_{α}	=0.01	ASE_{α}	=0.1	ASE_{α}	= 0.5
Workload	abs. err.	rlt. err.	abs. err.	rlt. err.	abs. err.	rlt. err
LOAD1	3.38	16.7	3.58	25.7	4.71	30.0

2.66

4.19

 Table 6: Characteristics of Three Update Workloads

Table 7: Ave. Errors in Different Update Workloads

and LOAD2. This is no surprise since in LOAD1, a vast amount of update is done at once and thus it is advantageous to forget previous feedbacks and rely mainly on new ones. Therefore, the smallest fading weight $ASE_{0.01}$ (which forgets previous feedbacks to the greatest extent) outperforms the other two in this case. Similarly, in LOAD2, the shape of the distribution does not change too much during successive updates, and thus $ASE_{0.5}$ benefits the most by using old knowledge during transition. Finally, in LOAD3, where the distribution shape changes greatly through gradual updates, the use of $ASE_{0.1}$ offers a compromise between the two extremes.

LOAD2

LOAD3

3.35

5.58

22.2

31.0

4 Conclusions

In this paper, we have presented a new approach for selectivity estimation. Capitalizing on the technique of recursive weighted least-square-error, we devised an adaptive selectivity estimator which uses query feedbacks to approximate the actual attribute distribution and to provide efficient and accurate estimations. The most significant advantage of this approach over traditional methods is that it incurs no extra cost for gathering database statistics. Furthermore, it adapts better to updates and query localities.

We hope this study will inspire a new direction for data knowledge acquisition, especially in systems where statistics gathering is cost prohibitive because of large data sizes (such as tertiary databases). The adaptive selectivity estimator can be further improved in several ways and explored in several directions. First, we will refine the feedback mechanism so that adaptation will stop after the approximating distribution converges and will be triggered after updates. We would also like to extend this work to complex queries which involve compound predicates or joins. Lastly, mathematical analysis of ASE is desired in order to give deeper insight into its performance behavior under diverse query distributions and into its theoretical limits.

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2.59

4.24

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15.9

21.6

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21.3

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Appendix

Specifications of Update Workloads

In our experiments, an update query is simulated by its effect on the value distribution of the attribute of interest. An update query is specified by five parameters:

$$(i, N, D, [min, max], prob_{INS}),$$

where *i* means this update takes place immediately before the *i*th query in the query stream. *N* is the number of tuples updated (either inserted or deleted). Each tuple's attribute value is randomly generted from range [min,max] according to a distribution *D*. A tuple is inserted with probability $prob_{INS}$ or deleted with probability $1 - prob_{INS}$. Three different update workloads are tested, each of which is interleaved with another 40 random selection queries. The three update workloads are specified in the following, with U(x, y)denotes the uniform distribution among range [x, y], $N(\mu, \sigma)$ the normal distribution with mean μ and standard deviation σ .

- **LOAD1**: (11, 4500, U(-50, 250), [-50, 250], 1.0)
- $$\begin{split} \mathbf{LOAD2:} & (11, 2250, U(-150, 550), [-150, 550], 0.75), \\ & (17, 2250, U(-150, 550), [-150, 550], 0.75), \\ & (23, 2250, U(-150, 550), [-150, 550], 0.75), \\ & (29, 2250, U(-150, 550), [-150, 550], 0.75). \\ \mathbf{LOAD3:} & (11, 3000, N(-63, 50), [-150, 25], 0.9), \\ & (17, 1500, N(112, 40), [25, 200], 0.1), \\ & (23, 2250, N(290, 60), [200, 375], 1.0), \\ & (29, 2250, N(455, 50), [375, 550], 0.4). \end{split}$$





