15-859(B) Machine Learning Learning finite state environments

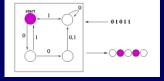
Avrim Blum 04/02/12

Consider the following setting

- Say we are a baby trying to figure out the effects our actions have on our environment...
 - Perform actions
 - Get observations
 - Try to make an internal model of what is happening.

<u>A model: learning a finite state</u> <u>environment</u>

- Let's model the world as a DFA. We perform actions, we get observations.
- Our actions can also change the state of the world. # states is finite.



Another way to put it

We have a box with buttons and lights.



- Can press the buttons, observe the lights.
 lights = f(current state)
 next state = g(button, current state)
- · Goal: learn predictive model of device.

Learning a DFA

In the language of our standard models...

- Asking if we can learn a DFA from Membership Queries.
 - Issue of whether we have counterexamples (Equivalence Queries) or not.

[for the moment, assume not]

- Also issue of whether or not we have a reset button.

[for today, assume yes]

<u>Learning DFAs</u>



This seems really hard. Can't tell for sure when world state has changed.

Let's look at an easier problem first: state = observation.



An example w/o hidden state

2 actions: a, b.



Generic algorithm for lights=state:

- ·Build a model.
- ·While not done, find an unexplored edge and take it.

Now, let's try the harder problem!

Some examples

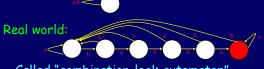
Example #1 (3 states)

Example #2 (3 states)

Can we design a procedure to do this in general?

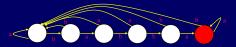
One problem: what if we always see the same thing? How do we know there isn't something else out there?

Our model:



Called "combination-lock automaton"

Can we design a procedure to do this in general?



Combination-lock automaton: basically simulating a conjunction.

This means we can't hope to efficiently come up with an exact model of the world from just our own experimentation. (I.e., MQs only).

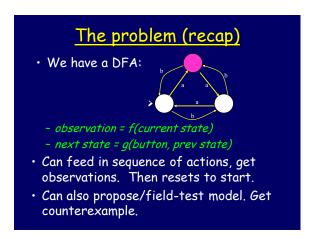
How to get around this?

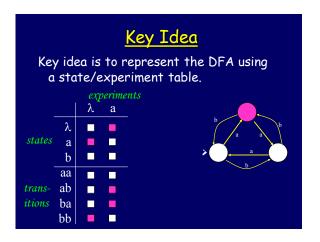
- · Assume we can propose model and get counterexample. (MQ+EQ)
- · Equivalently, goal is to be predictive. Any time we make a mistake, we think and perform experiments. (MQ+MB)
- Goal is not to have to do this too many times. For our algorithm, total # mistakes will be at most # states.

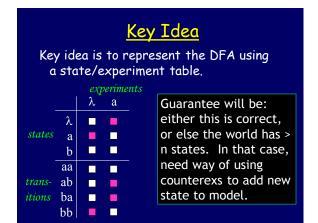
Algorithm by Dana Angluin

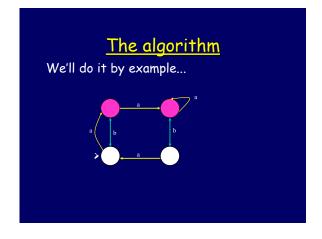
(with extensions by Rivest & Schapire)

- To simplify things, let's assume we have a RESET button. [Back to basic DFA problem]
- · Can get rid of that using something called a "homing sequence" that you can also learn.









Algorithm (formally) Begin with S = {λ}, E = {λ}. 1. Fill in transitions to make a hypothesis FSM. 2. While exists s ∈ SA such that no s' ∈ S has row(s') = row(s), add s into S, and go to 1. 3. Query for counterexample z. 4. Consider all splits of z into (p_i, s_i), and replace p_i with its predicted equivalent α_i ∈ S. 5. Find α_ir_i and α_{i+1}r_{i+1} that produce different observations. 6. Add r_{i+1} as a new experiment into E.go to 1.