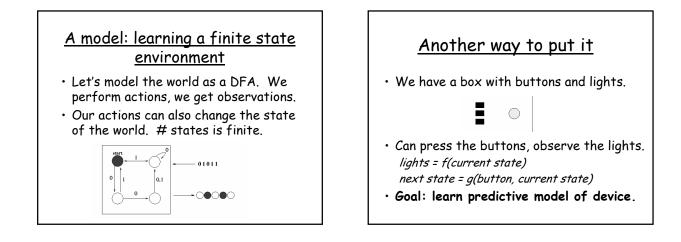
<u>15-859(B) Machine Learning</u> Learning finite state environments

Avrim Blum 03/26/08

Consider the following setting

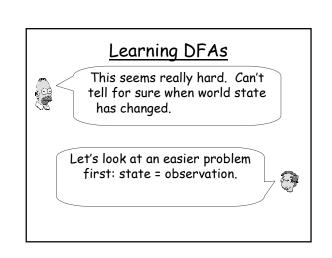
- Say we are a baby trying to figure out the effects our actions have on our environment...
 - Perform actions
 - Get observations
 - Try to make an internal model of what is happening.

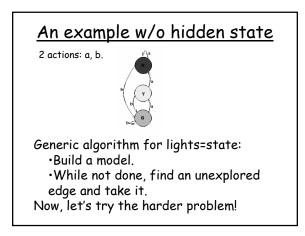


Learning a DFA

In the language of our standard models...

- Asking if we can learn a DFA from Membership Queries.
 - Issue of whether we have counterexamples (Equivalence Queries) or not.
 - [for the moment, assume not]
 - Also issue of whether or not we have a reset button.
 - [for today, assume yes]

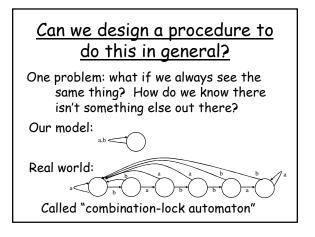


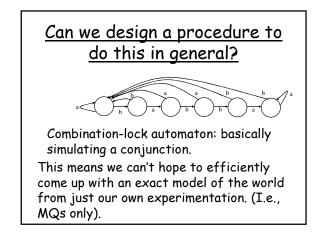




Example #1 (3 states)

Example #2 (3 states)





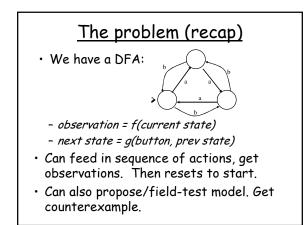
How to get around this?

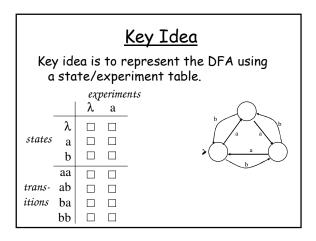
- Assume we can propose model and get counterexample. (MQ+EQ)
- Equivalently, goal is to be predictive. Any time we make a mistake, we think and perform experiments. (MQ+MB)
- Goal is not to have to do this too many times. For our algorithm, total # mistakes will be at most # states.

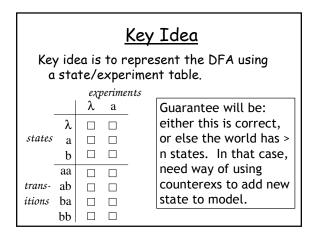
Algorithm by Dana Angluin

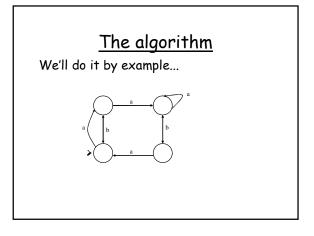
(with extensions by Rivest & Schapire)

- To simplify things, let's assume we have a RESET button. [Back to basic DFA problem]
- Can get rid of that using something called a "homing sequence" that you can also learn.









Algorithm (formally)

Begin with $S = \{\lambda\}, E = \{\lambda\}$.

- 1. Fill in transitions to make a hypothesis FSM.
- 2. While exists $s \in SA$ such that no $s' \in S$ has row(s') = row(s), add s into S, and go to 1.
- 3. Query for counterexample z.
- 4. Consider all splits of z into (p_i, s_i) , and replace p_i with its predicted equivalent $\alpha_i \in S$.
- 5. Find $\alpha_i r_i$ and $\alpha_{i+1} r_{i+1}$ that produce different observations.
- 6. Add r_{i+1} as a new experiment into E.go to 1.